

# Astrometry & Exoplanet Host Star Properties



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*Stellar Properties: what  
are they and what can  
we measure?*

**What are some examples of fundamental stellar properties?**





# Fundamental

Effective Temperature ( $T_{\text{eff}}$ )

Radius (R)

Mass (M)

Chemical Composition

Surface Gravity (g)

Luminosity (L)

Density ( $\rho$ )

Age

# Observed

Color

Spectral Type

Luminosity Class

Rotation Period

Activity Level / Cycle

Multiplicity



# Fundamental Properties of Stars

Effective Temperature ( $T_{\text{eff}}$ )

Radius ( $R$ )

Mass ( $M$ )

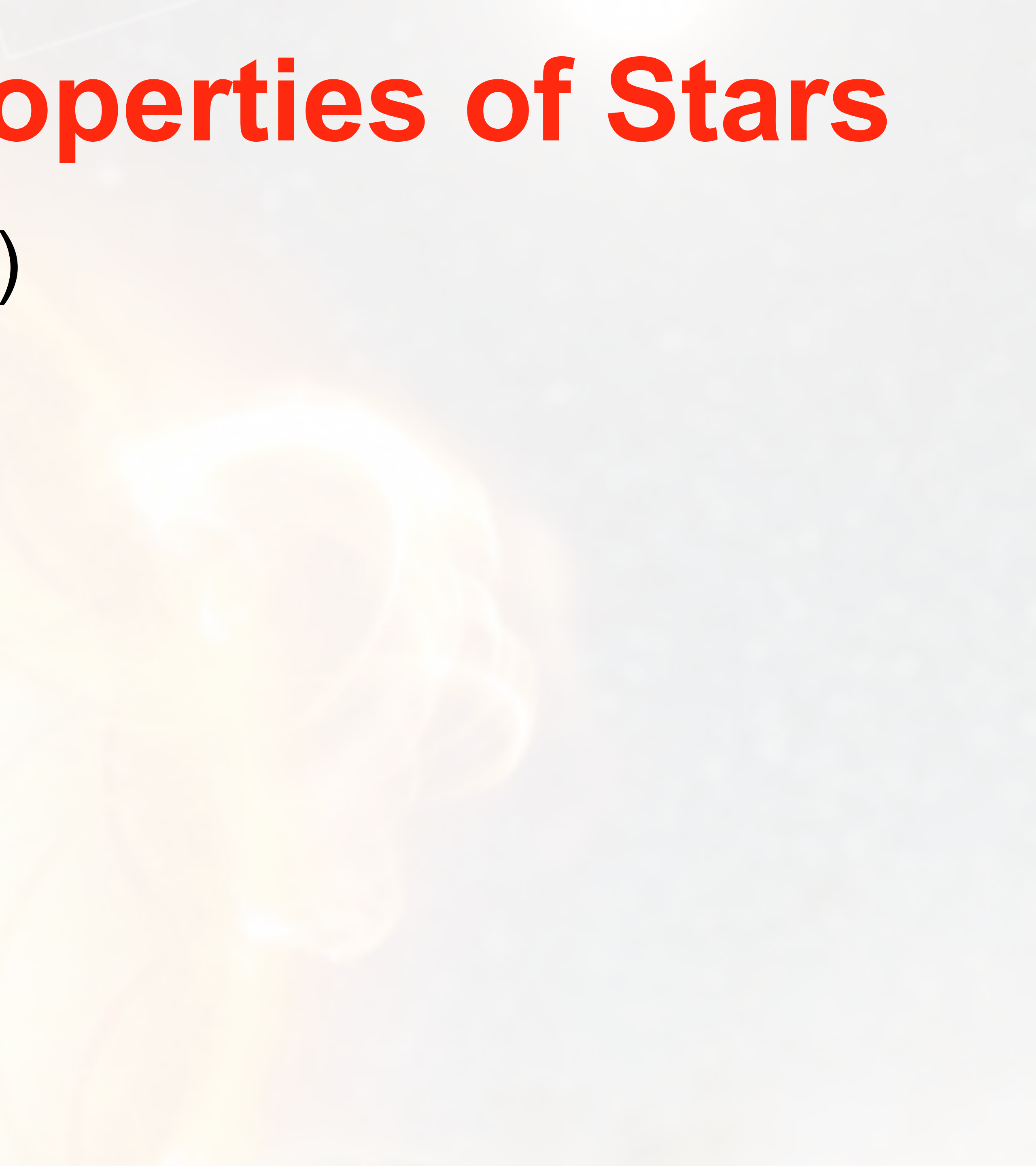
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*Most fundamental properties are not independent*

$$\rho \propto M/R^3$$

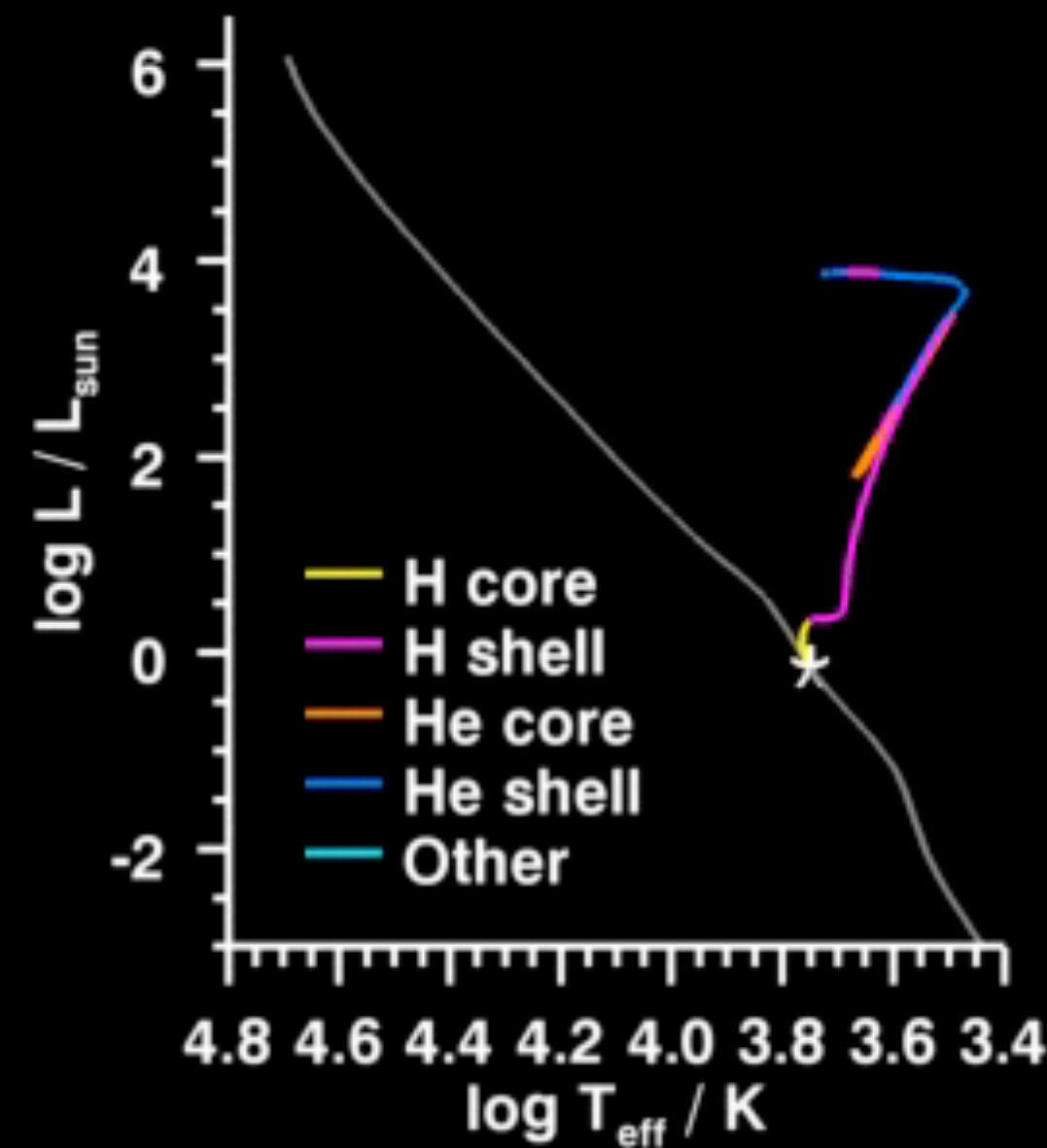
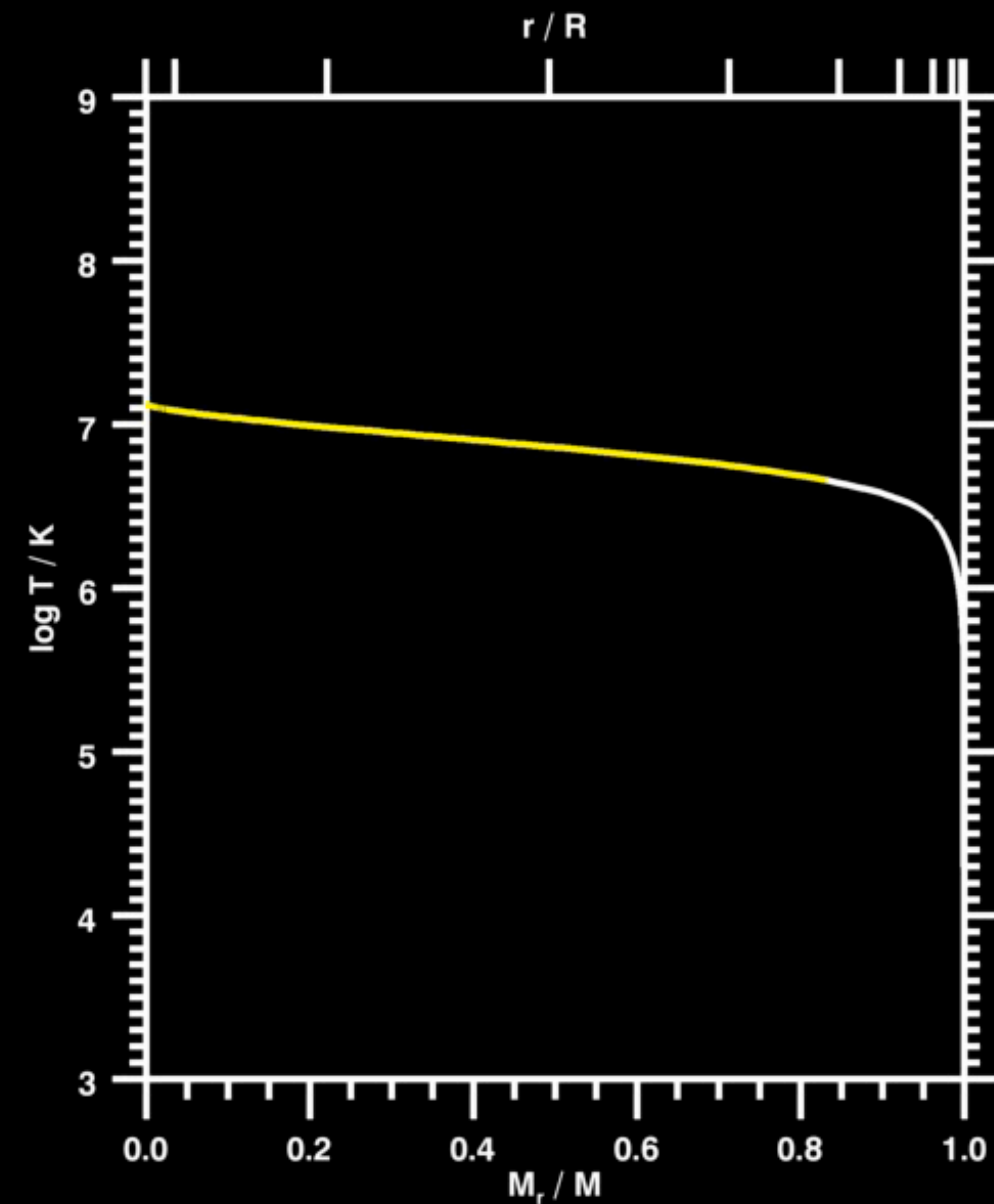
$$g \propto M/R^2$$

$$L \propto R^2 T_{\text{eff}}^4$$

*Assumes: atmospheres are thin  
& stars ~ blackbodies*

# Mass, composition & age uniquely define other fundamental stellar properties

(Vogt-Russell "Theorem")



$M / M_{\text{sun}}: 1.000$   
 $L / L_{\text{sun}}: 6.98\text{E-}01$   
 $R / R_{\text{sun}}: 8.86\text{E-}01$   
 $T_{\text{eff}} / K: 5609$   
 $\text{Age} / \text{yrs}: 0.00\text{E+}00$

