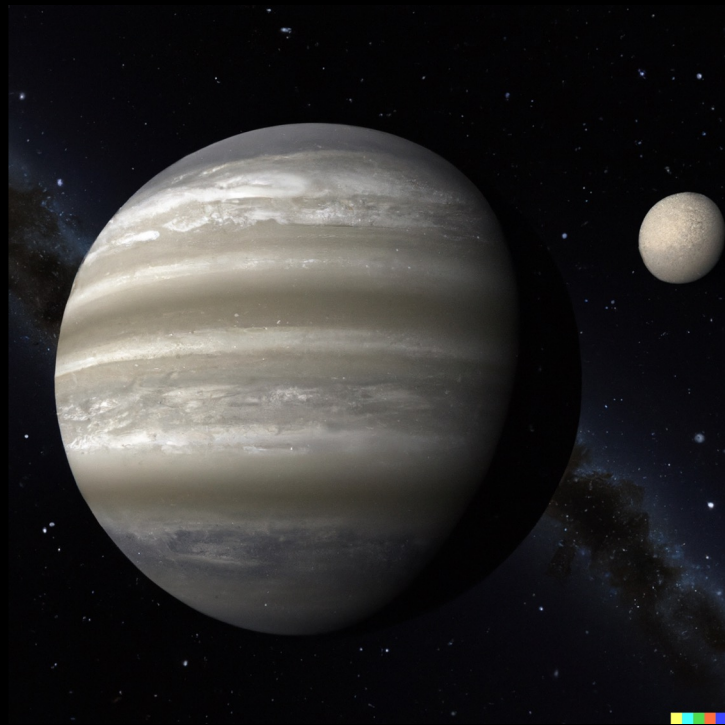


# Resolved BD Companions: Combining Gaia and Direct Imaging

G. Mirek Brandt  
Sagan Workshop 2022

# Outline

- Importance of Brown Dwarfs (BDs)
- Tools to derive masses
- Understanding 1d measurements from Gaia/Hipparcos.
- Fitting orbits/masses to 1d measurements.








# Based on work by











Yiting Li, Tim Brandt, Daniel Michalik, Minghan Chen, Trent Dupuy, Brendan Bowler, Thayne Currie, and many others...

On systems such as HR 8799, beta pic, Gl 229, Gl 758, 51 Eri, and more!

## Precise Dynamical Masses and Orbital Fits for $\beta$ Pic b and $\beta$ Pic c


G. Mirek Brandt<sup>4,1</sup> , Timothy D. Brandt<sup>1</sup> ,  
Trent J. Dupuy<sup>2</sup> , Yiting Li<sup>1</sup> , and Daniel Michalik<sup>5,3</sup> 

## Improved Dynamical Masses for Six Brown Dwarf Companions Using Hipparcos and Gaia EDR3

G. Mirek Brandt<sup>9,1</sup> , Trent J. Dupuy<sup>2</sup> , Yiting Li<sup>1</sup> ,  
Minghan Chen<sup>1</sup>, Timothy D. Brandt<sup>1</sup> ,  
Tin Long Sunny Wong<sup>1</sup> , Thayne Currie<sup>3,4,5</sup> ,  
Brendan P. Bowler<sup>6</sup> , Michael C. Liu<sup>7</sup> ,  
William M. J. Best<sup>6</sup> , and Mark W. Phillips<sup>8</sup> 

## Limits on the mass and initial entropy of 51 Eri b from *Gaia* EDR3 astrometry

[Get access >](#)

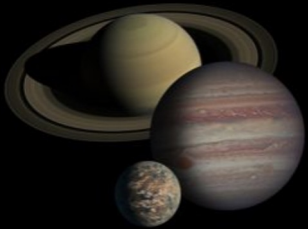
Trent J Dupuy , G Mirek Brandt, Timothy D Brandt

Brown  
Dwarfs



~13x to 80x  
Jupiter's mass

Planets &  
Exoplanets



Up to ~13x  
Jupiter's mass

**Brown Dwarfs bridge  
the gap between  
planet & star  
formation**

**Stars**

(Fueled by Nuclear Fusion)



Over ~80x  
Jupiter's mass

# The masses of BD's and Giant Planets are key






An *independently* measured mass can tell us

- 1. How old the companion is *and*
- 2. How the companion formed\* and/or which model(s) it matches

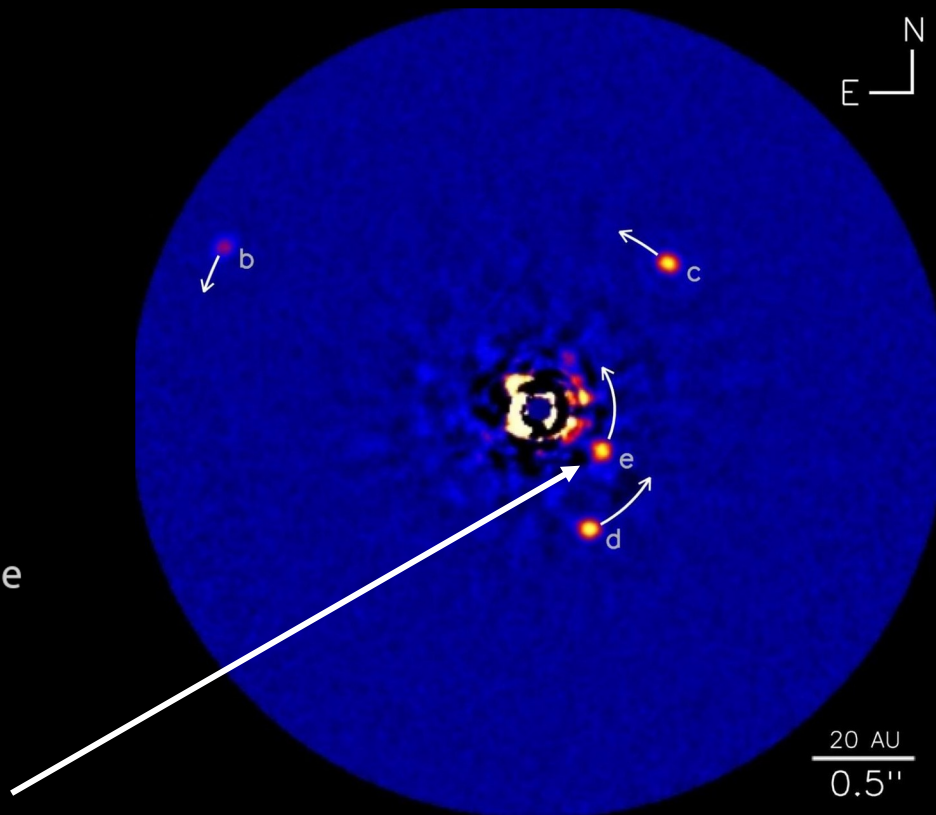
\* E.g., differences between cold/hot starts, e.g., Marleau, G. -D. ; Cumming, A. 2014 , or application to Beta pic b/c (Nowak et al. 2020, A&A 642)