Rich Townsend

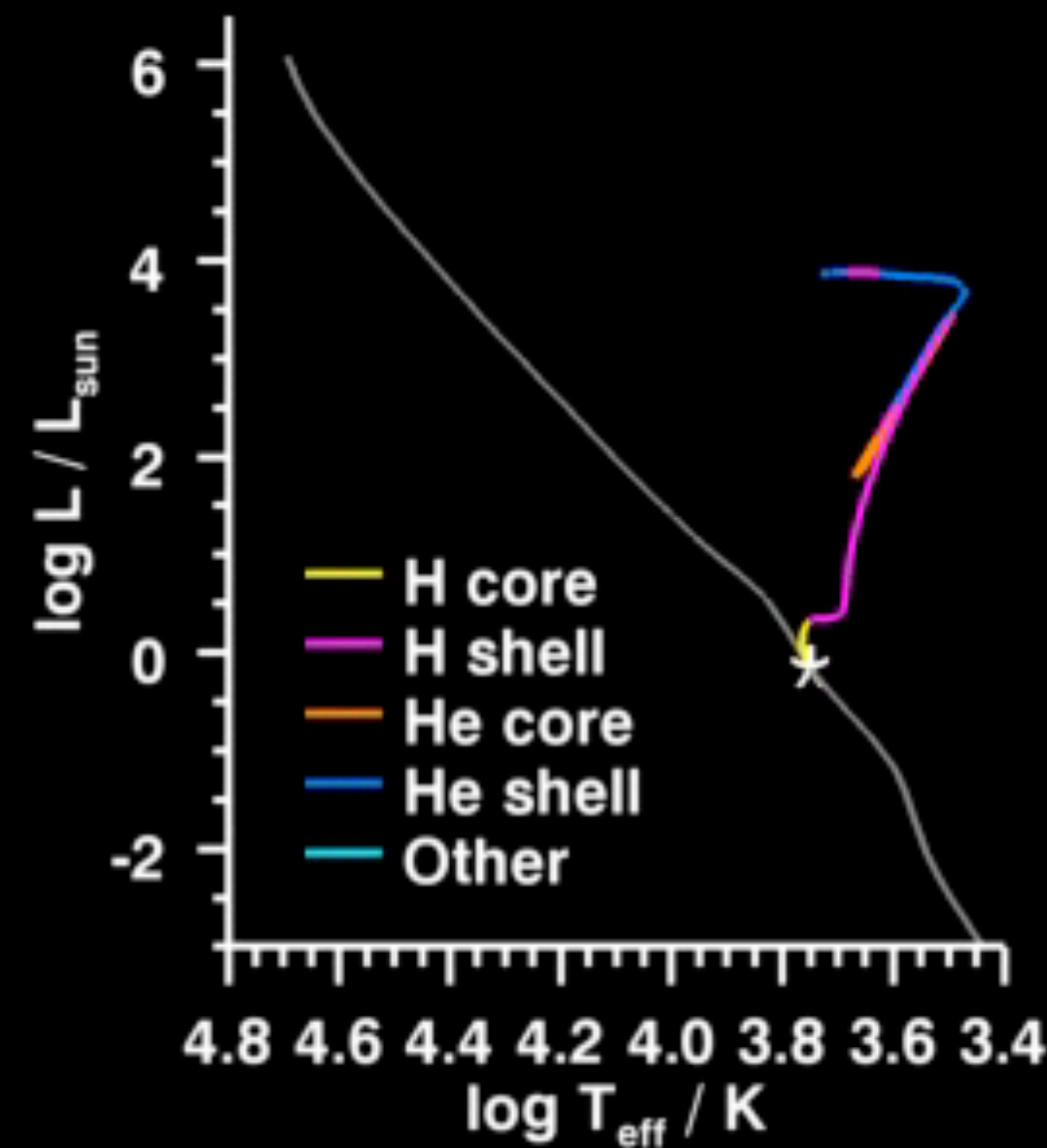
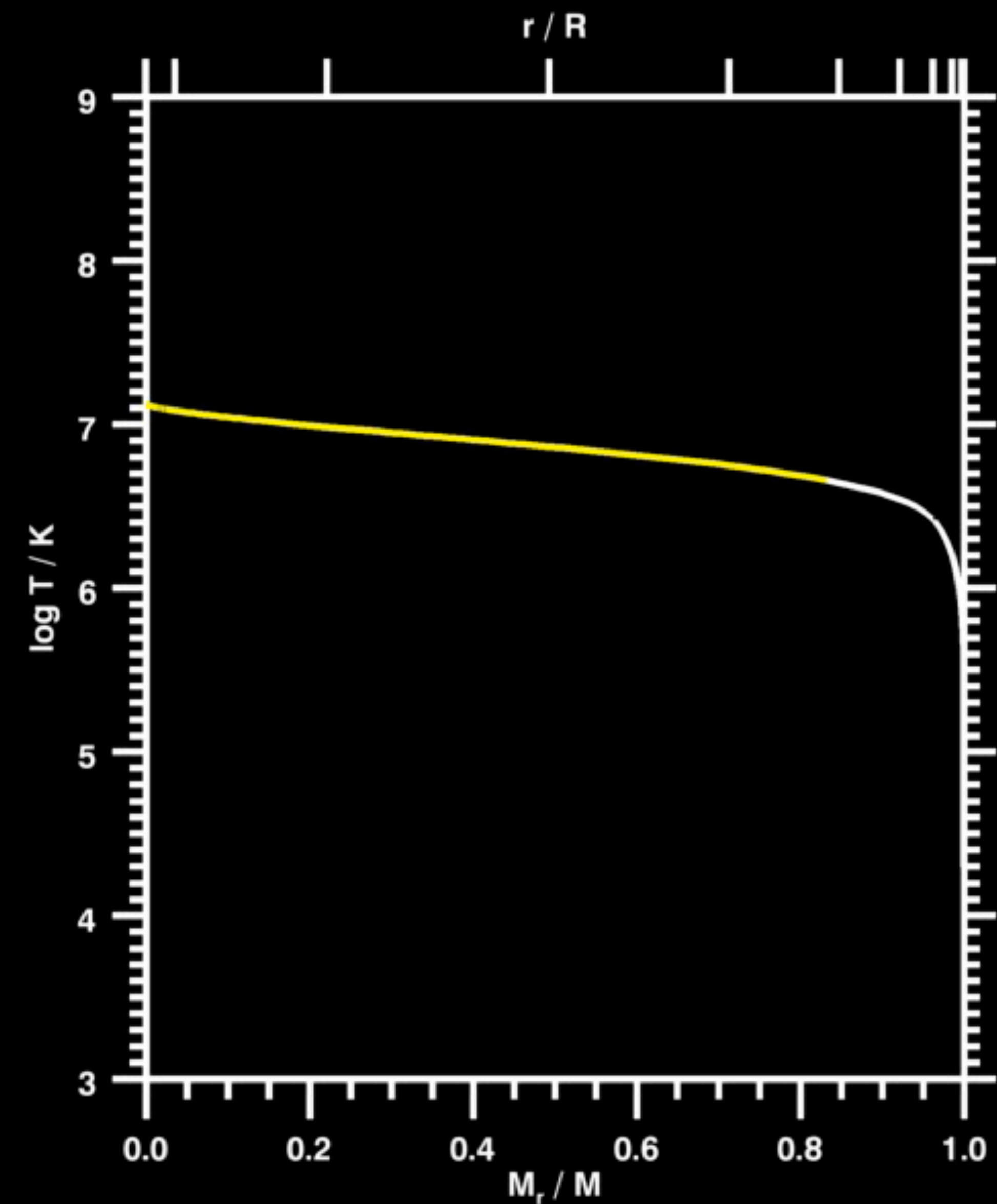
(<http://www.astro.wisc.edu/~townsend>)



# Mass, composition & age uniquely define other fundamental stellar properties

(Vogt-Russell "Theorem")

Unfortunately, mass & age (+ some elements such as He) are hard to measure!



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 $L / L_{\text{sun}}: 6.98\text{E-}01$   
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“Easy”

Possible

Hard

*Astrometry is critical for  
inferring ~ all  
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# Stellar Luminosity: Distance Modulus

$$m_b - M_b = 5 \log_{10}(d) - 5 + A_b$$

↑  
observed  
(apparent)  
magnitude in  
band b

↖  
d=10pc  
(absolute)  
magnitude in  
band b

↑  
distance in  
pc

↑  
interstellar  
extinction  
in band b

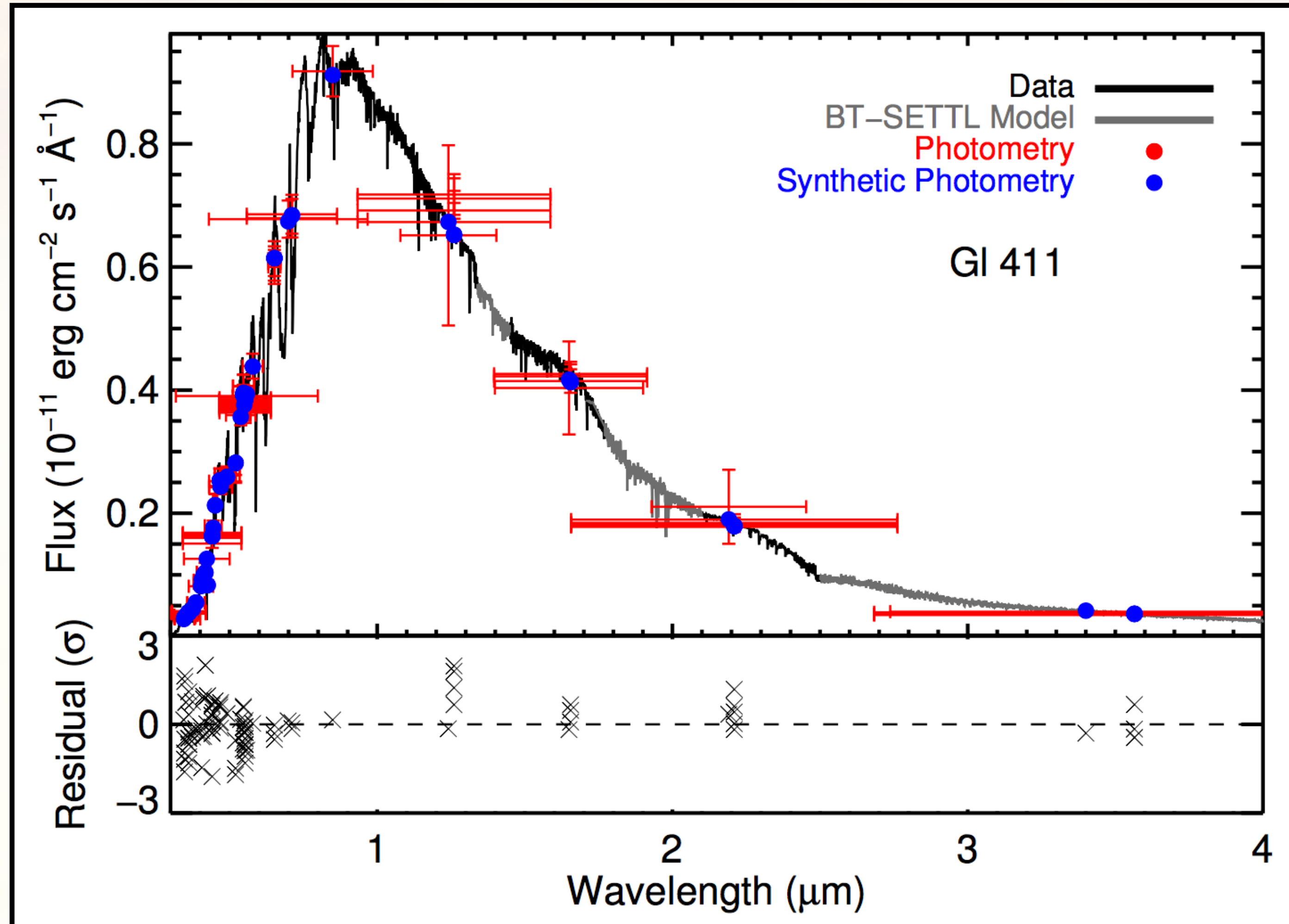
$$M_{\text{bol}} = M_b + BC_b \quad \text{BC} = \text{bolometric correction (from model atmospheres)}$$

$$M_{\text{bol}} - M_{\text{bol},\odot} = -2.5 \log_{10}(L/L_{\odot})$$

Advantage: Observables ( $m_b$  &  $d$ ) are available for lots of stars

Disadvantage: Need to be confident in your **BC** and **extinction** model!

# Bolometric Fluxes: SED Fitting



Mann+ 2016

$$L = 4\pi f_{\text{bol}} d^2$$

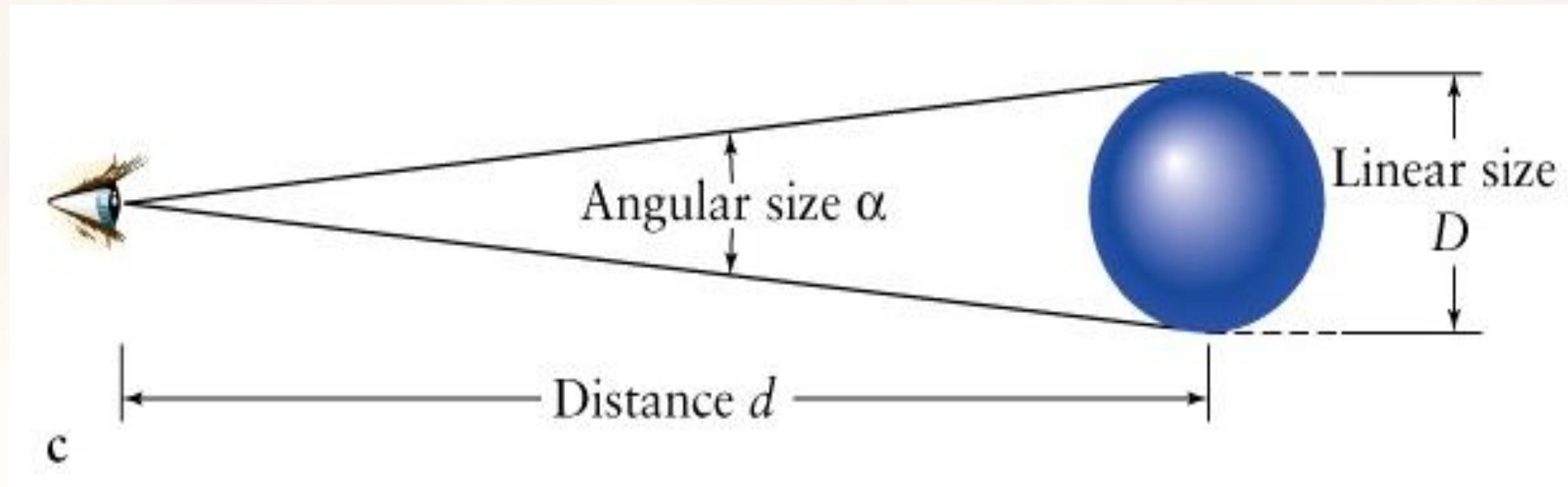
**Advantage:** Less model dependent than bolometric corrections

**Disadvantage:** Zeropoint offsets between photometric surveys

**Challenge (also true for BCs):** Depends on  $T_{\text{eff}}$  and extinction, which are highly degenerate

*Gaia Bp/Rp spectra are critical for this! See Orlagh's talk tomorrow*

# Stellar Radii from Parallaxes



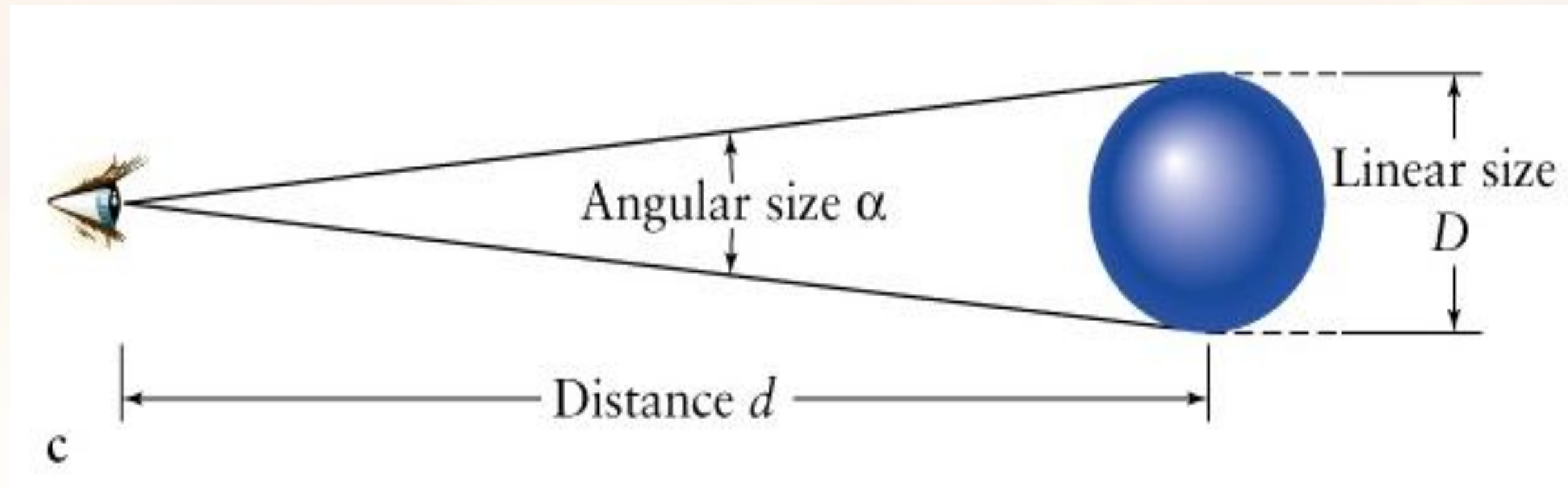
$$R = d \alpha / 2$$

Angular size + Distance gives a direct measurement of the star's Radius

Problem: stellar diameters are small and require interferometry to be resolved.  
*More on this by Roxanne tomorrow!*



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Angular size + Distance gives a direct measurement of the star's Radius

Problem: stellar diameters are small and require interferometry to be resolved.  
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Alternative: Stefan-Boltzmann Law

$$R_{\star} = \sqrt{\frac{F_{\text{bol}} d^2}{\sigma T_{\text{eff}}^4}}$$

But what is  $T_{\text{eff}}$  and how well do we know it?

# Effective Temperatures

$T_{\text{eff}}$  characterizes the total radiative flux transported through the atmosphere.

It can be regarded as an average of the temperature over depth in the atmosphere.

A blackbody radiating the same amount of total energy would have a temperature  $T = T_{\text{eff}}$ .

$$4\pi \int_0^{\infty} H_{\nu} d\nu = \sigma T_{\text{eff}}^4$$

$$F = \sigma T_{\text{eff}}^4 \longrightarrow \begin{array}{l} F = f_{\text{bol}} d^2/R^2 \\ R = d \alpha/2 \end{array} \longrightarrow T_{\text{eff}} = (4 f_{\text{bol}} / \sigma \alpha^2)^{1/4}$$

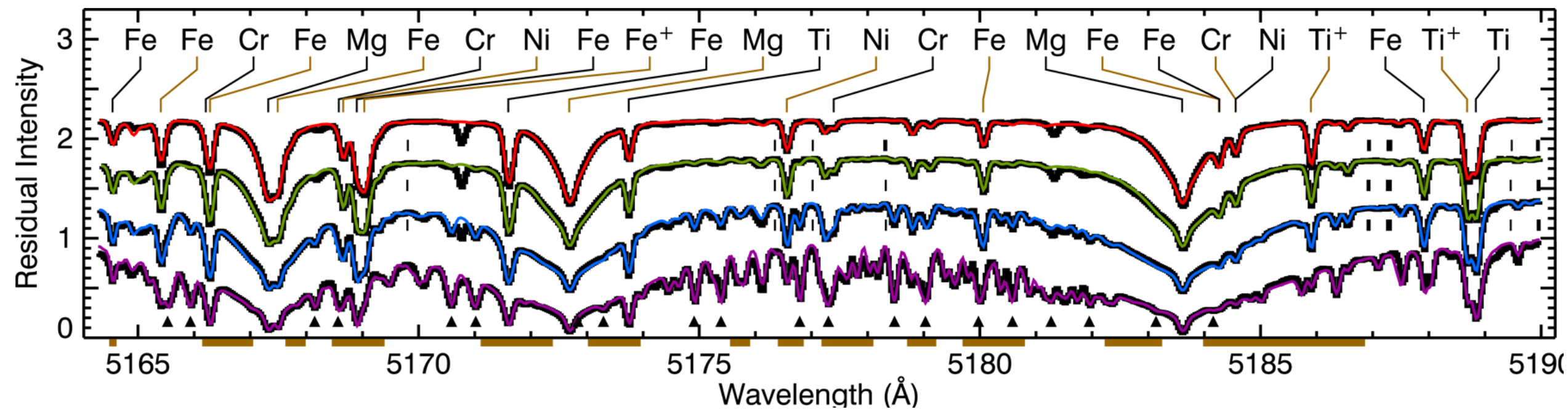
**Effective Temperature** is *defined* through **angular diameter** & **bolometric flux**



# Effective Temperatures

$$R_{\star} = \sqrt{\frac{F_{\text{bol}} d^2}{\sigma T_{\text{eff}}^4}}$$

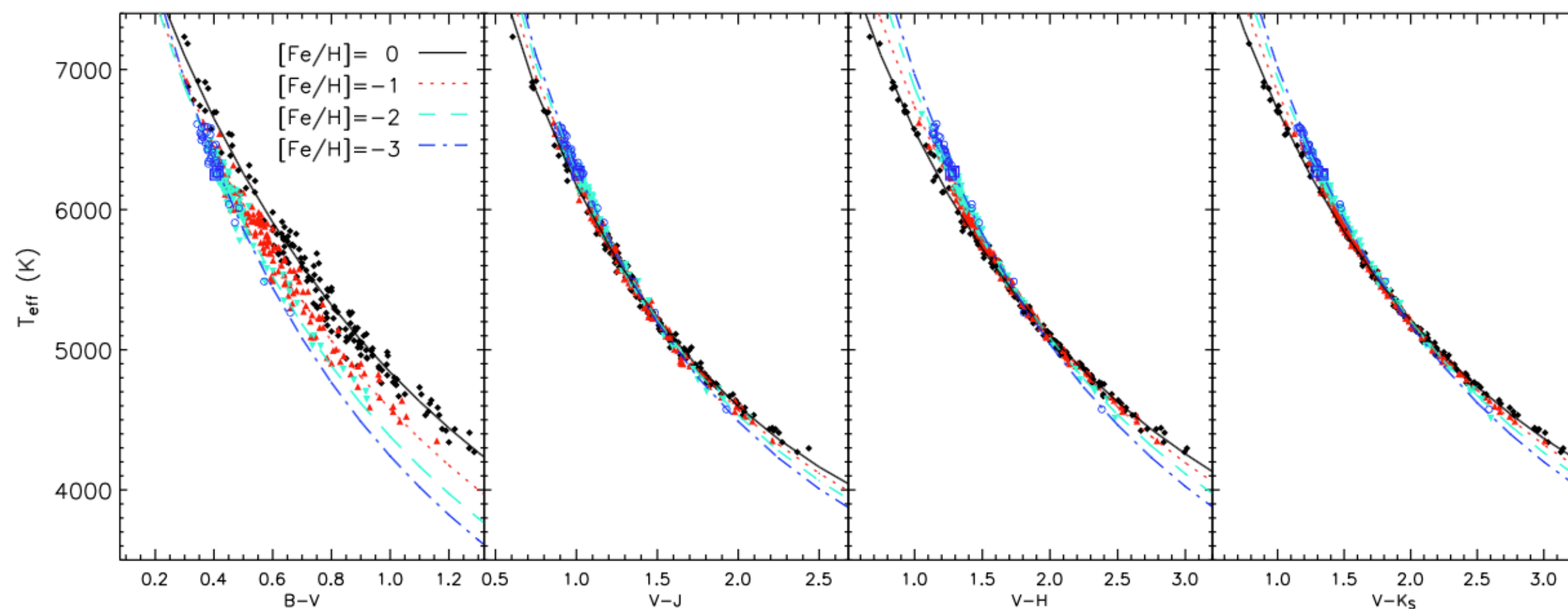
## High-Resolution Spectroscopy



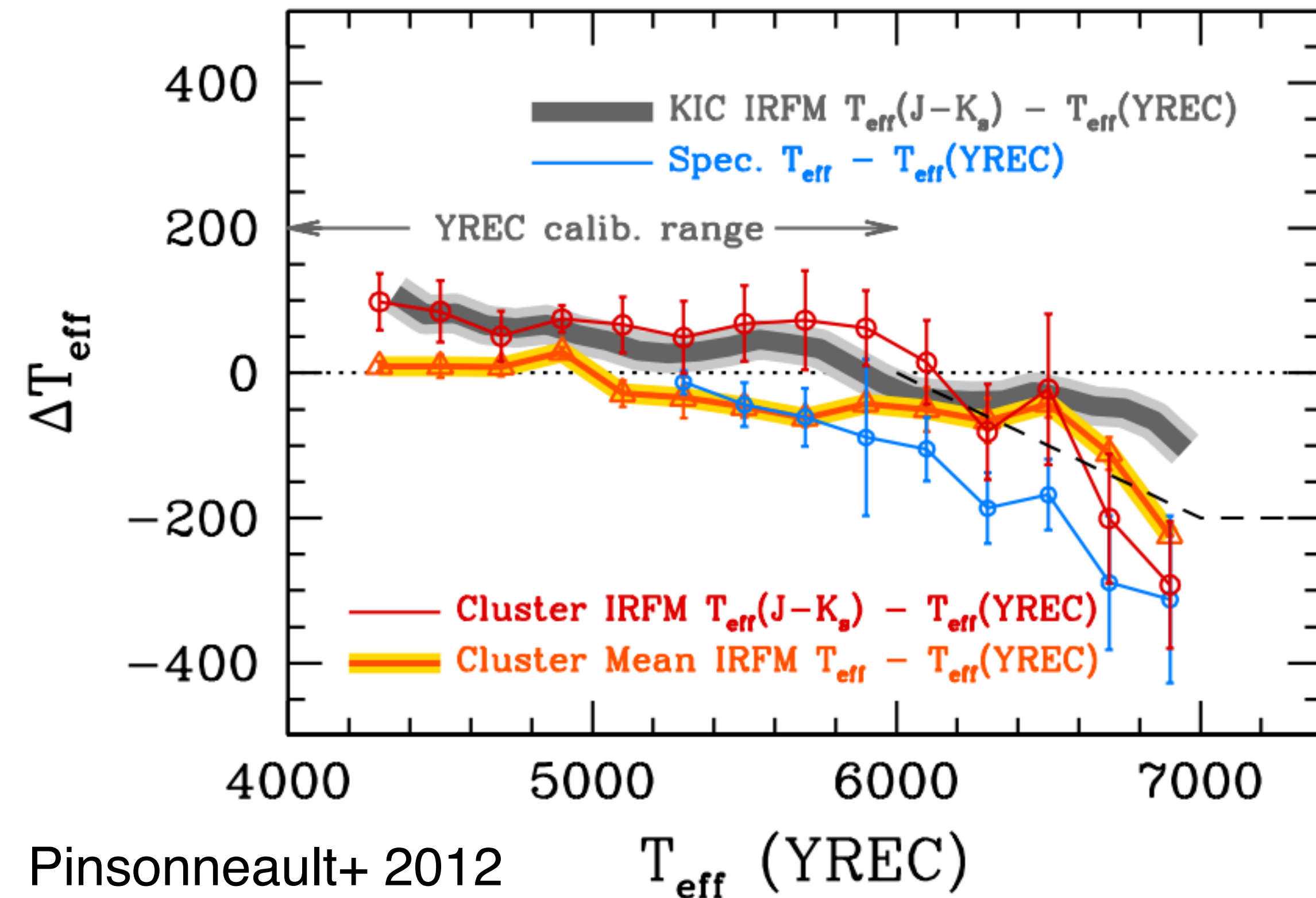
Petigura 2015

$T_{\text{eff}}$  from different methods (and absolute scale) can vary by up to ~2%.  
Sets a floor of ~4% on stellar radii!