# The age and mass of the innermost HR 8799 planet

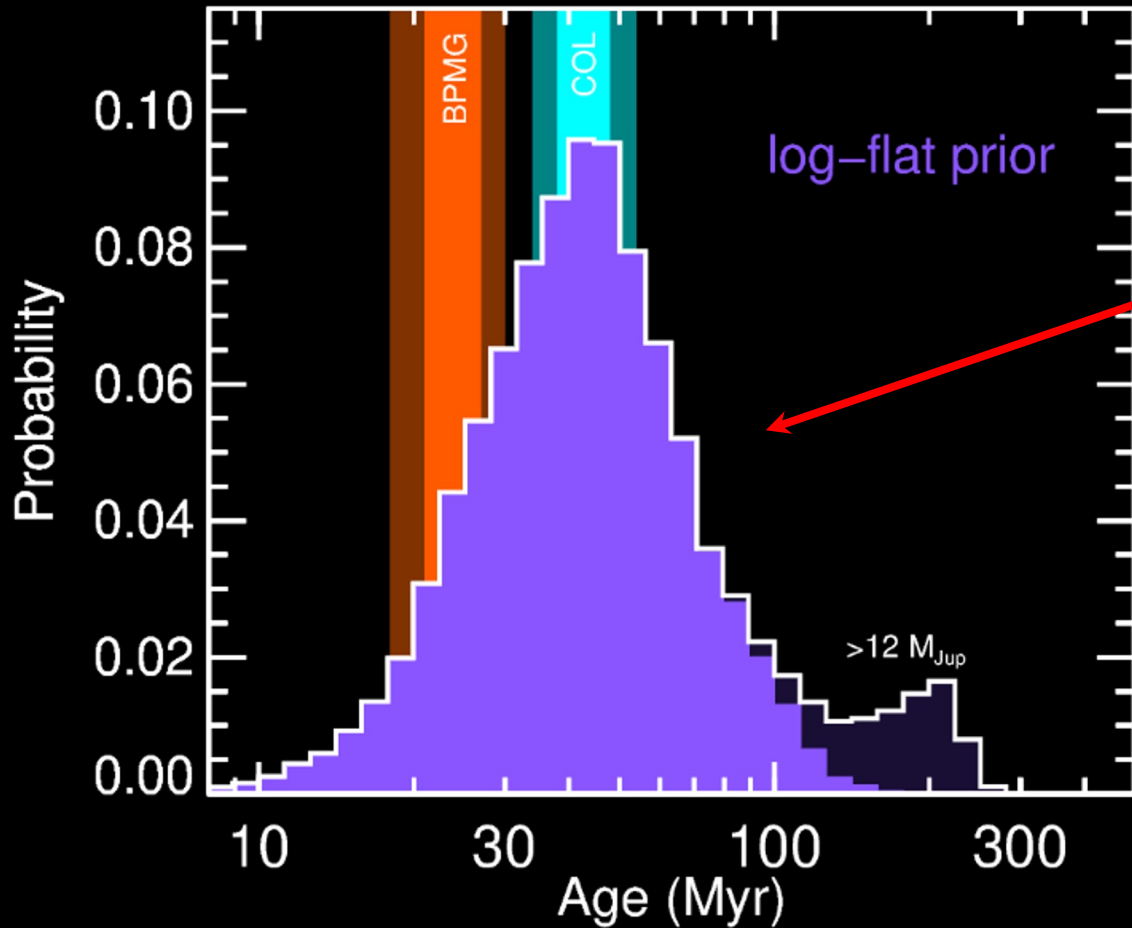
The First Dynamical Mass Measurement in the HR 8799 System

G. Mirek Brandt<sup>7,1</sup> , Timothy D. Brandt<sup>1</sup> , Trent J. Dupuy<sup>2</sup> ,  
Daniel Michalik<sup>3</sup> , and Gabriel-Dominique Marleau<sup>4,5,6</sup> 

## HR 8799 e



NRC-HIA, C. Marois, and Keck  
Observatory



The planet's age  
from its mass!






M. Brandt et al. 2021, arxiv:  
2105.12820

The HR 8799 work was a result of coupling HTOF with REBOUND.



UCSB

htof: A New Open-source Tool for  
Analyzing Hipparcos, Gaia, and Future  
Astrometric Missions

G. Mirek Brandt<sup>5,1</sup> , Daniel Michalik<sup>6,2</sup> , Timothy D. Brandt<sup>1</sup> ,  
Yiting Li<sup>1</sup> , Trent J. Dupuy<sup>3</sup> , and Yunlin Zeng<sup>1,4</sup>



# HTOF: all things absolute astrometry

[github.com/gmbrandt/HTOF](https://github.com/gmbrandt/HTOF)

- Automatic downloading of Hip1 and Hip2, Gaia raw data for on-sky positions (a.k.a the intermediate astrometry; IAD).
- Easy parsing of the IAD files/scanning law
- Fit 5,7,9 parameter skypaths, compute hip2 error inflations etc..









HTOF: M Brandt. et al. 2021, arxiv: 2109.06761 (developed by myself, Daniel Michalik, Tim Brandt & Gavin K. Hung)  
REBOUND: Rein & Liu 2012, [github.com/hannorein/rebound](https://github.com/hannorein/rebound)

# Open-source software framework for masses+orbits

Orvara combines absolute astrometry with relative astrometry (also RVs and relative RVs).

orvara: An Efficient Code to Fit  
Orbits Using Radial Velocity,  
Absolute, and/or Relative  
Astrometry









[github.com/t-brandt/orvara](https://github.com/t-brandt/orvara)

Timothy D. Brandt<sup>1</sup> , Trent J. Dupuy<sup>2</sup> , Yiting Li<sup>1</sup> ,  
G. Mirek Brandt<sup>7,1</sup> , Yunlin Zeng<sup>3</sup> ,  
Daniel Michalik<sup>4</sup> , Daniella C. Bardalez Gagliuffi<sup>5</sup> , and  
Virginia Raposo-Pulido<sup>6</sup> 

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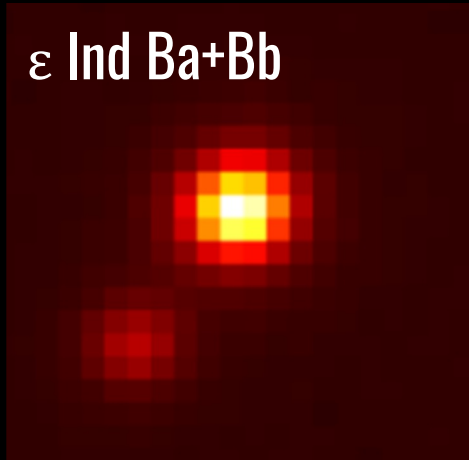
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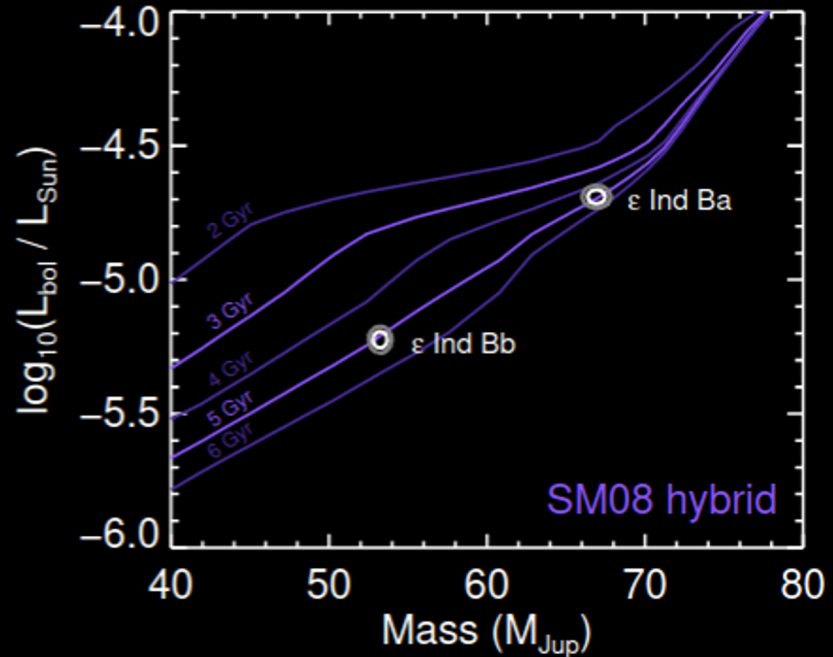
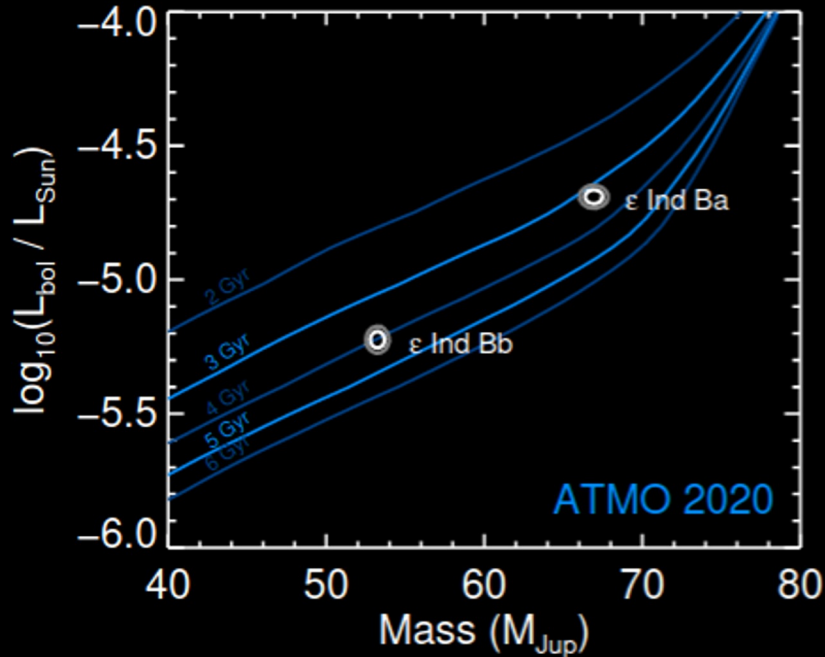
HTOF inside!