## Color- $T_{\text{eff}}$ Relations, SED, IRFM



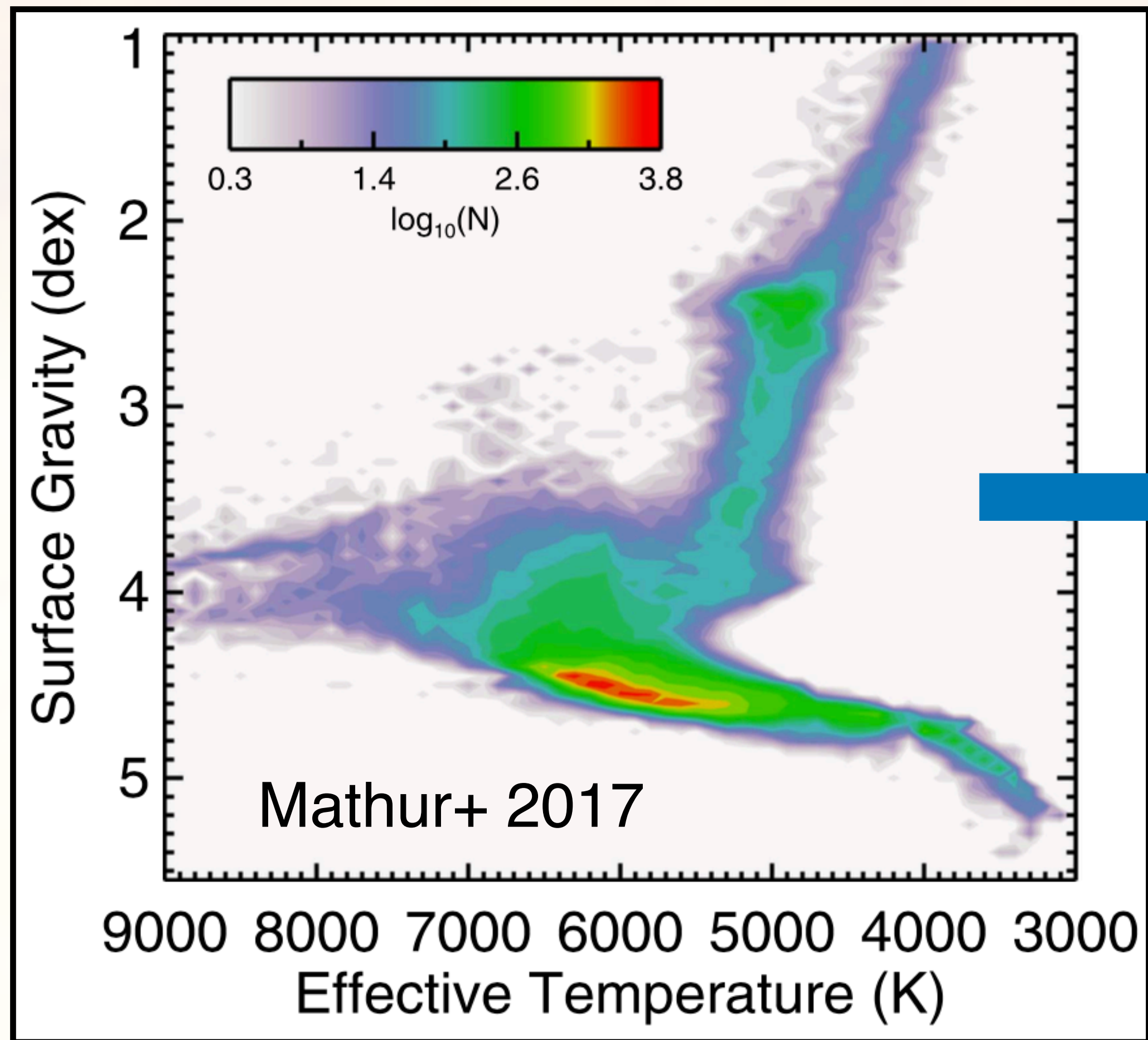
Casagrande+ 2010



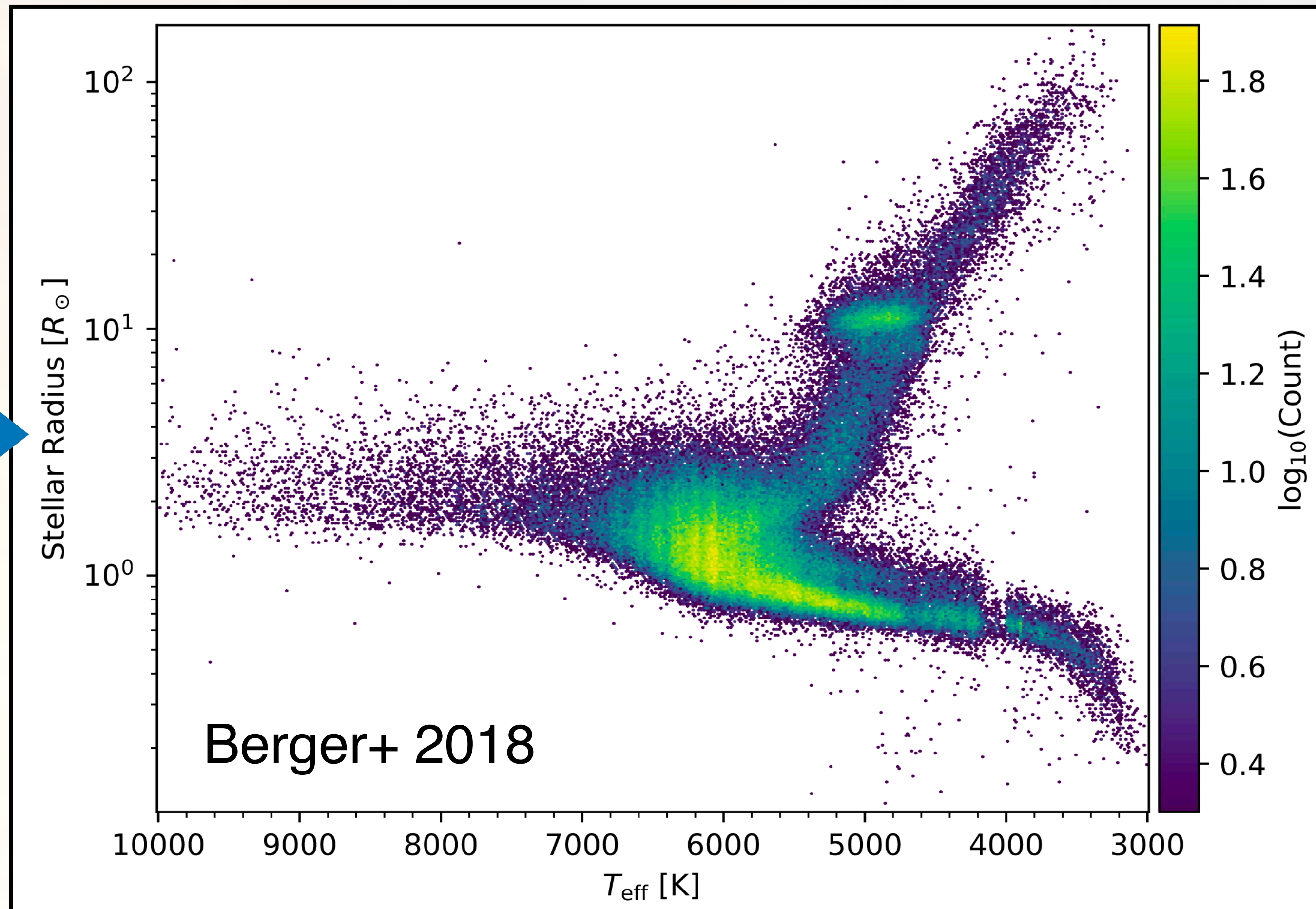
Pinsonneault+ 2012



# pre-Gaia



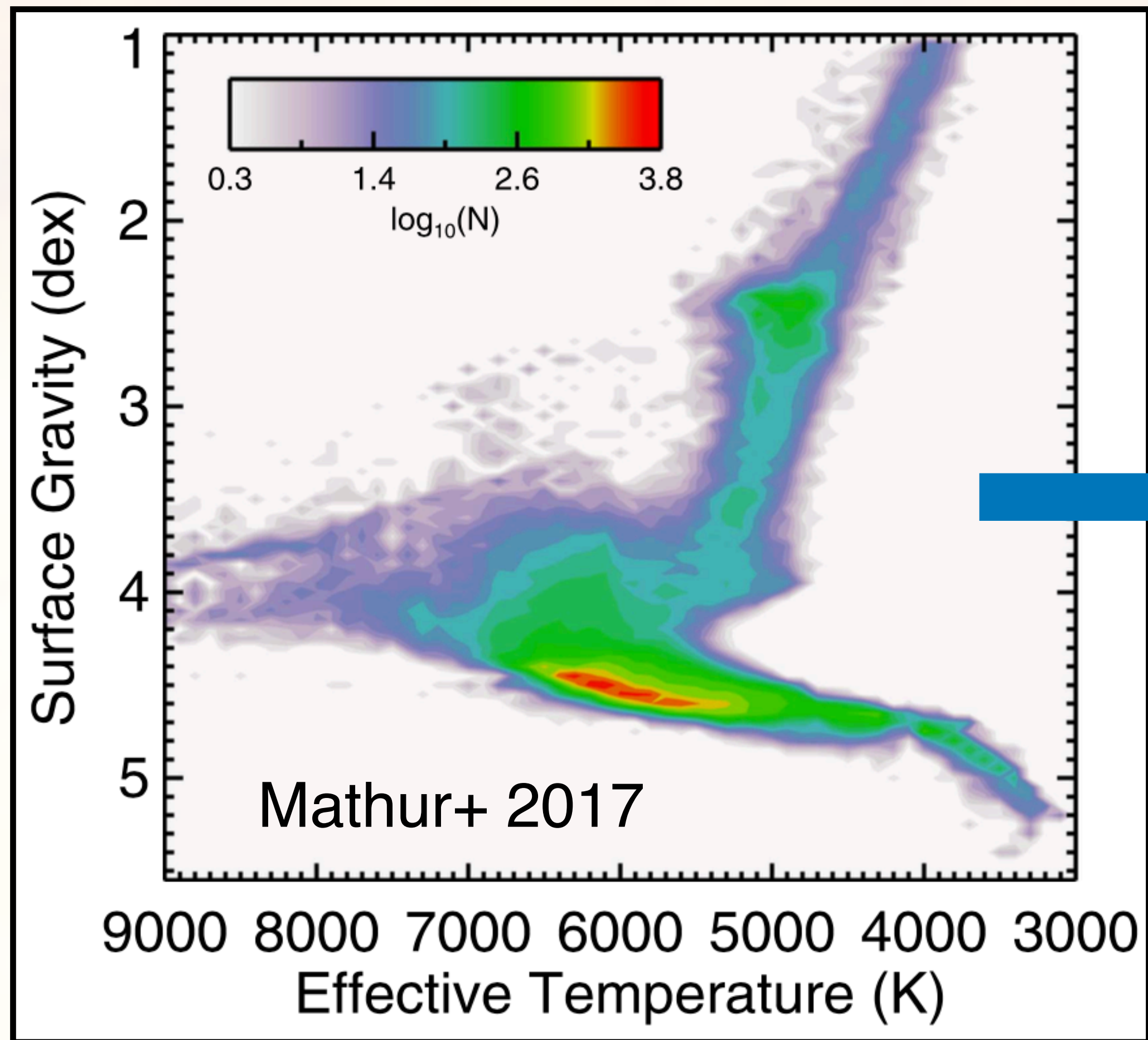
# post-Gaia



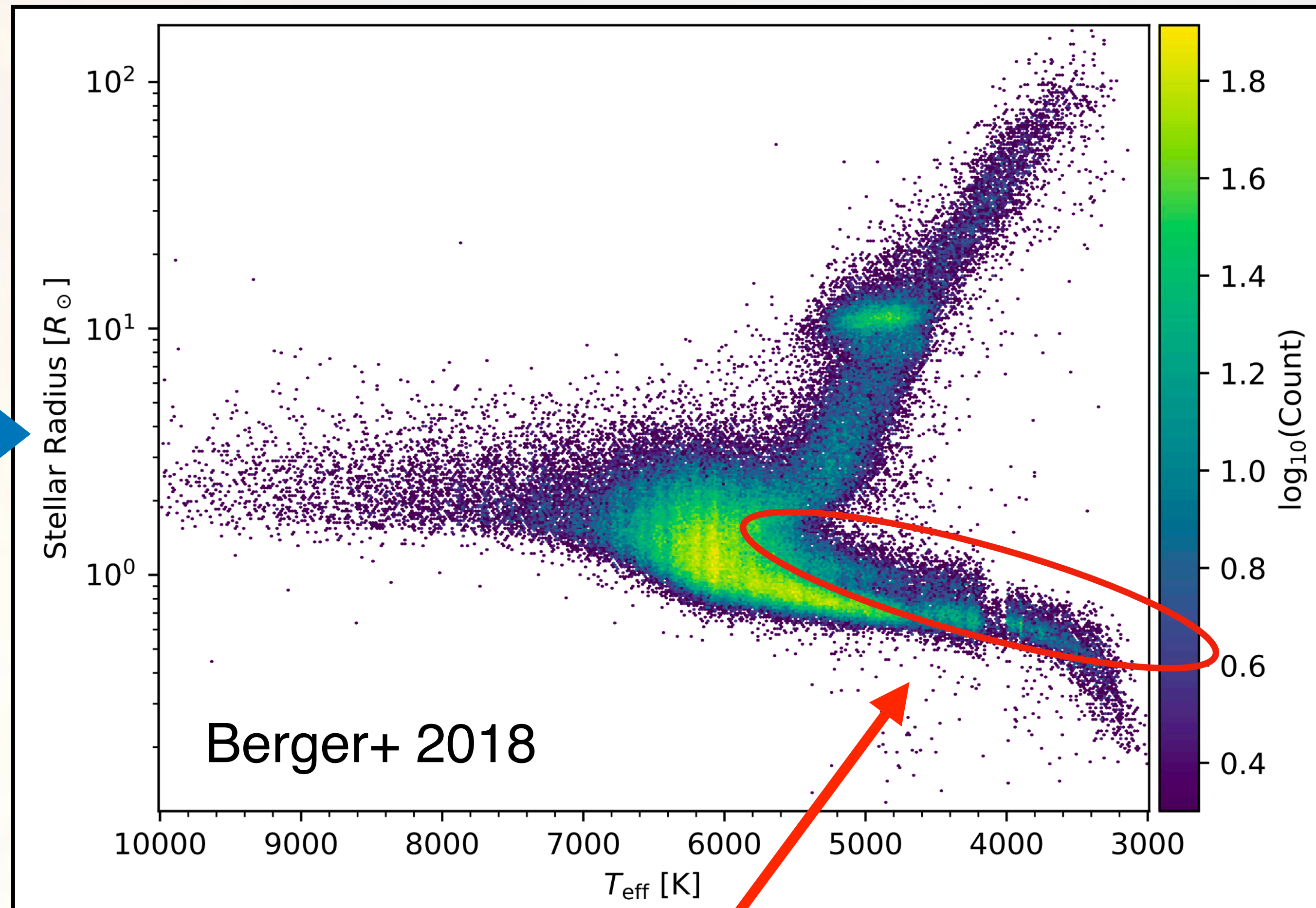
Gaia parallaxes decreased radius uncertainties for Kepler stars by a factor of  $\sim 5-6$ !



# pre-Gaia



# post-Gaia



Challenge (opportunity?): **unresolved binaries**. In general, causes overestimation of L and underestimation of  $T_{\text{eff}}$

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**Density ( $\rho$ )**

**Age**

“Easy”

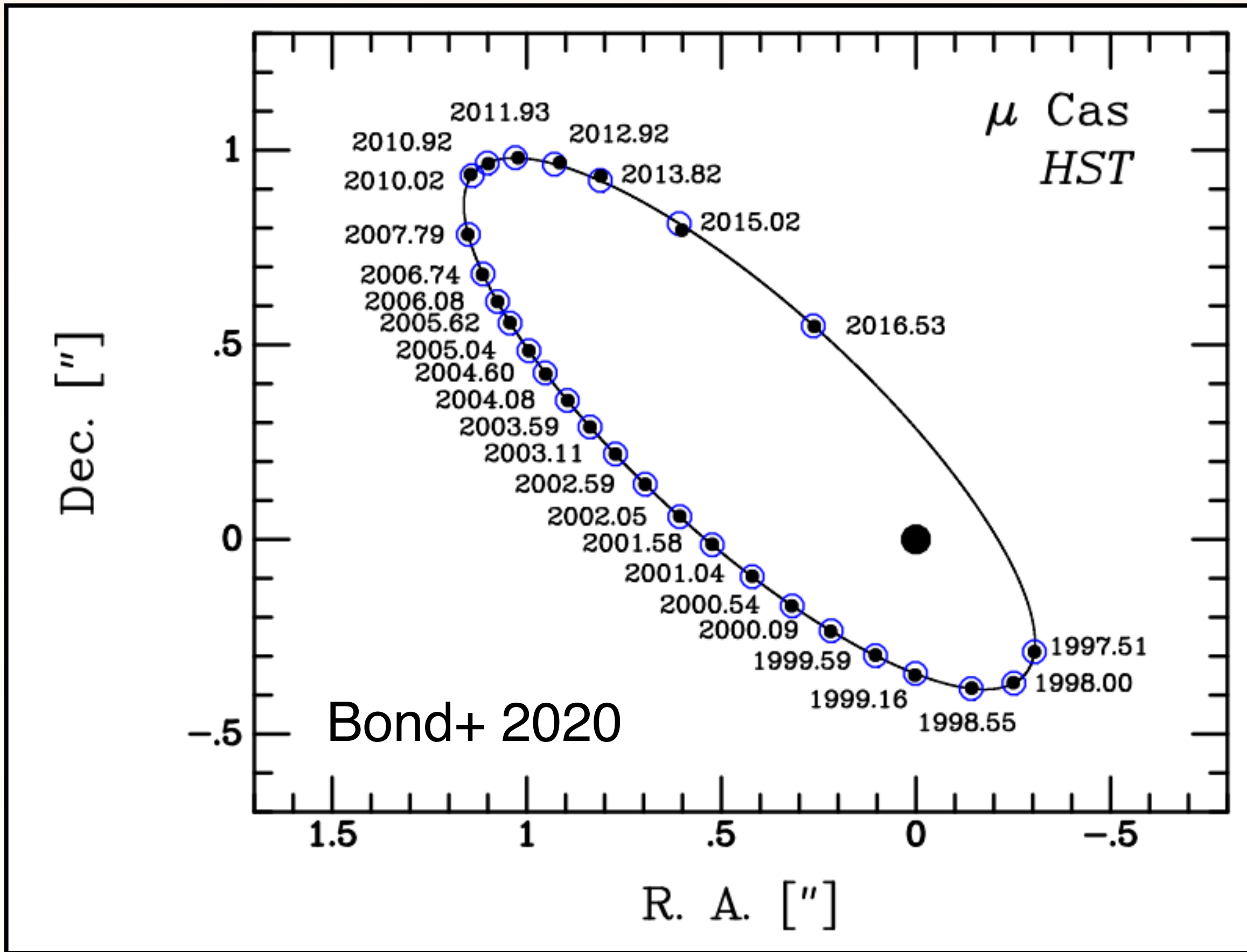
Possible

Hard

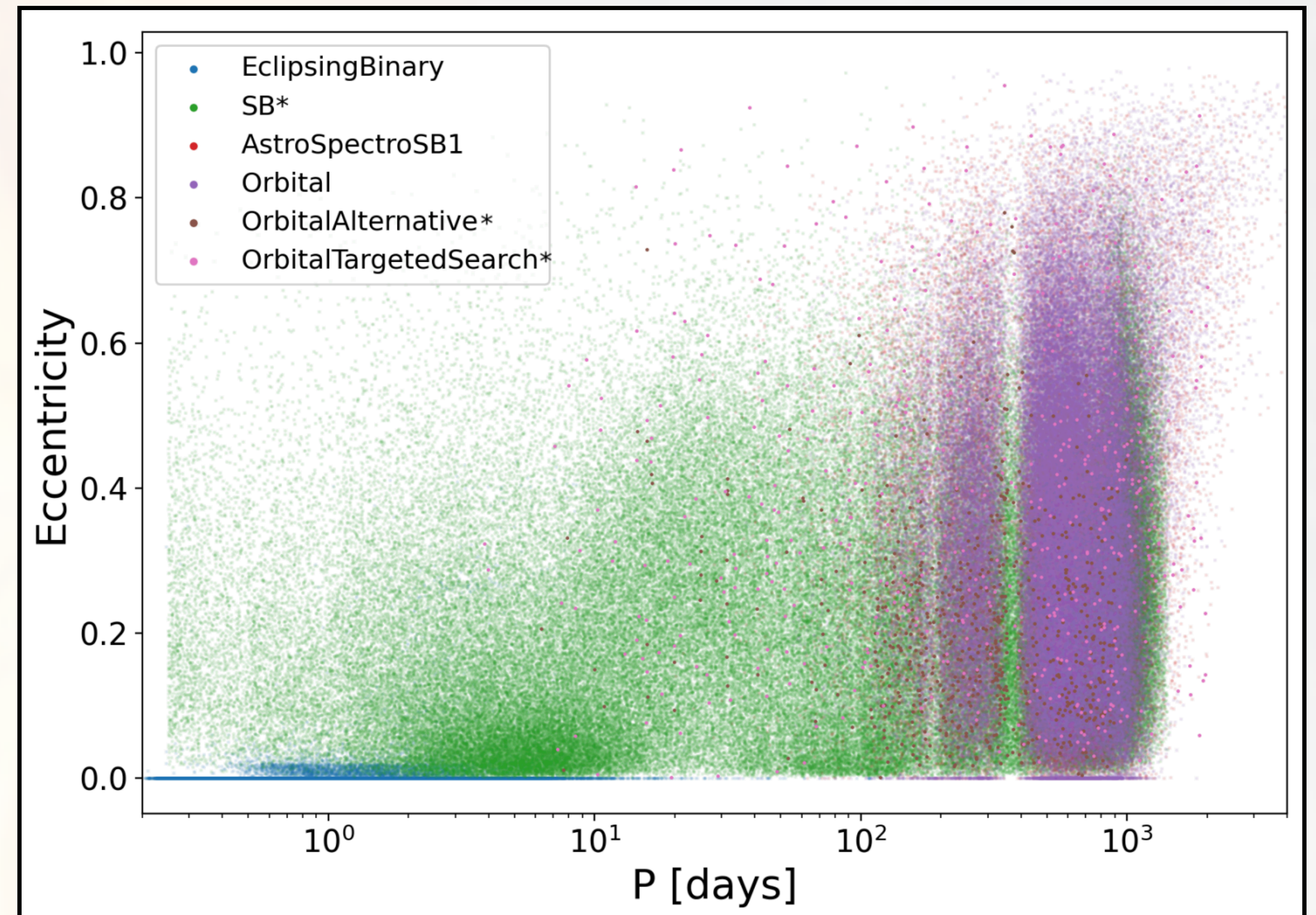
*Astrometry is critical for  
inferring ~ all  
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parameters of stars*



# Dynamical Masses from Astrometry



A hidden treasure:  $\sim 10^5$  astrometric solutions from Gaia



**$\sim 1-2\%$   
Masses!**

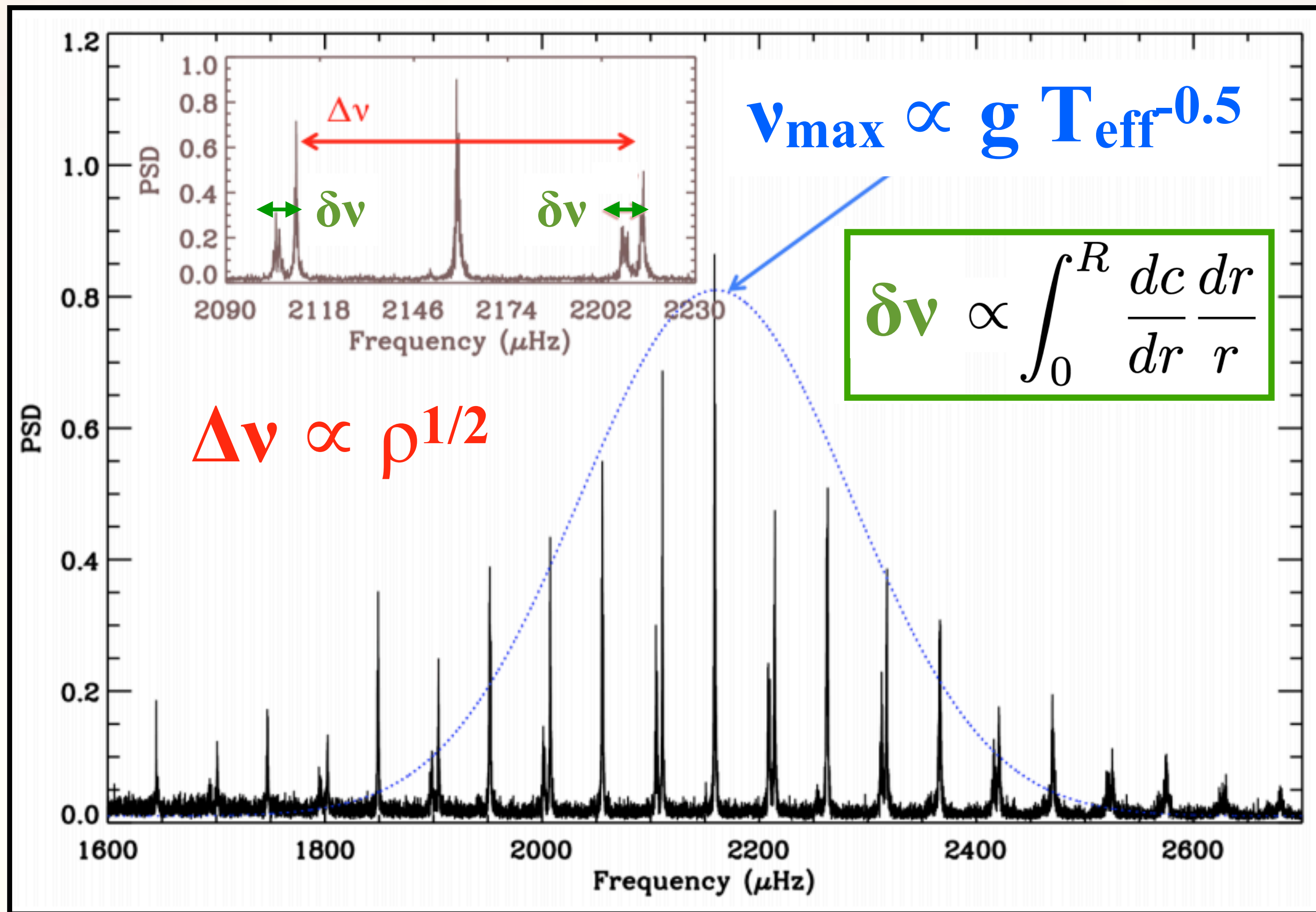
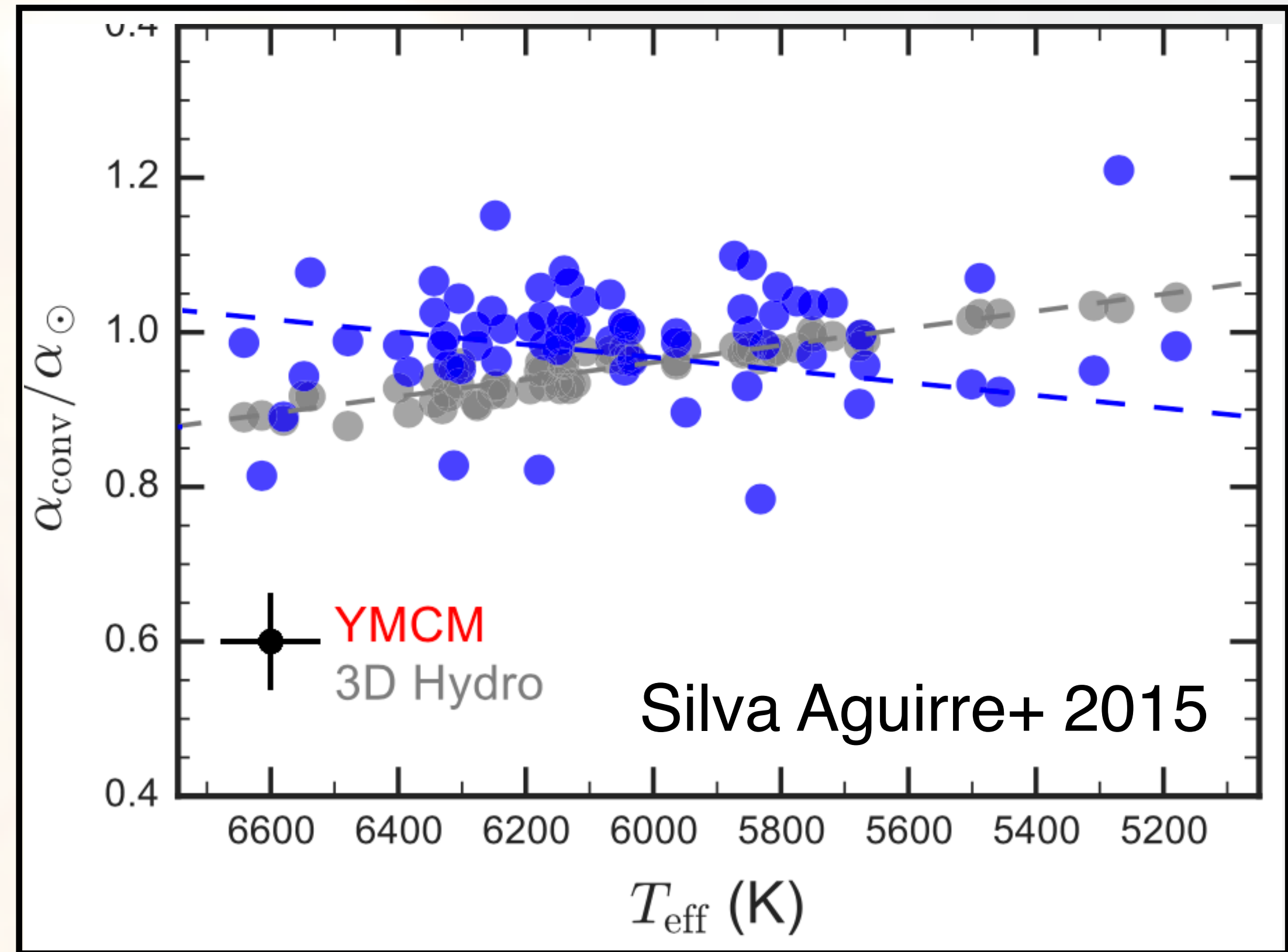
Quantity	This paper
Total mass, $M_A + M_B$	$0.9168 \pm 0.0148 M_\odot$
Mass of $\mu$ Cas A, $M_A$	$0.7440 \pm 0.0122 M_\odot$
Mass of $\mu$ Cas B, $M_B$	$0.1728 \pm 0.0035 M_\odot$

Gaia Collaboration+ 2022



# Asteroseismology: Densities, $\log(g)$ & Ages

Gaia luminosity is an important external constraint for testing model physics (e.g. convection)



Garcia & Ballot 2019



# Masses & Ages of Single Stars: “Isochrone” Fitting

Models (**Mass, Age, Composition**) predict quantities to be compared to observations ( $T_{\text{eff}}$ ,  $L$ ,  $[M/H]$ , absolute mag, colors)

Available software tools (incomplete list!):

*isochrones*: <https://github.com/timothymorton/isochrones>

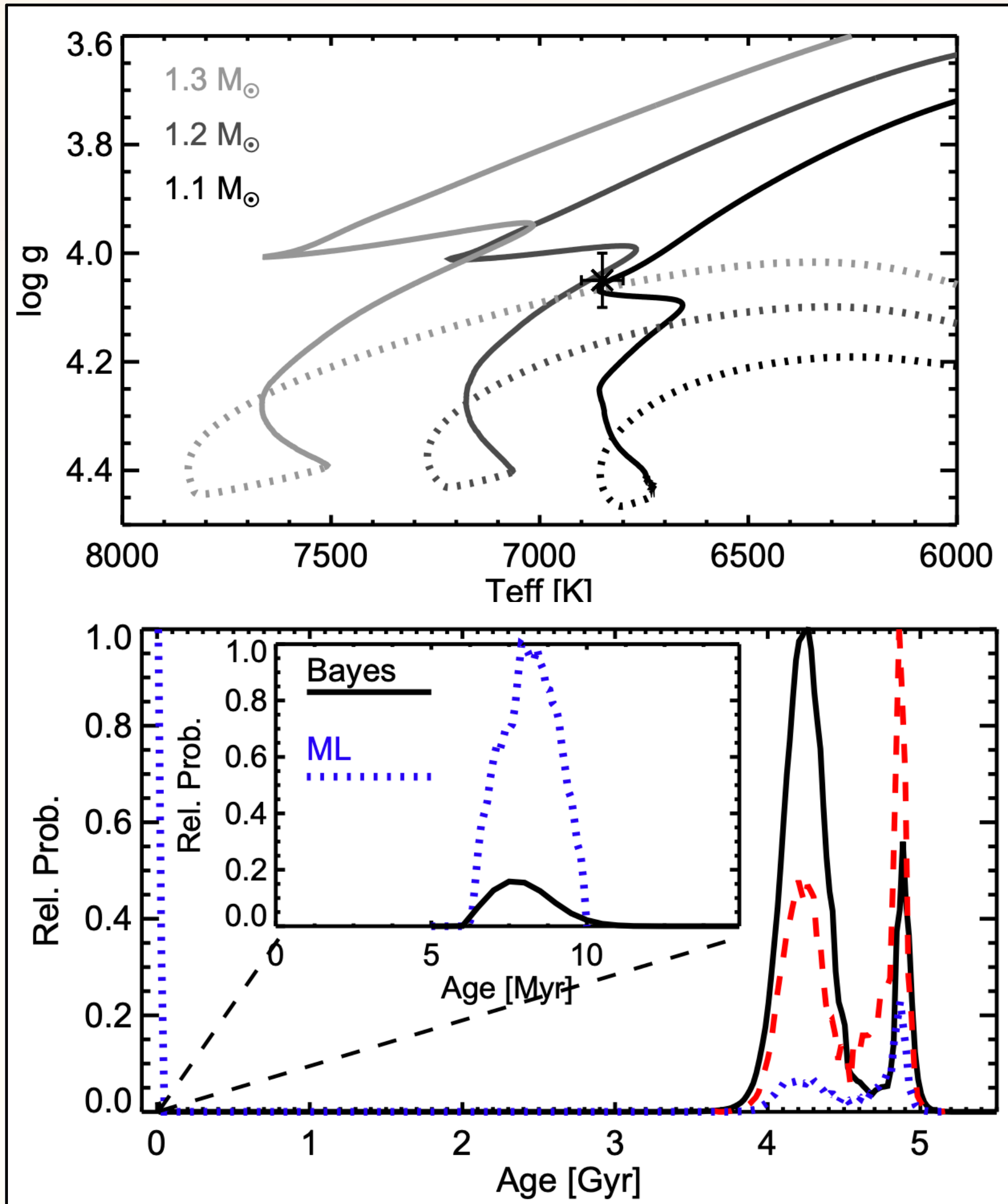
*isoclassify*: <https://github.com/danxhuber/isoclassify>

*BASTA*: <https://github.com/BASTAcode/BASTA>

*Param*: <http://stev.oapd.inaf.it/cgi-bin/param>

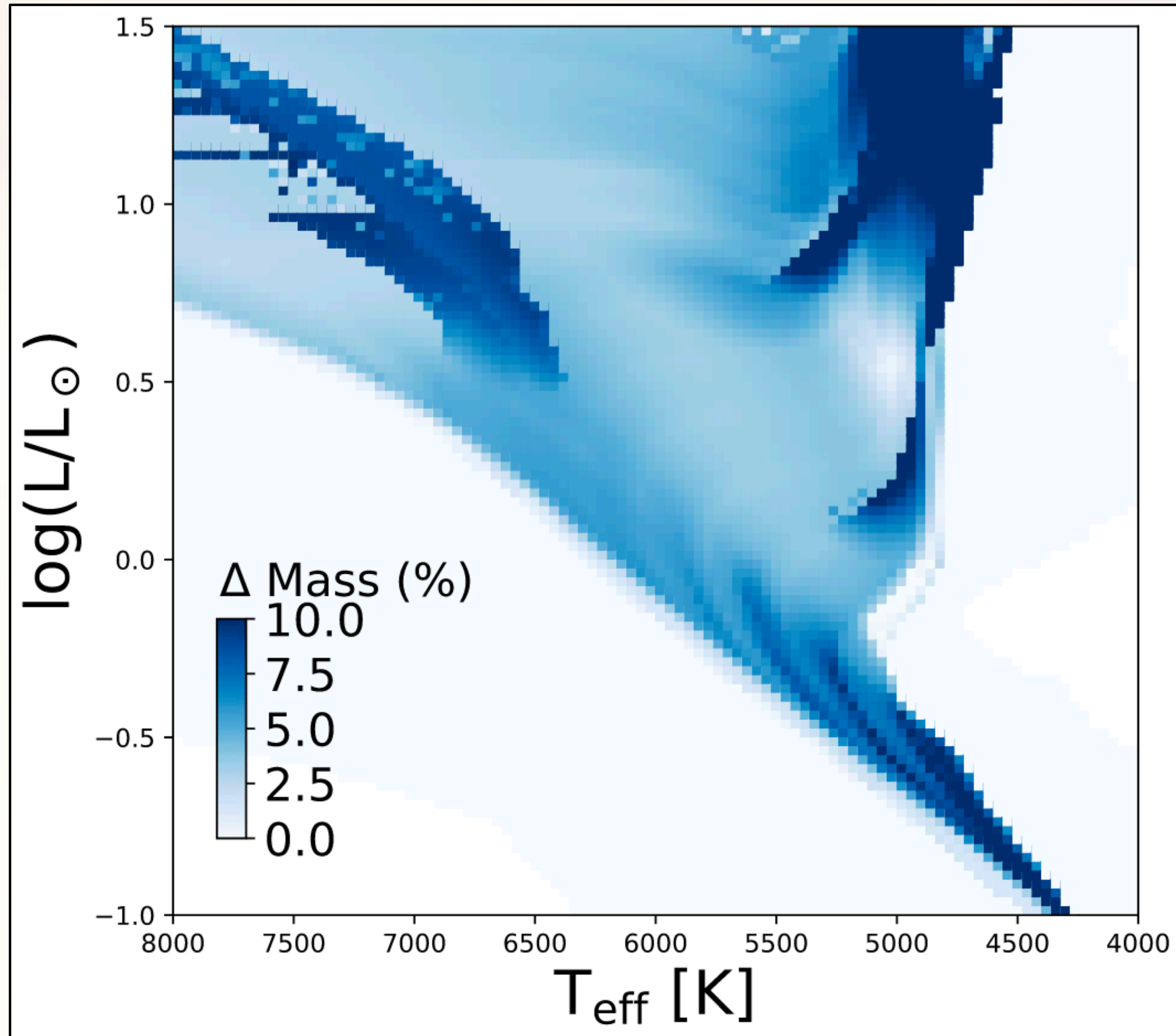
Morton+ 2015, Huber+ 2017, Silva Aguirre+ 2022, da Silva+ 2006