A fantastic example of  
constraining detailed attributes of Brown  
Dwarfs, not just the age



# Empirically testing BD Model Isochrones



Using orvara ! Minghan Chen + Yiting Li et al. 2022, arxiv: 2205.08077

**The common denominator of both examples:  
Relative astrometry + absolute astrometry to  
arrive at the mass. No radial velocities were  
used in either case!**

# Masses give us so much!

But we have *so few* of them...

All known exoplanets

About 5000

Brown Dwarfs

(defined here as  
mass > 13 M<sub>jup</sub>)

About 100

Imaged Brown Dwarfs  
with known mass\*

About 20

\*meaning the mass is independently measured,  
not inferred from a cooling model.

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We need to build up this sample size!

Imaged Brown Dwarfs  
with known mass\*

About 20

\*meaning the mass is independently measured,  
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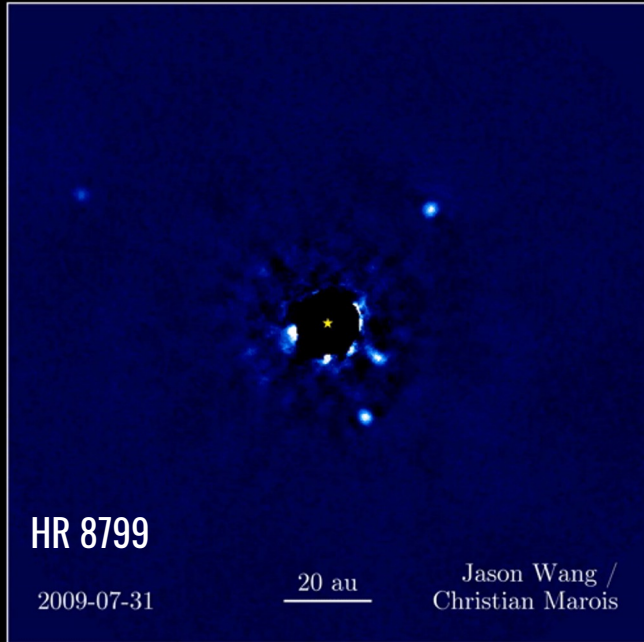
# How to measure more masses

Combine relative astrometry + absolute astrometry (and RVs too).

For absolute astrometry: The standard is to use proper motion anomalies.

But with Gaia DR4 we will have the individual position measurements on-sky. (often called the epoch astrometry; or IAD for Hipparcos)

## Relative motion



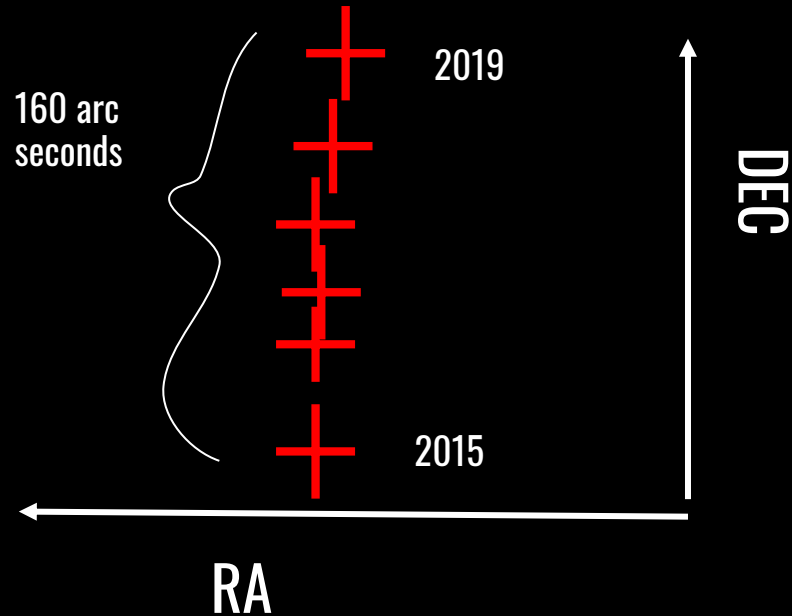
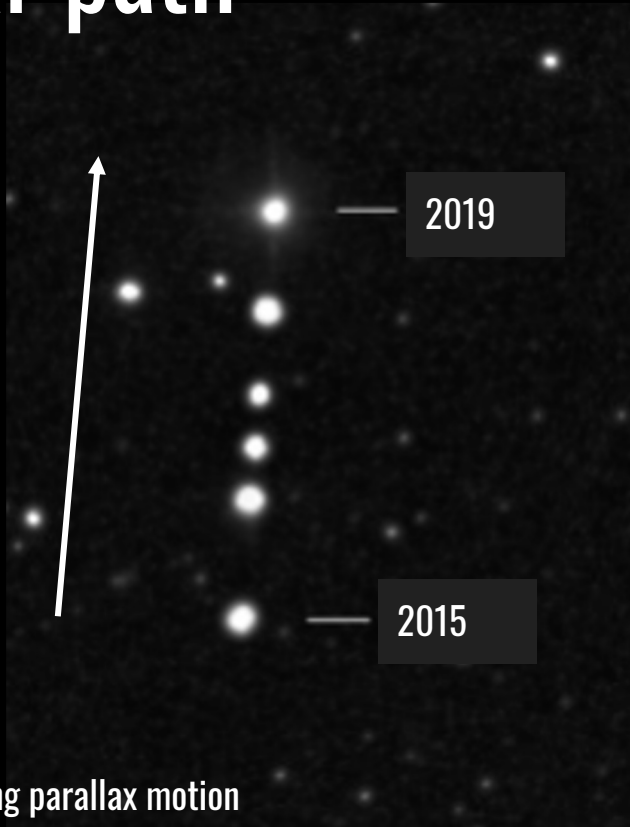
+

## Absolute motion from Epoch Astrometry



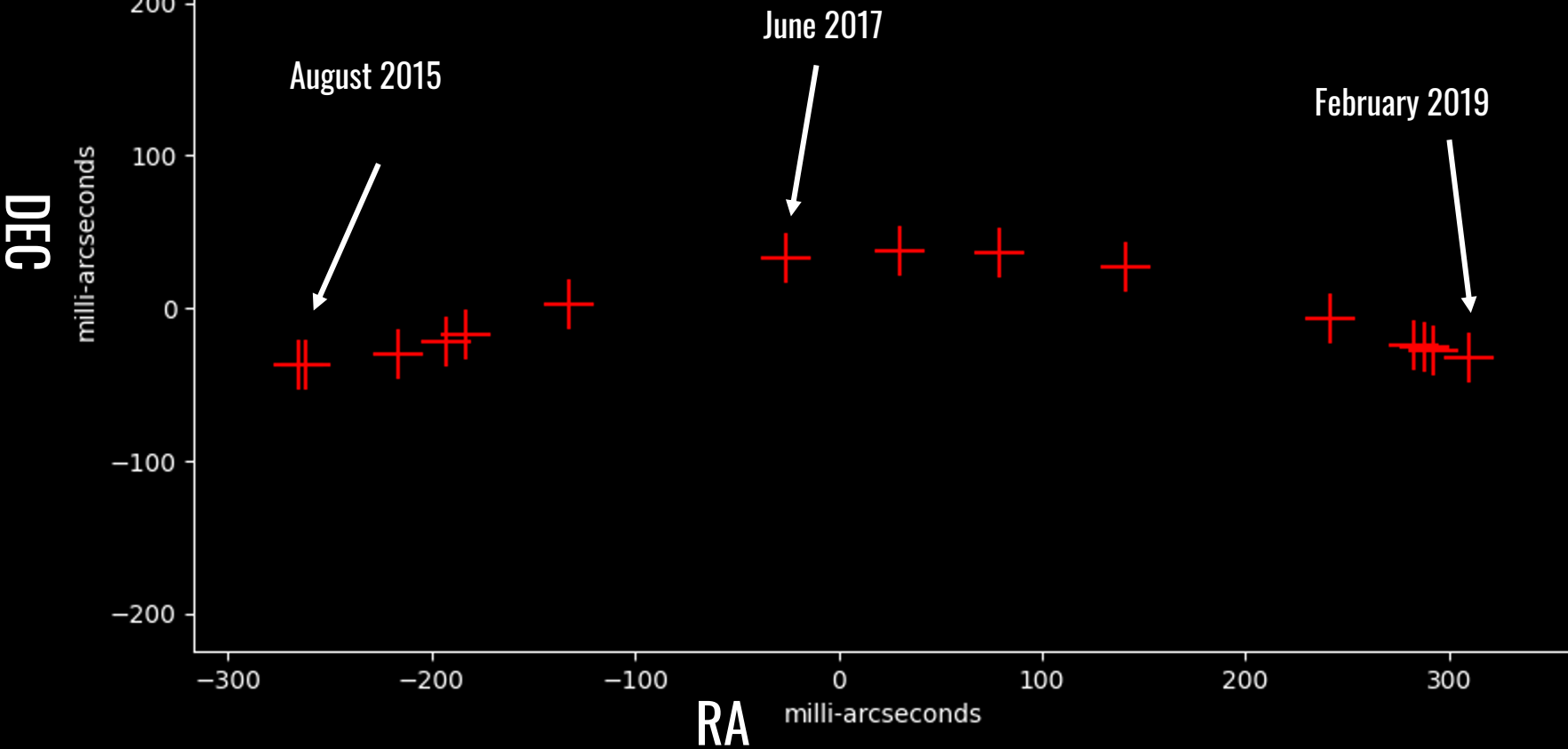
= the mass (and other orbital elements)