**Age diagnostics not discussed here:** rotation, chemical abundances, kinematics & clusters  
(*more on this from Melissa & Marina tomorrow!*)



Serenelli+ 2017

# Caveat: Stellar models have systematic errors



Tayar et al. 2022

## Source of systematics:

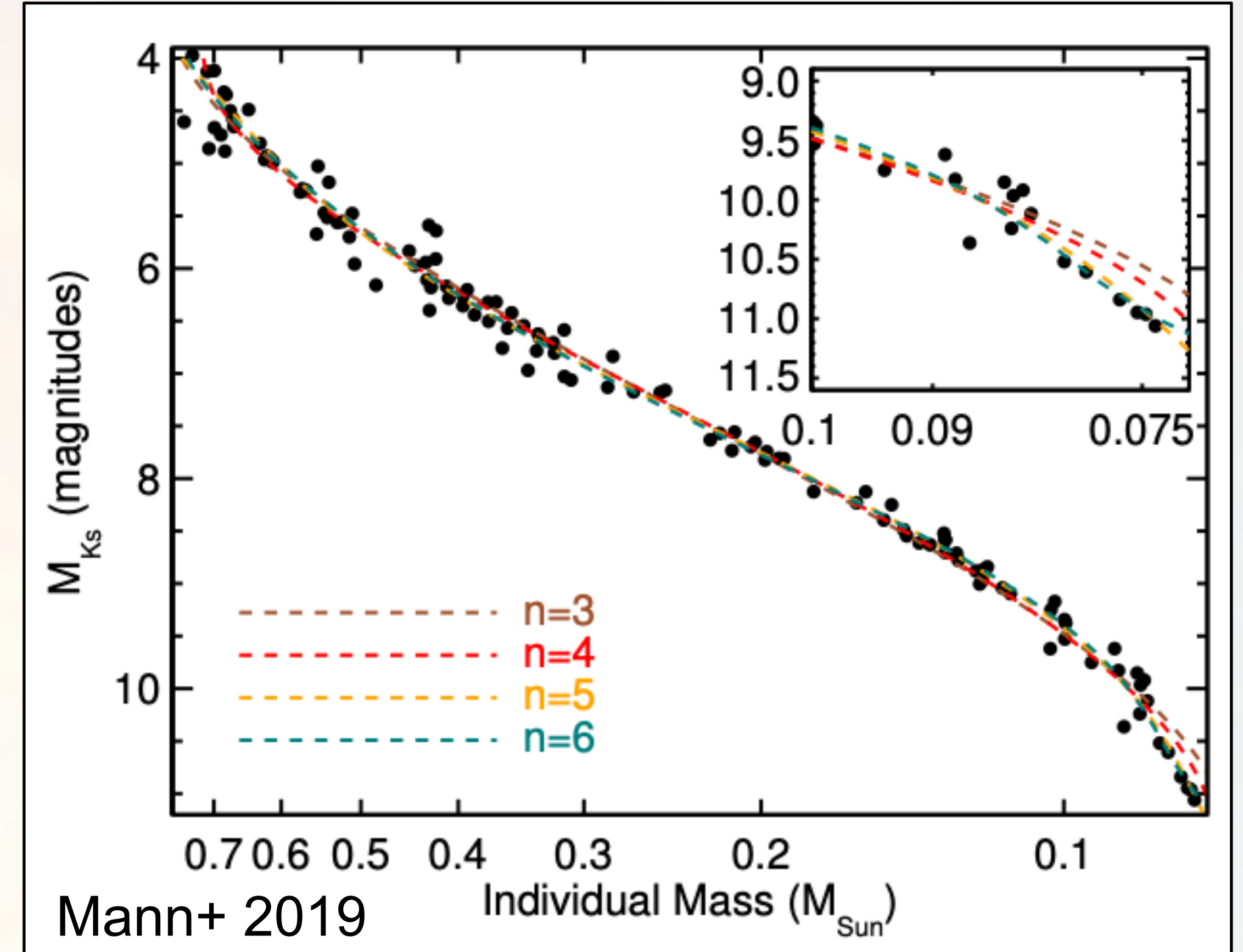
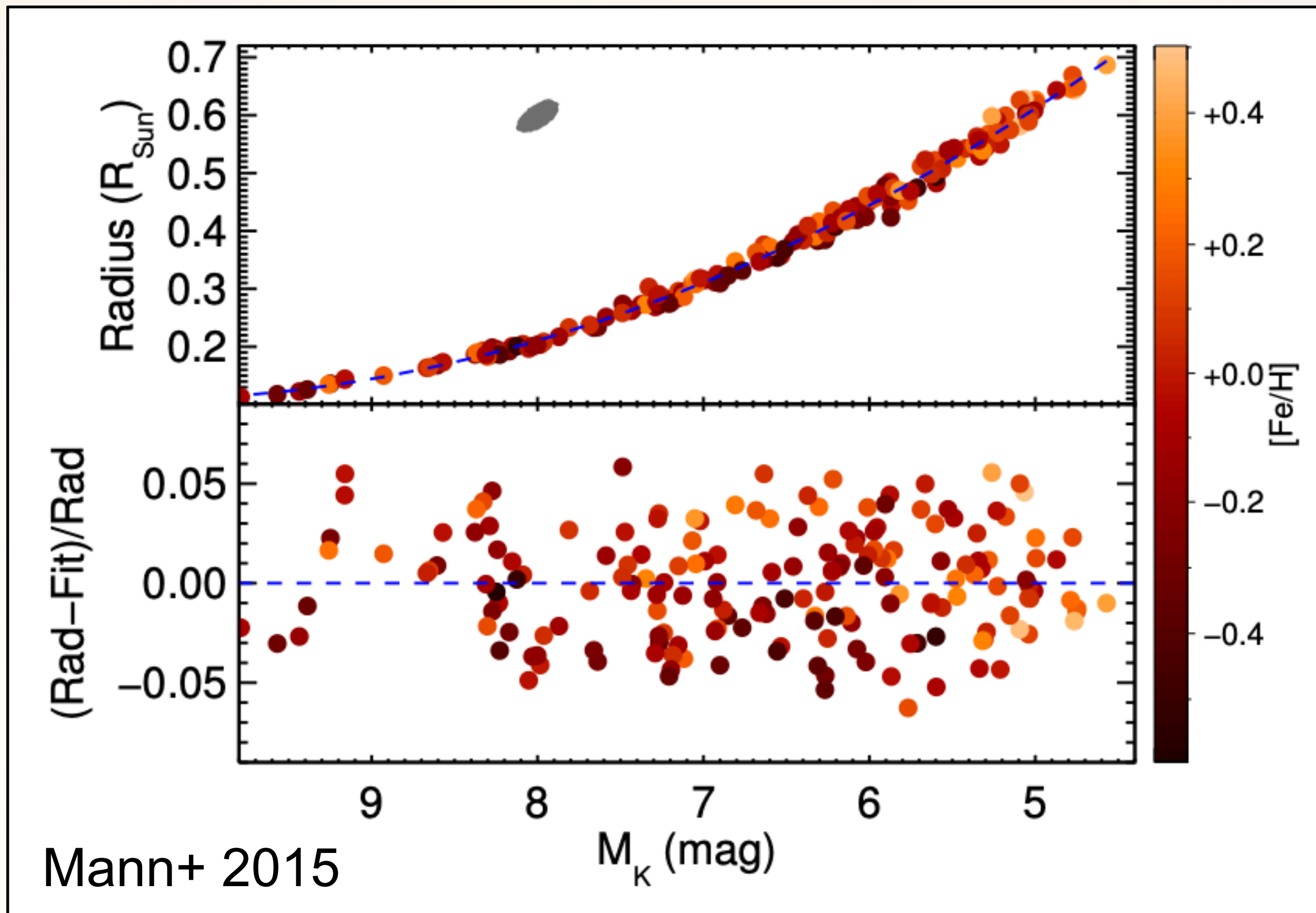
uncertain input physics such as convection, atmospheric boundary conditions, rotation, opacities and overshoot

Sets **error floor of  $\sim 5\%$  in mass and  $\sim 20\%$  in age** for solar-type stars, with variation across HRD

Always a good idea to establish systematic errors by using **different model grids!**



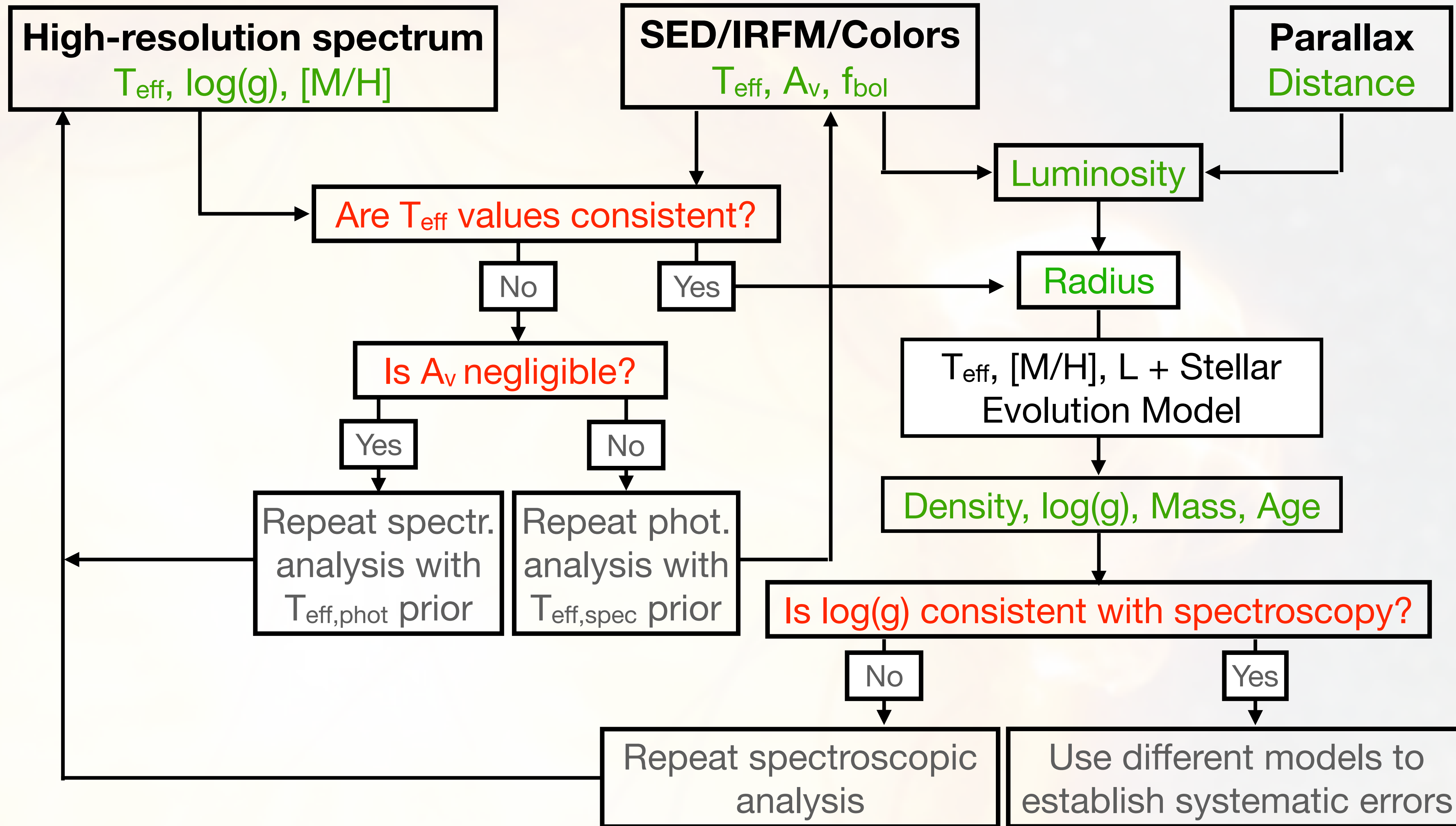
# Empirical Relations for M Dwarfs



**$T_{\text{eff}}$ -L-R-M relations** calibrated using interferometric angular diameters, bolometric fluxes and dynamical masses. Possible because M dwarfs hardly evolve!