# Stars without heavy companions follow a linear path\*\*

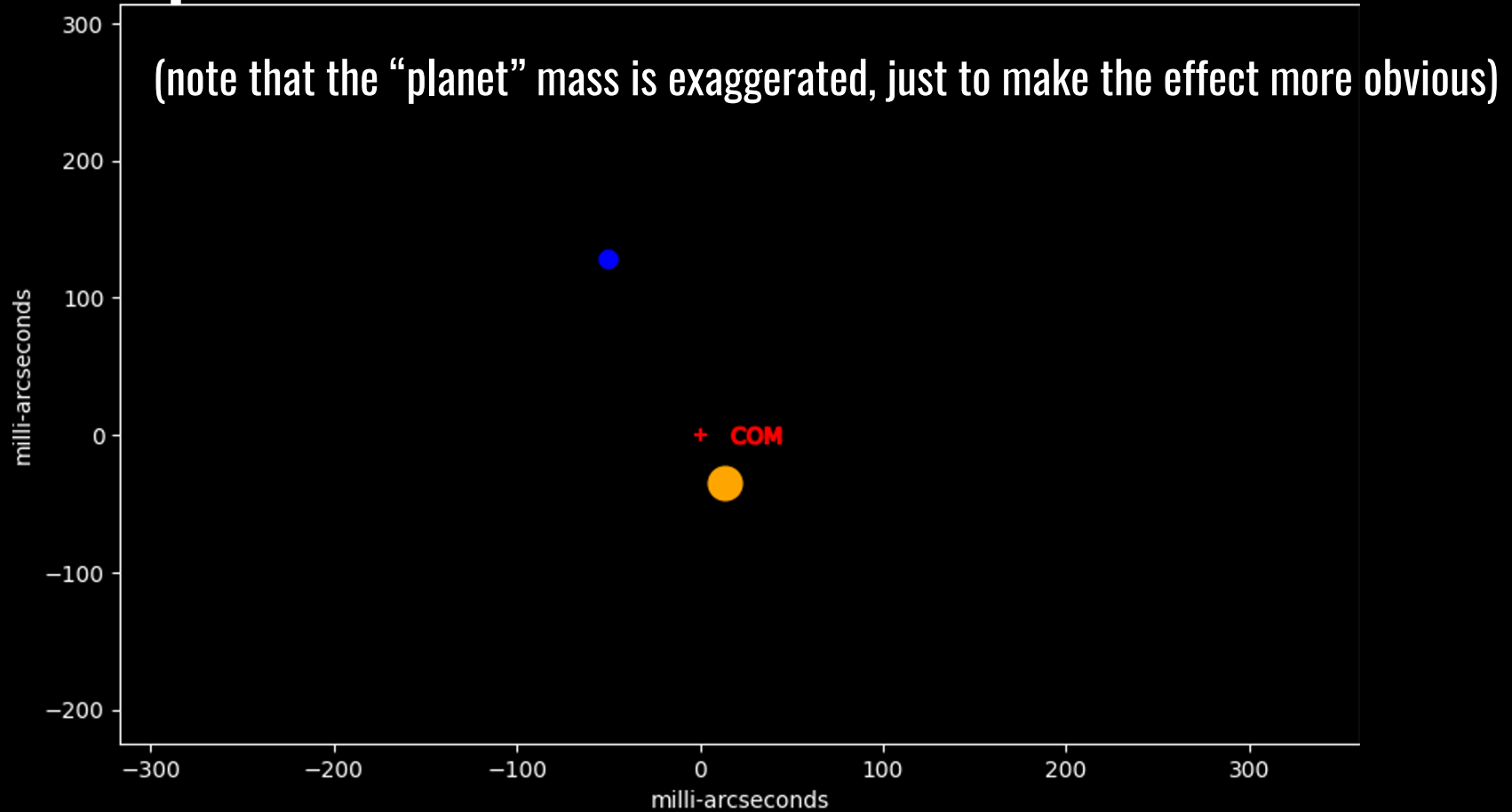


\*\* after removing parallax motion

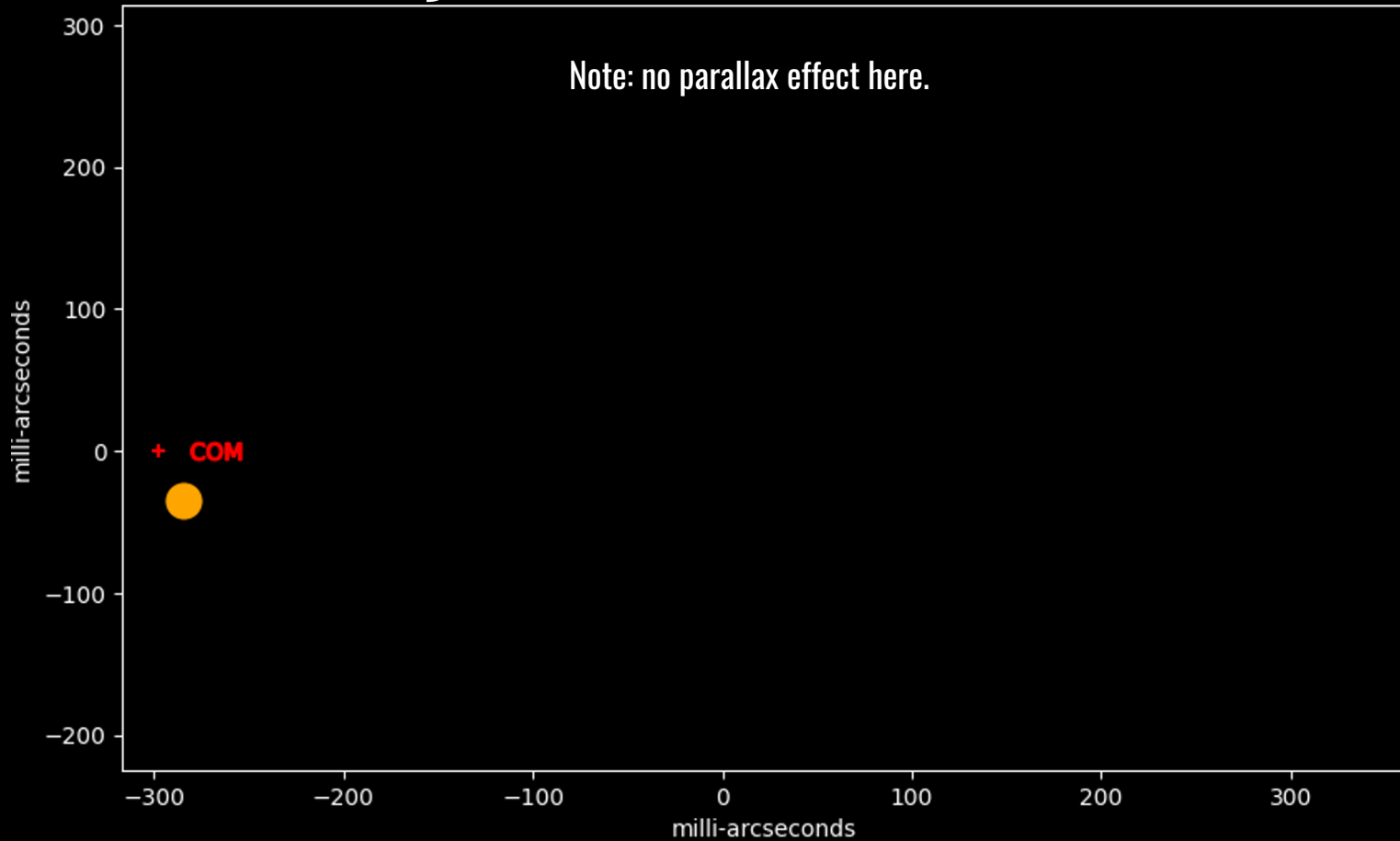
Let's imagine a fictitious heavy companion around Barnard's star.



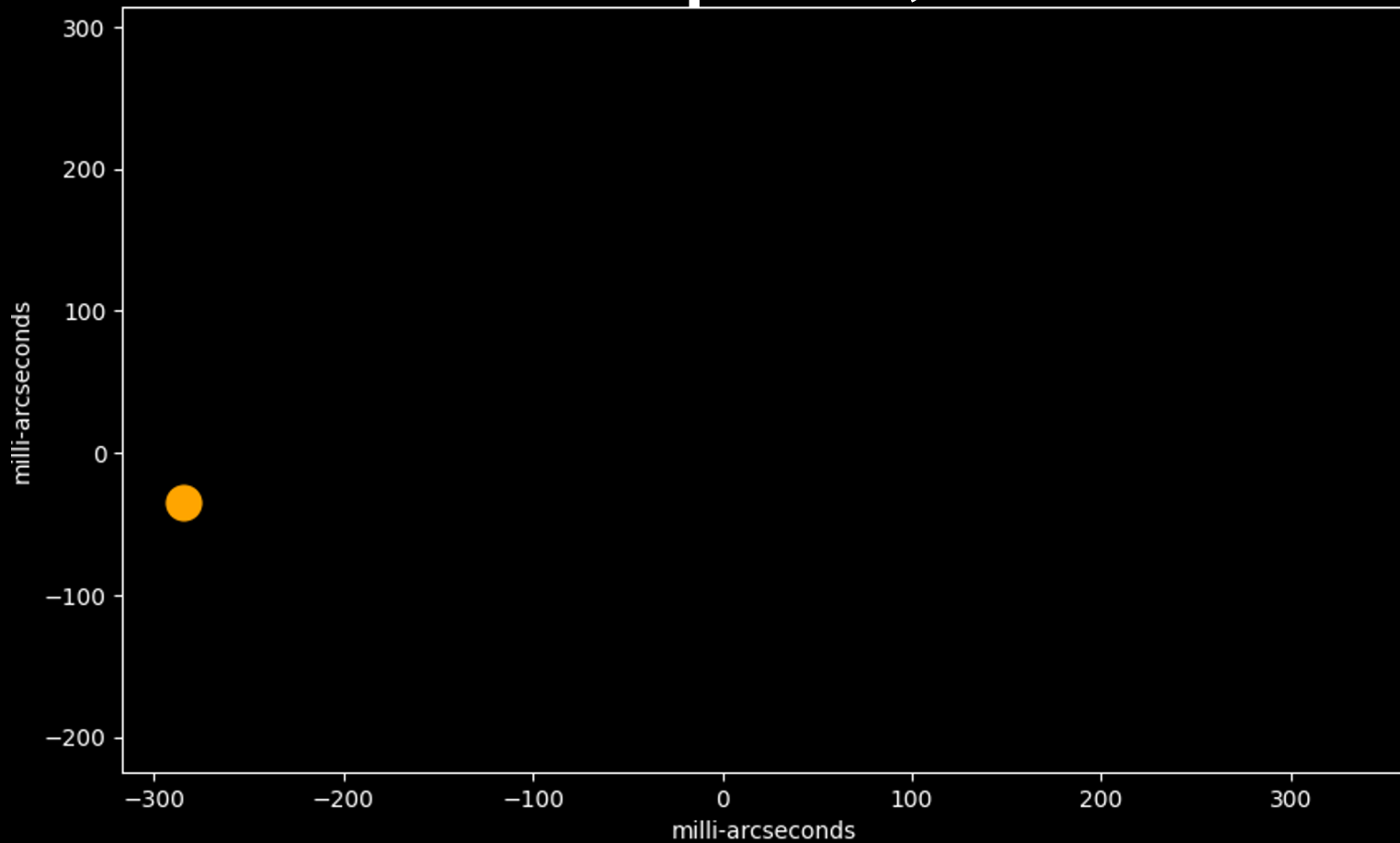
# A star + planet in their own frame of reference