# A Stellar Properties “Cook Book”

(for single, solar-type field stars)





*How do Stellar  
Properties Impact  
Exoplanet Properties?*

# Fundamental Properties of Stars

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Density ( $\rho$ )

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*Which stellar parameters are important for understanding exoplanets?*

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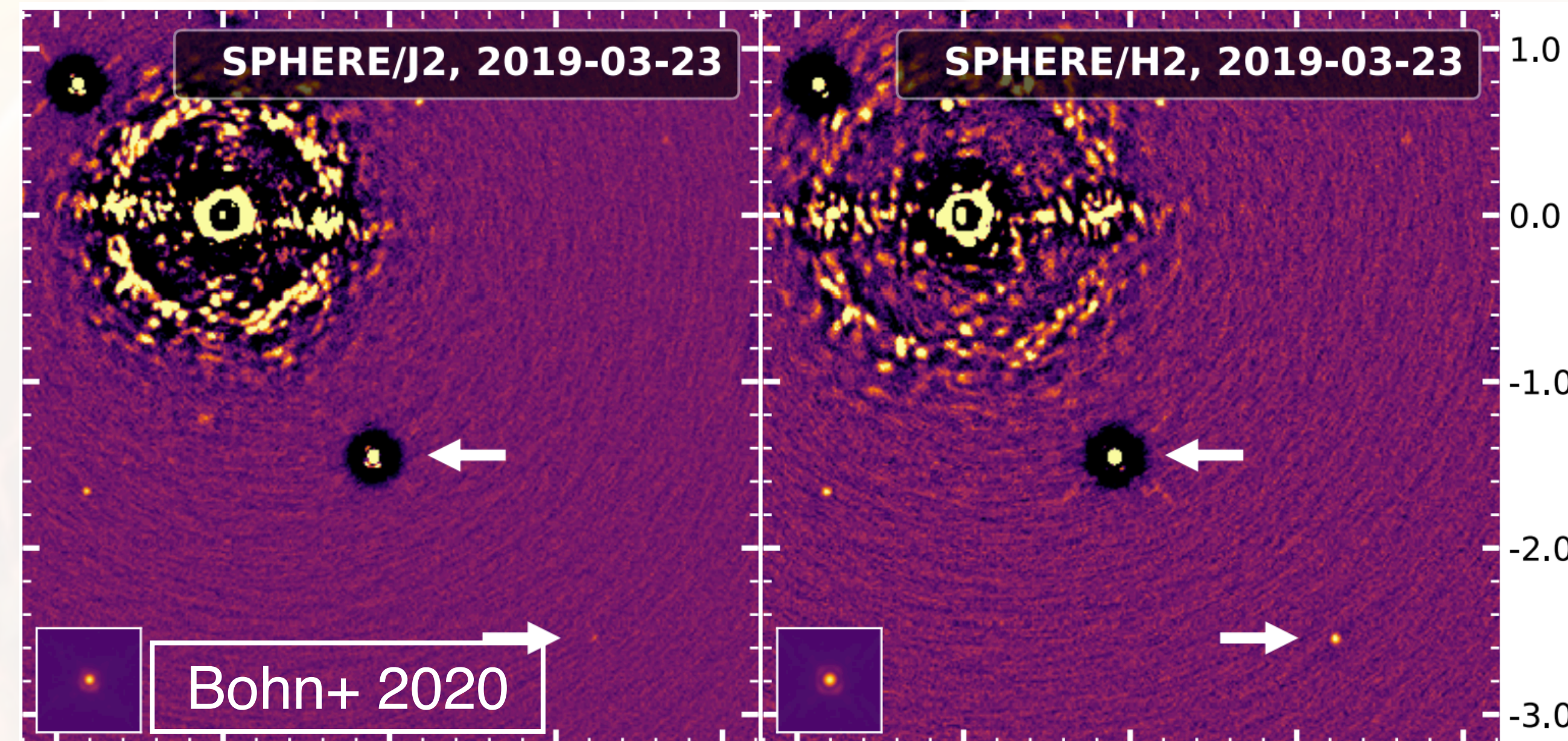
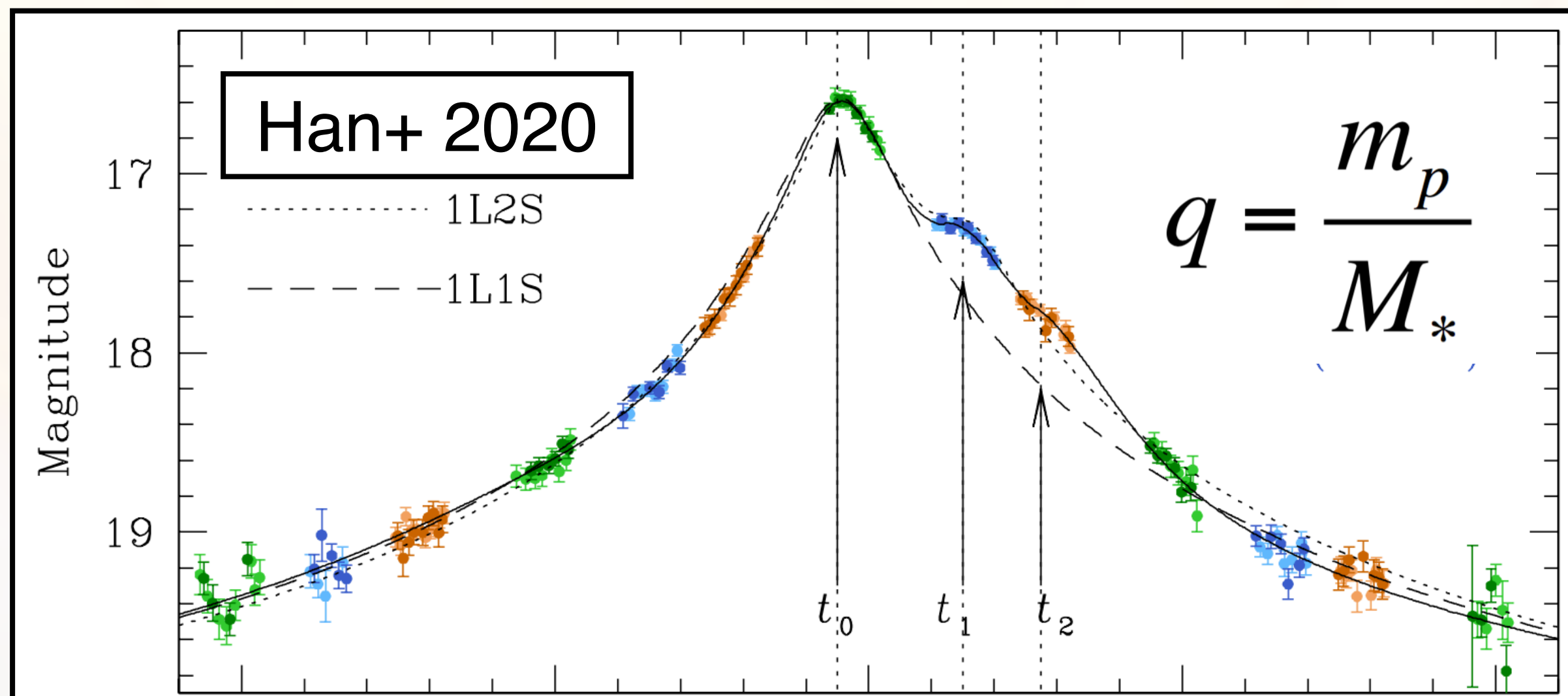
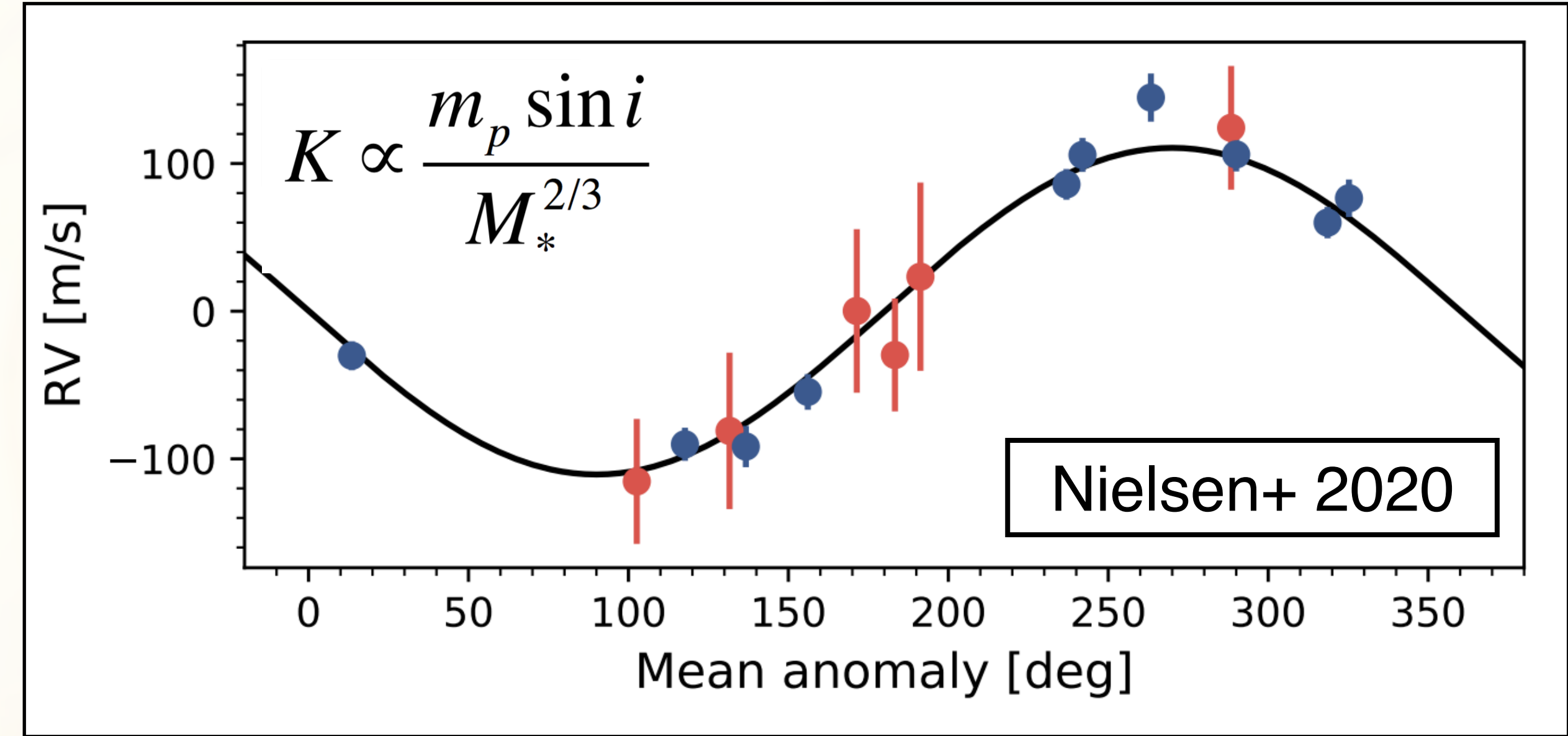
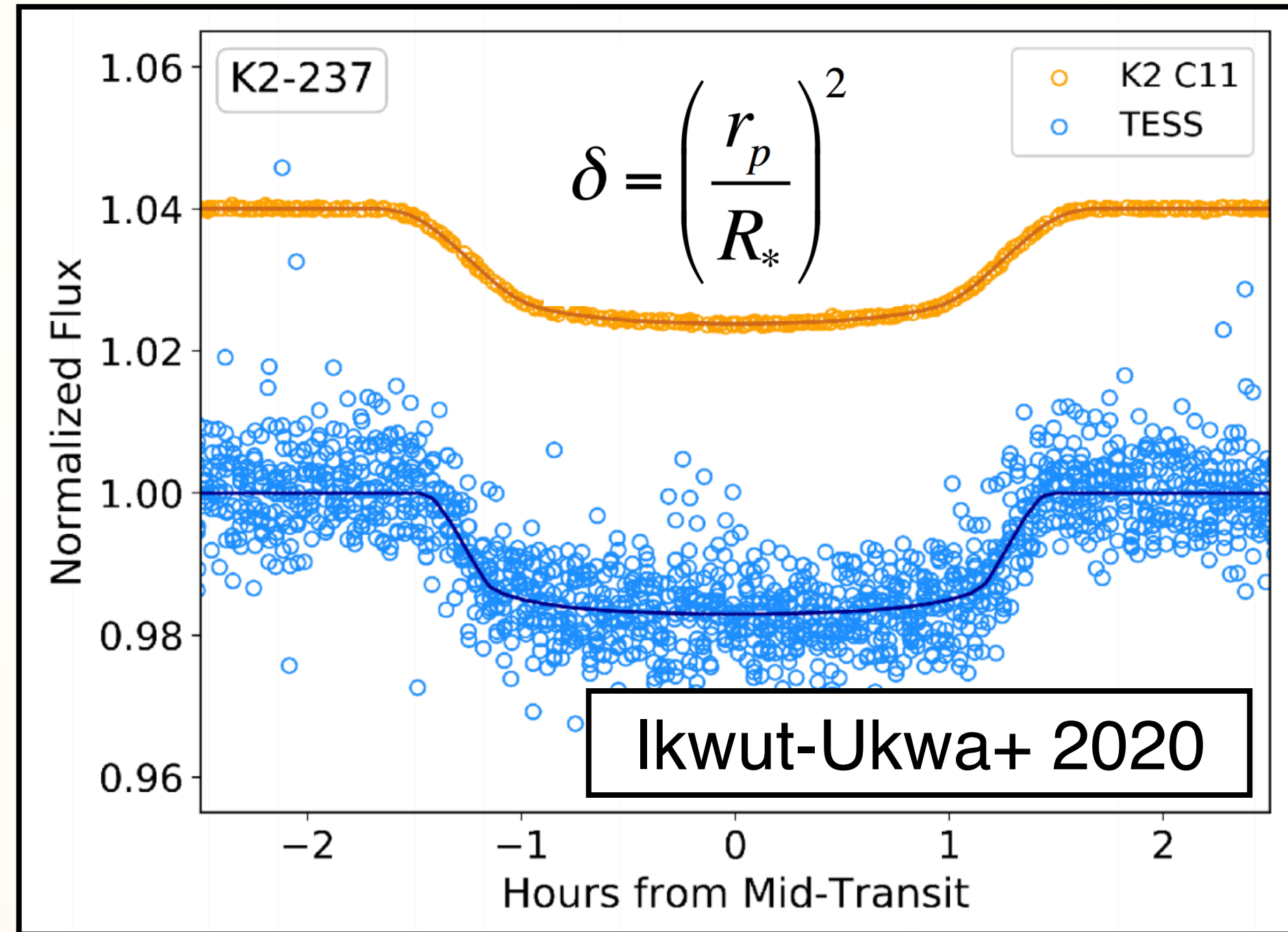
Age