# From our Earthly frame of reference.



# But we cannot see the planet, so:



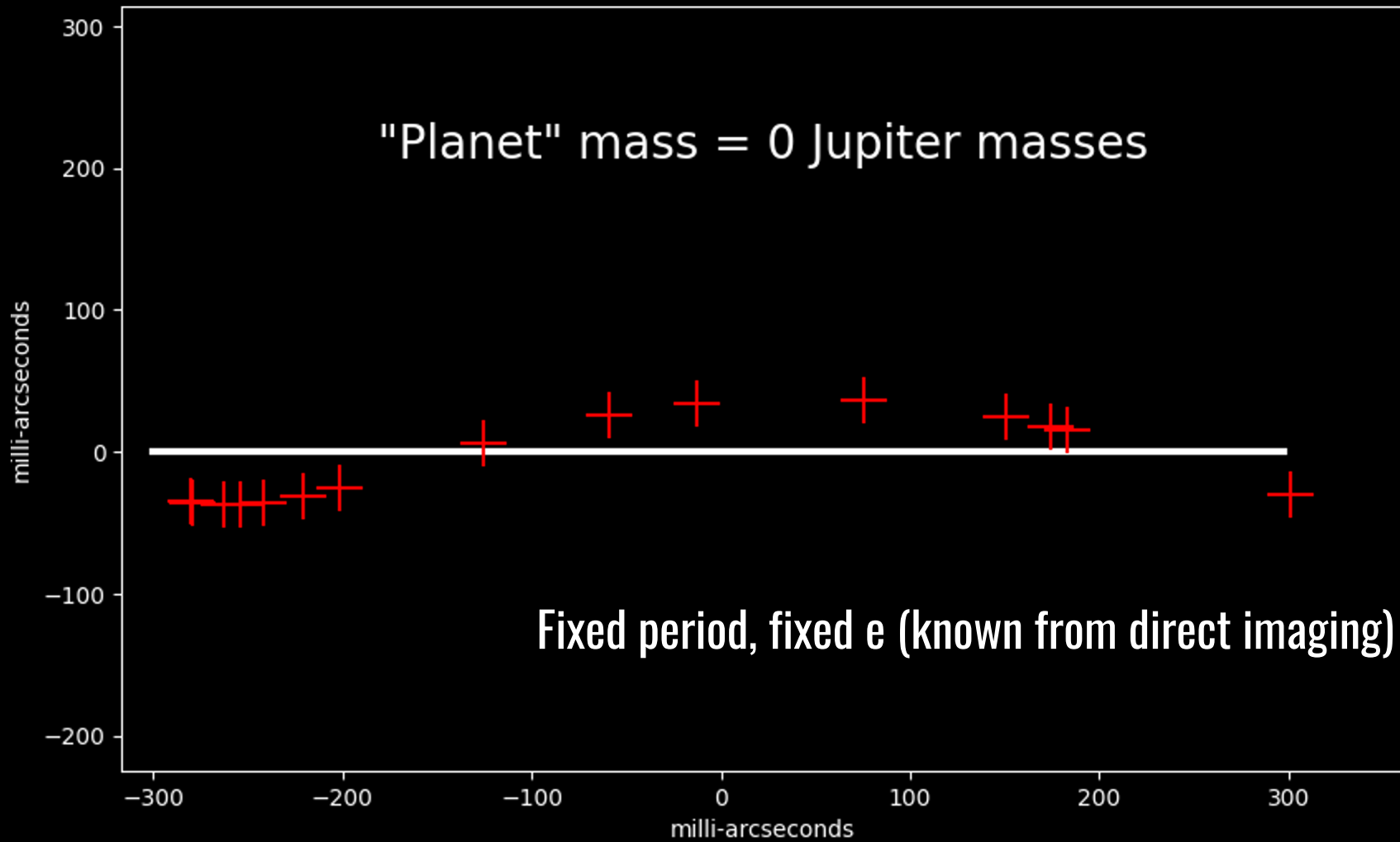
# How do we solve for the mass?

if we have direct imaging over a long enough baseline, we *already* have strong constraints on:

- the eccentricity  $e$
- the inclination  $i$
- the semi-major axis

We can combine those with absolute astrometry to get the mass.

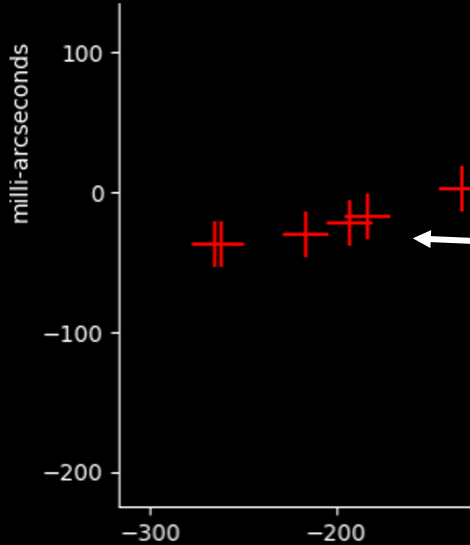




For a face-on circular orbit, the host star will exhibit sky-plane motion with an amplitude of

$$\text{astrometric semiamplitude} = \varpi \left( \frac{M_{\text{planet}}}{M_{\text{planet}} + M_{\text{star}}} \right) \left( \frac{a}{\text{A.U.}} \right)$$

# But using the on-sky positions can be tricky.



These 2d measurements were not exactly like real Gaia observations...

# Why one should interpret Hipparcos/Gaia on-sky positions carefully

For some systems, we know the companion orbits so well\* that we can predict what Gaia DR3 would have reported for accelerations.

\* from orvara fits to RV + proper motion anomalies + direct imaging (e.g, Y.Li + '21, Brandt+21, Qier An et al. '22)

# Two examples from Qier An et al. (2022, in prep)

Gaia DR3 accel_ra	accel_ra prediction (i.e., ground truth)	Gaussian sigma discrepancy
$17.8 \pm 0.3 \text{ mas/yr}^2$	$12.7 \pm 0.2 \text{ mas/yr}^2$	$14\sigma$
$-1.0 \pm 0.1 \text{ mas/yr}^2$	$-1.6 \pm 0.1 \text{ mas/yr}^2$	$4\sigma$

# Complications with real Gaia/Hipparcos

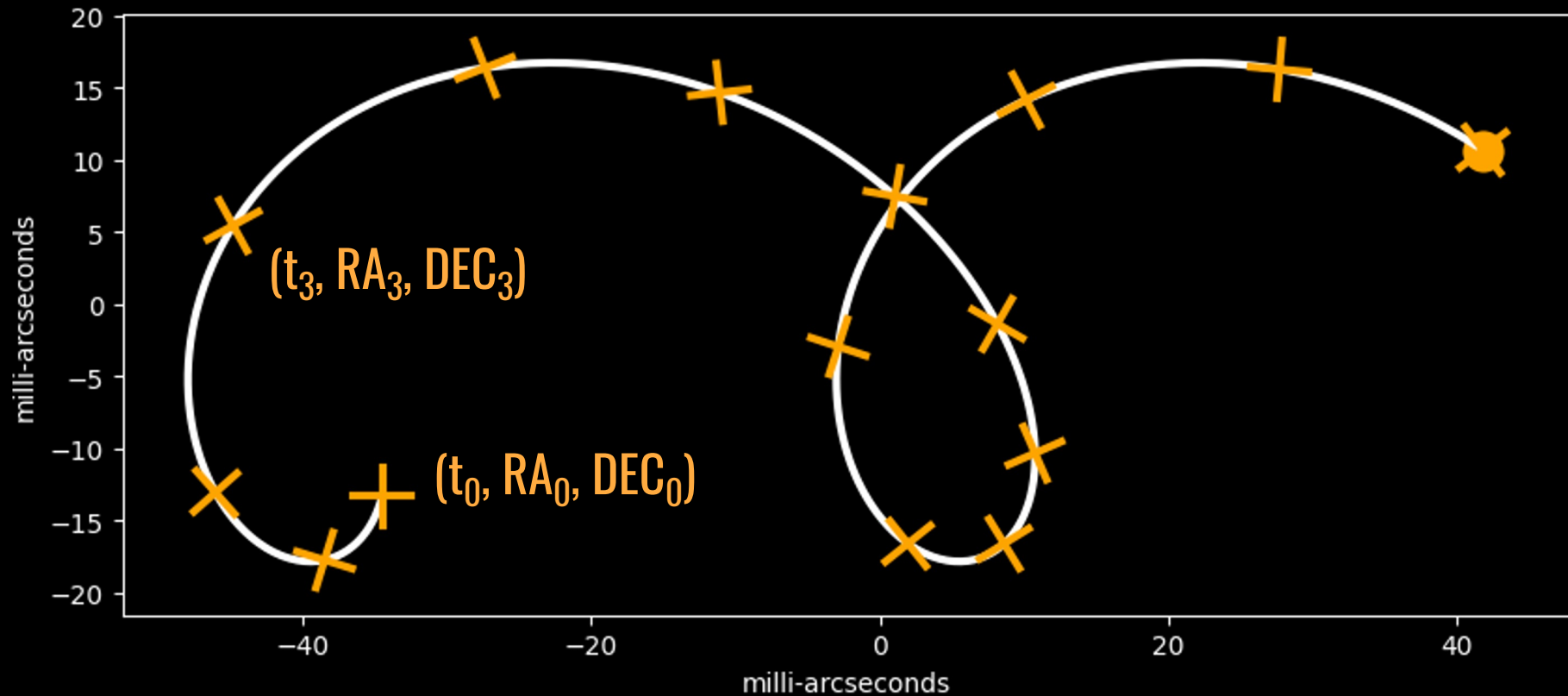
- 1-dimensional measurements.
- Potential systematics in the raw positions

# Simple example

skypath with proper motion + orbital motion from an unseen companion.

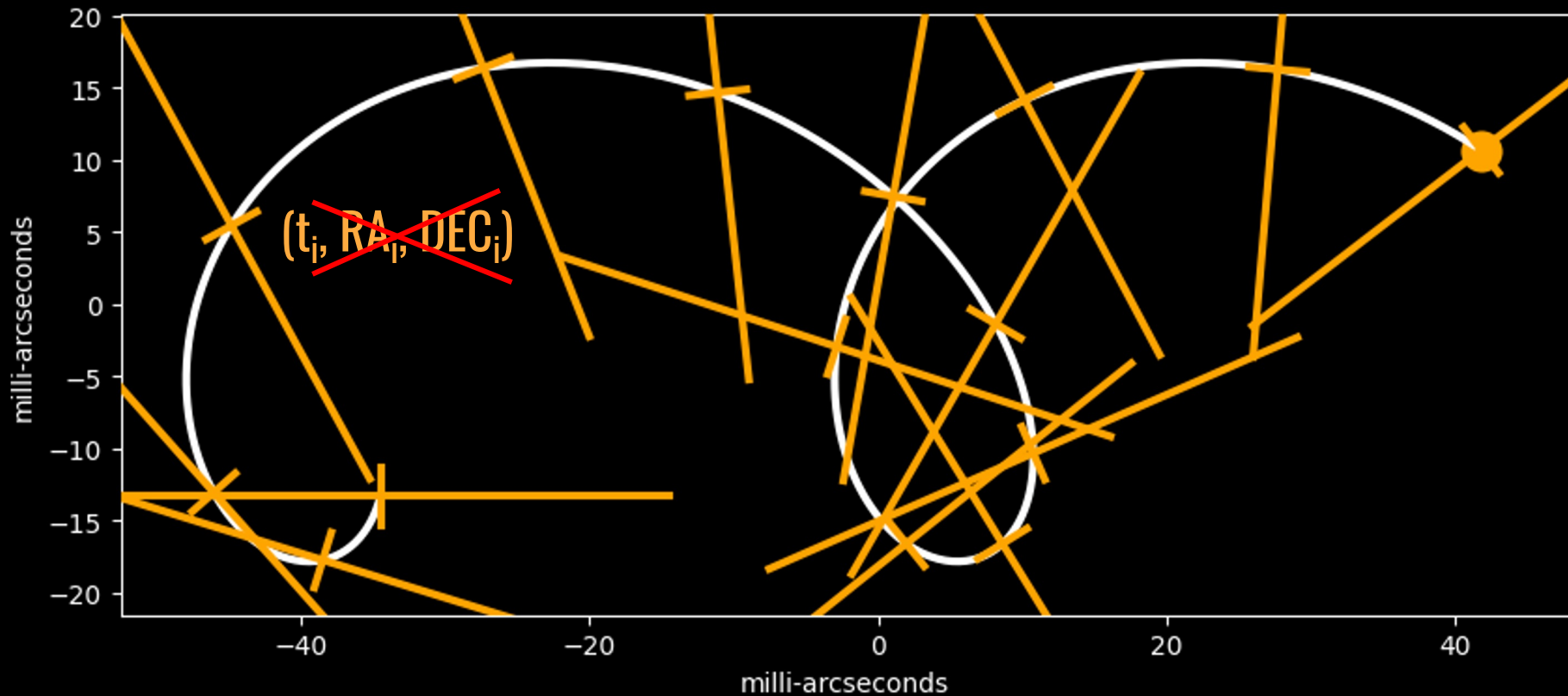
No parallax motion.

# 2d measurements

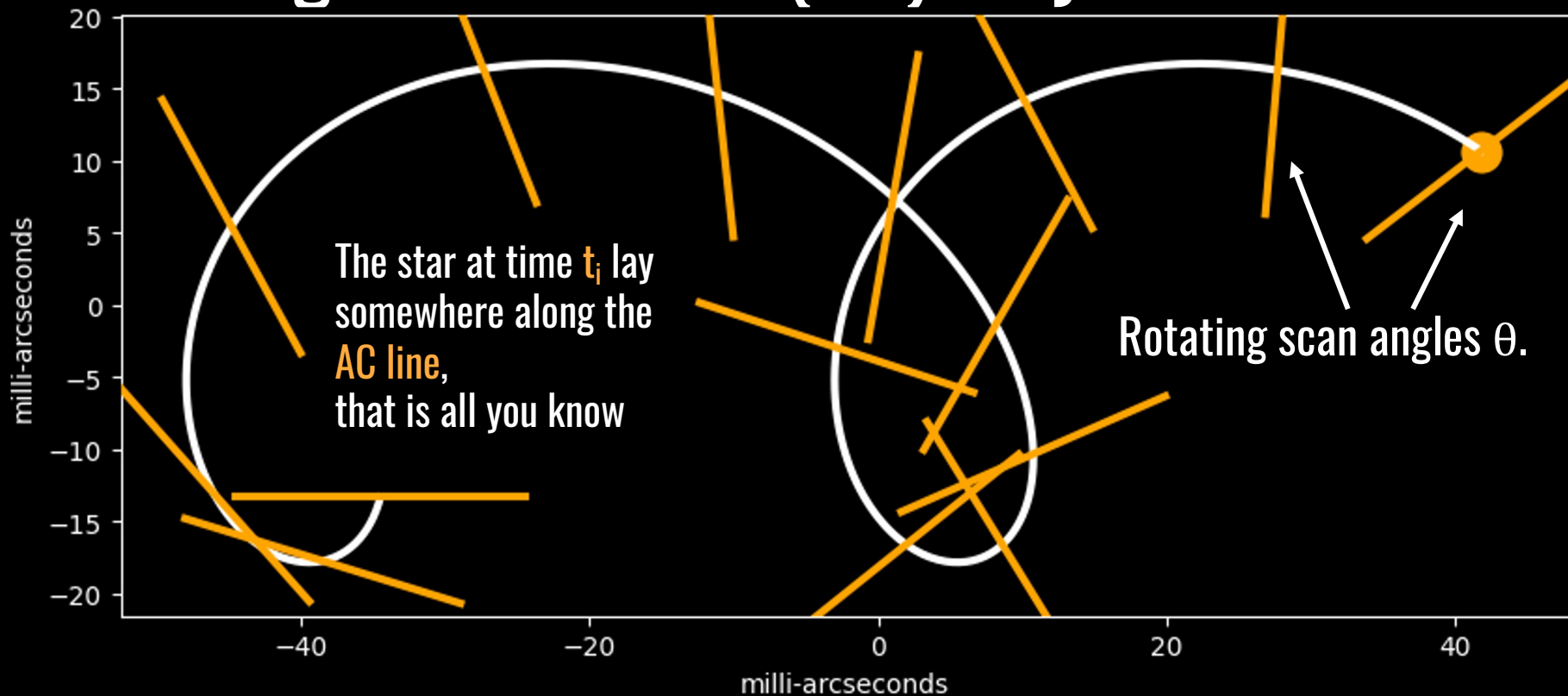




Gaia/Hipparcos: One axis has *much larger* uncertainty → “1d measurement”



# Showing Across-Scan (AC) only

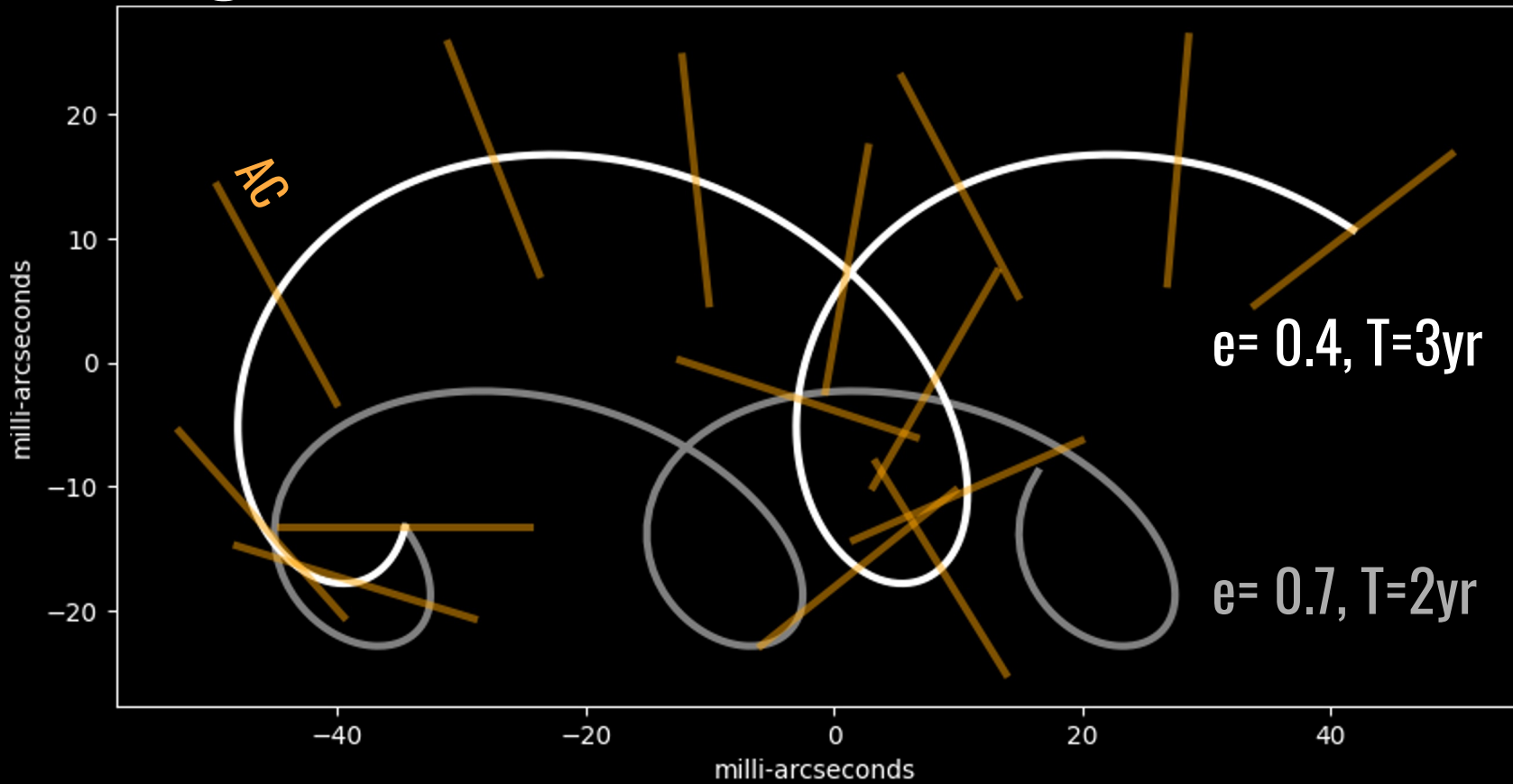


# Fitting orbits to epoch astrometry

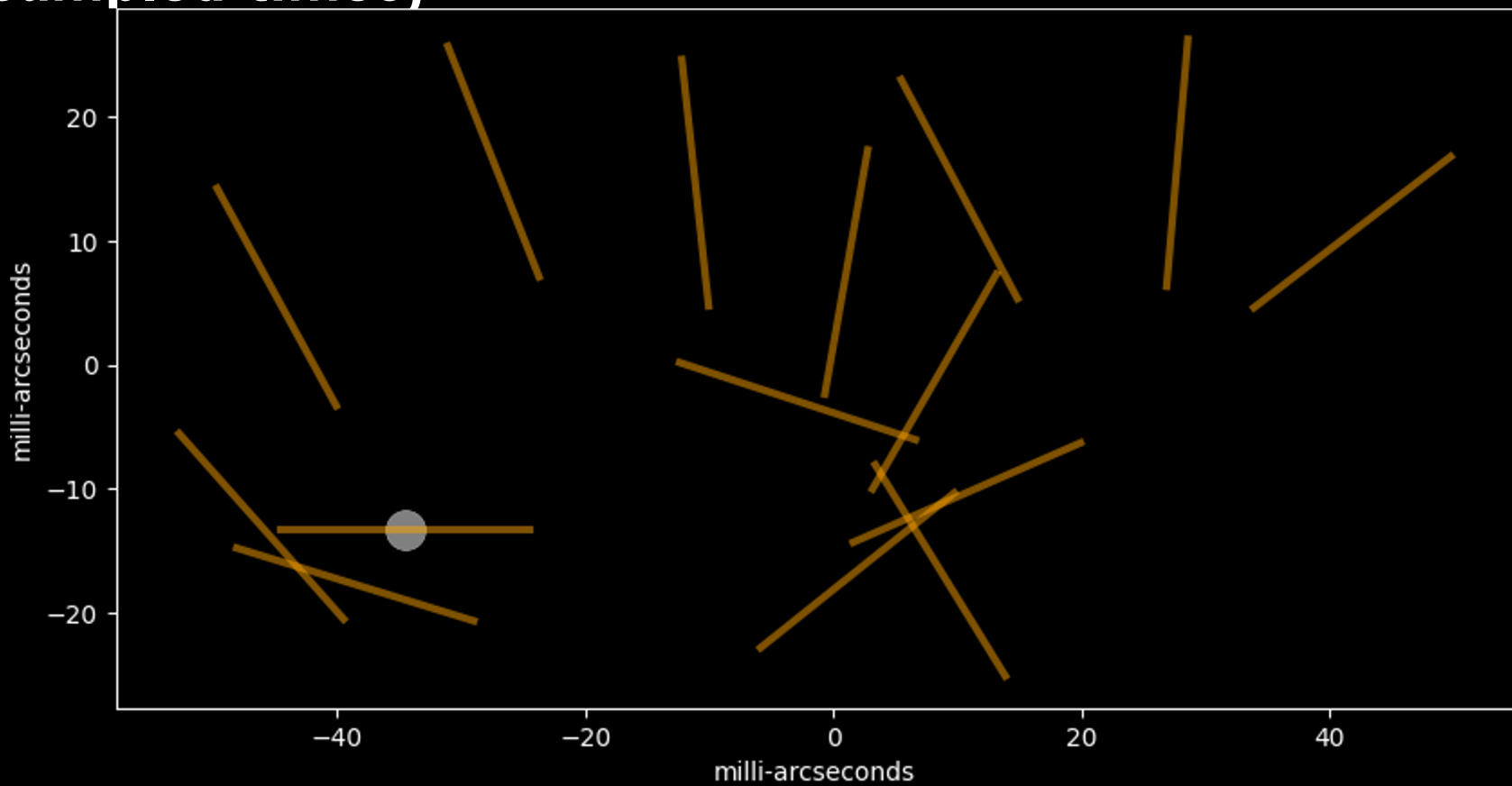
You can have multiple solutions that fit the data nearly equally as well but have very different orbital parameters.

To help illustrate that, next is an over-exaggerated example.

# Is the gray orbit an OK fit to the data too?



# Both orbits give the same projected positions! (at the sampled times)



So two **very different** orbits can fit a single absolute astrometric path.  
The last example was contrived but..

# In the hands-on session today

You'll generate real examples of families of modestly different orbits that all fit simulated Gaia epoch astrometry.

Confidence intervals on e&T in these cases are difficult to define.

# The complications

- 1-dimensional measurements.
- Potential systematics in the raw positions

Look out for G.M. Brandt et al. 2022 – discussion of systematics in Hipparcos epoch astrometry in great detail.



# The big takeaways

- direct imaging + absolute astrometry (+ RVs) is powerful & now is a golden age of open-source software (e.g., htof, orvara, orbitize\*)
- Orbit fitting to absolute astrometry 1d scans can be tricky.

\*S Blunt et al. 2019, arxiv: 1910.01756 , [github.com/sblunt/orbitize](https://github.com/sblunt/orbitize)

# Thank you!

Questions?



“An oil painting of the telescopes atop Maunakea”, created by the DALL·E neural net