*Which stellar parameters are important for understanding exoplanets?*

*All of them!*

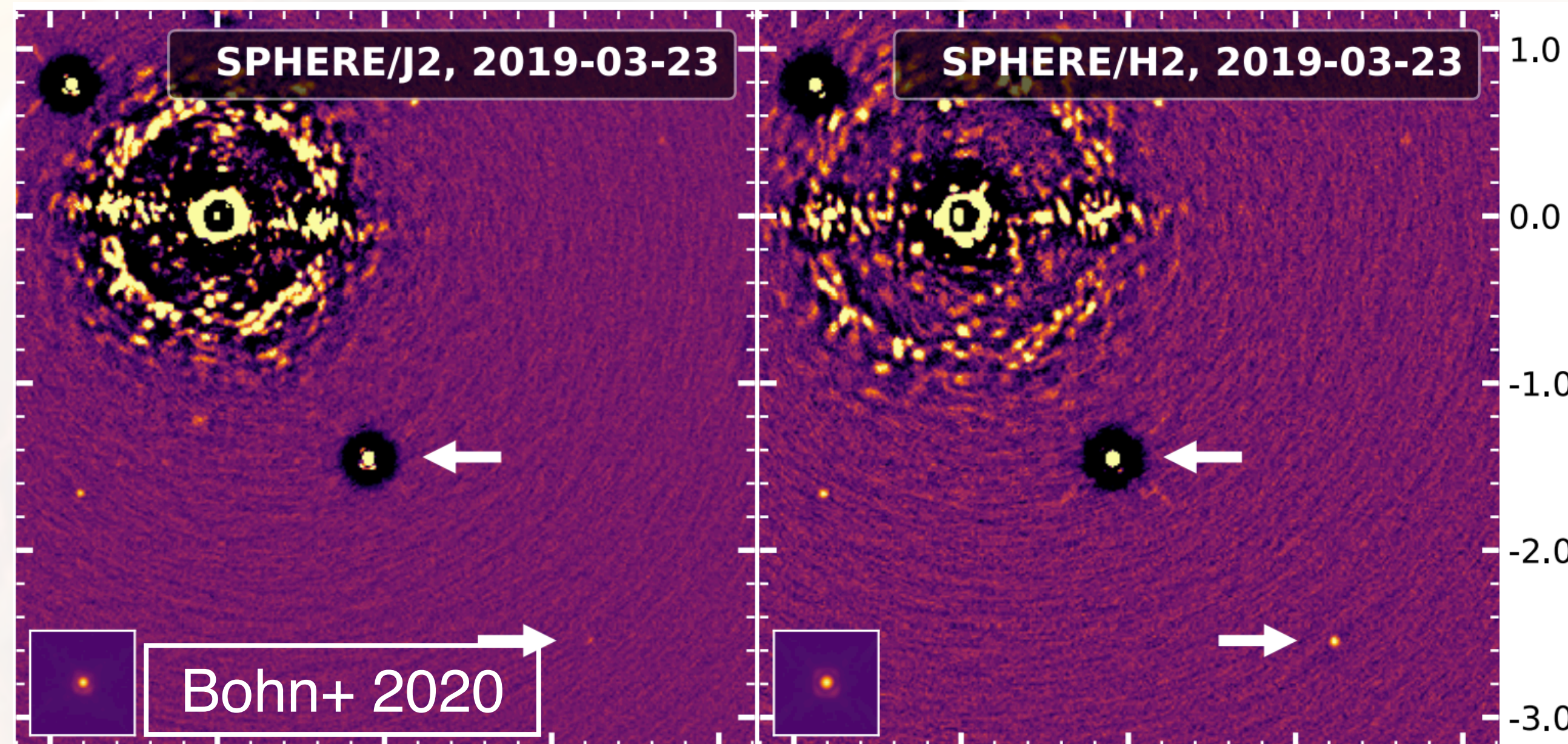
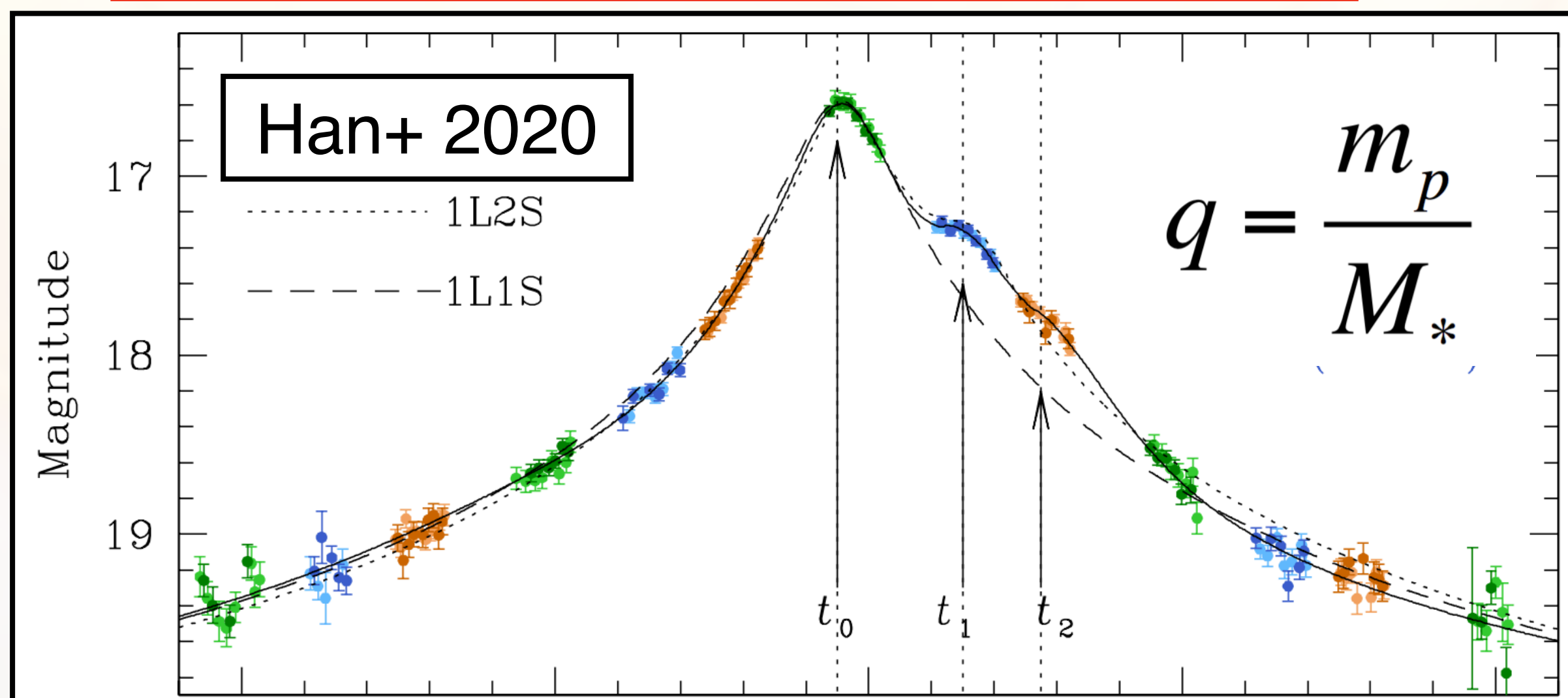
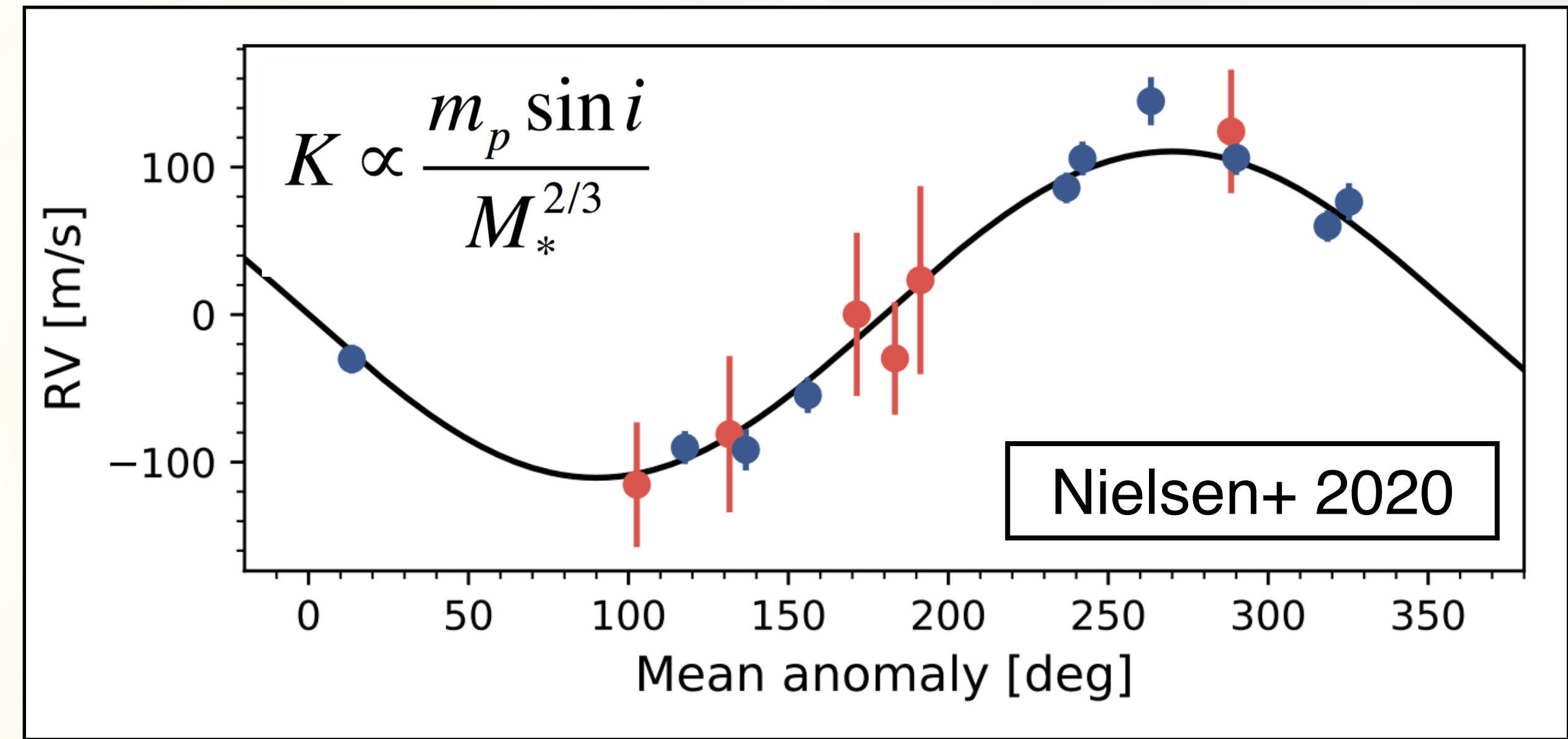
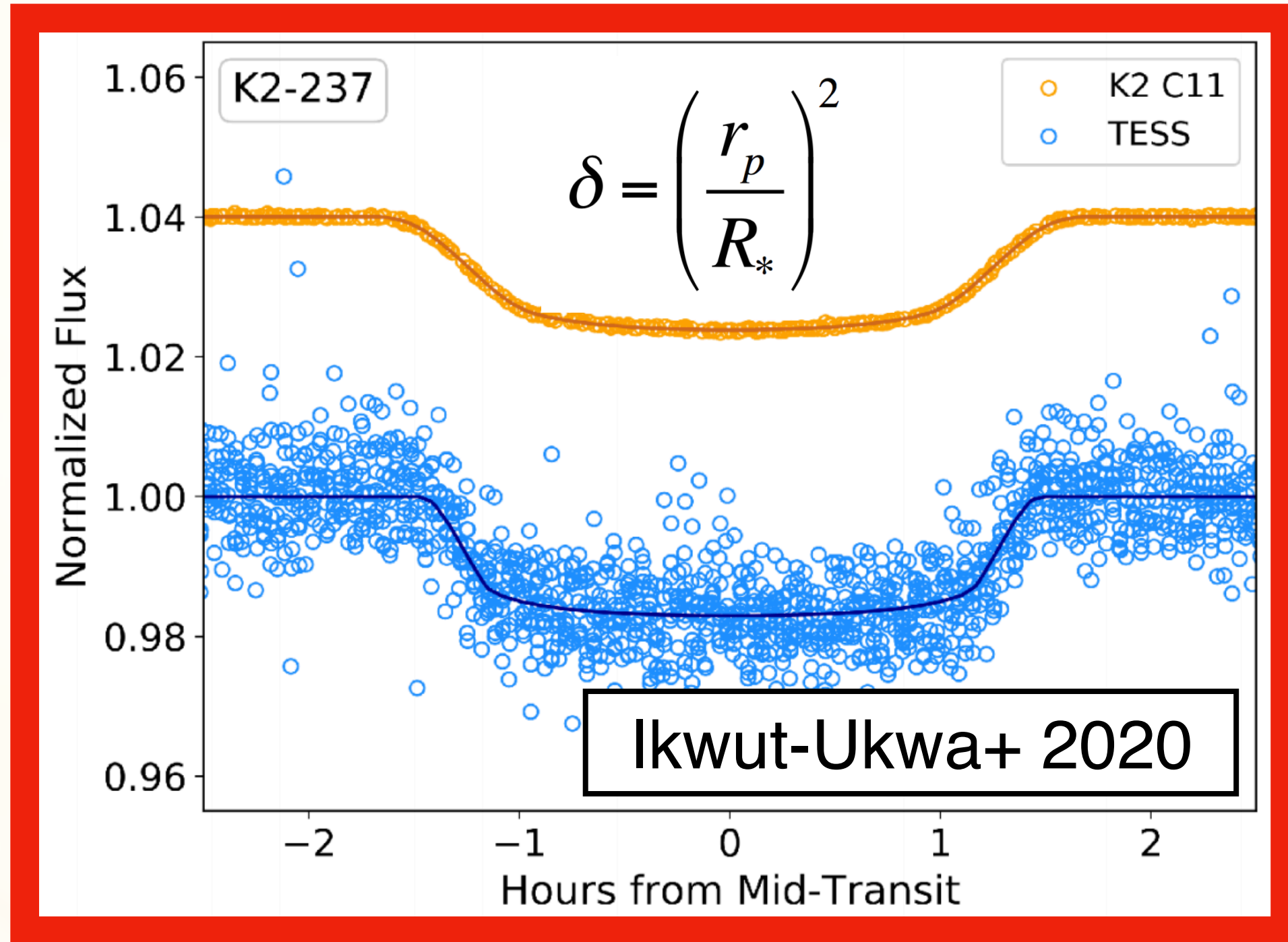


# "Know Thy Star, Know Thy Planet"





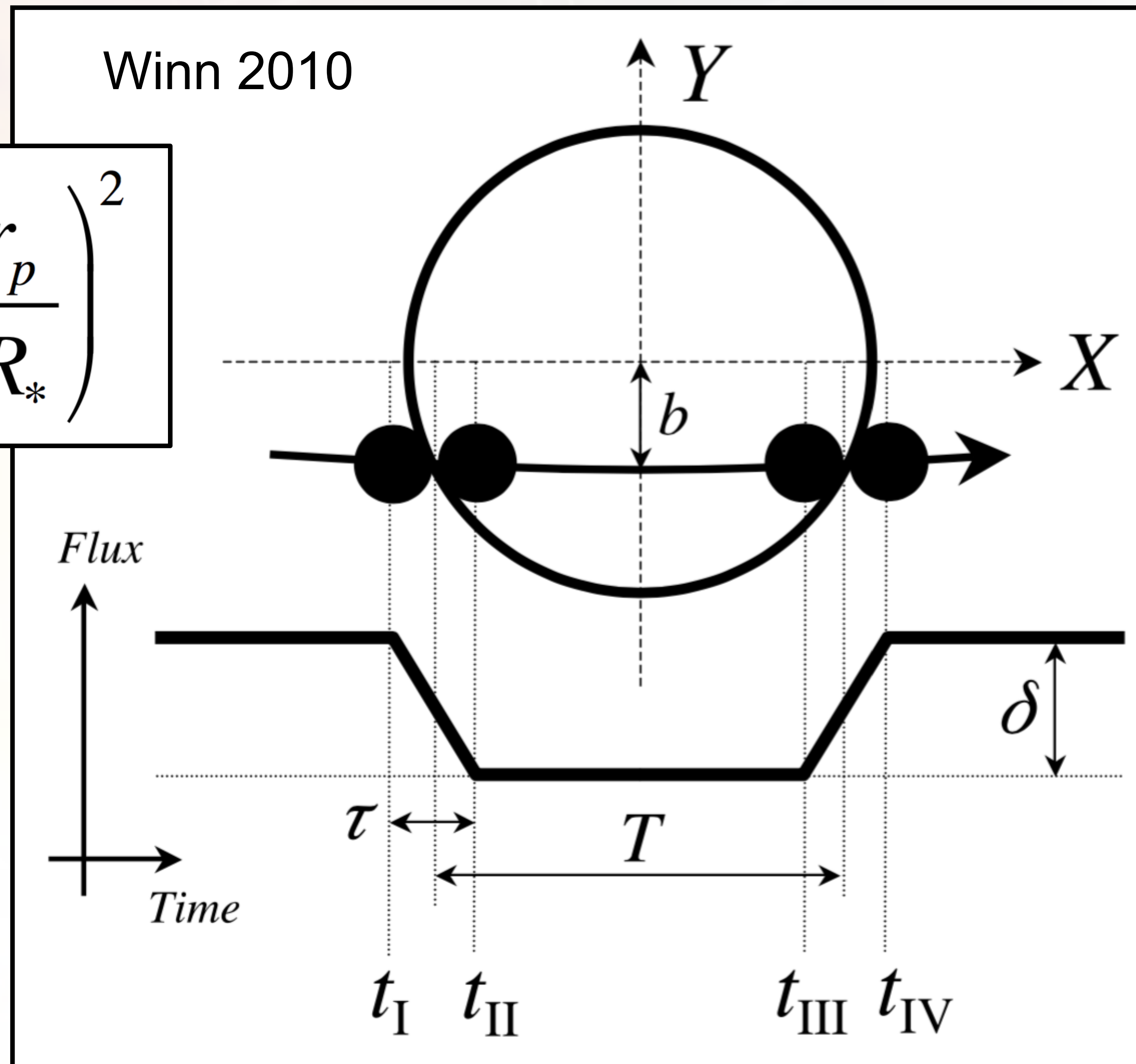
# "Know Thy Star, Know Thy Planet"





Winn 2010

$$\delta = \left( \frac{r_p}{R_*} \right)^2$$

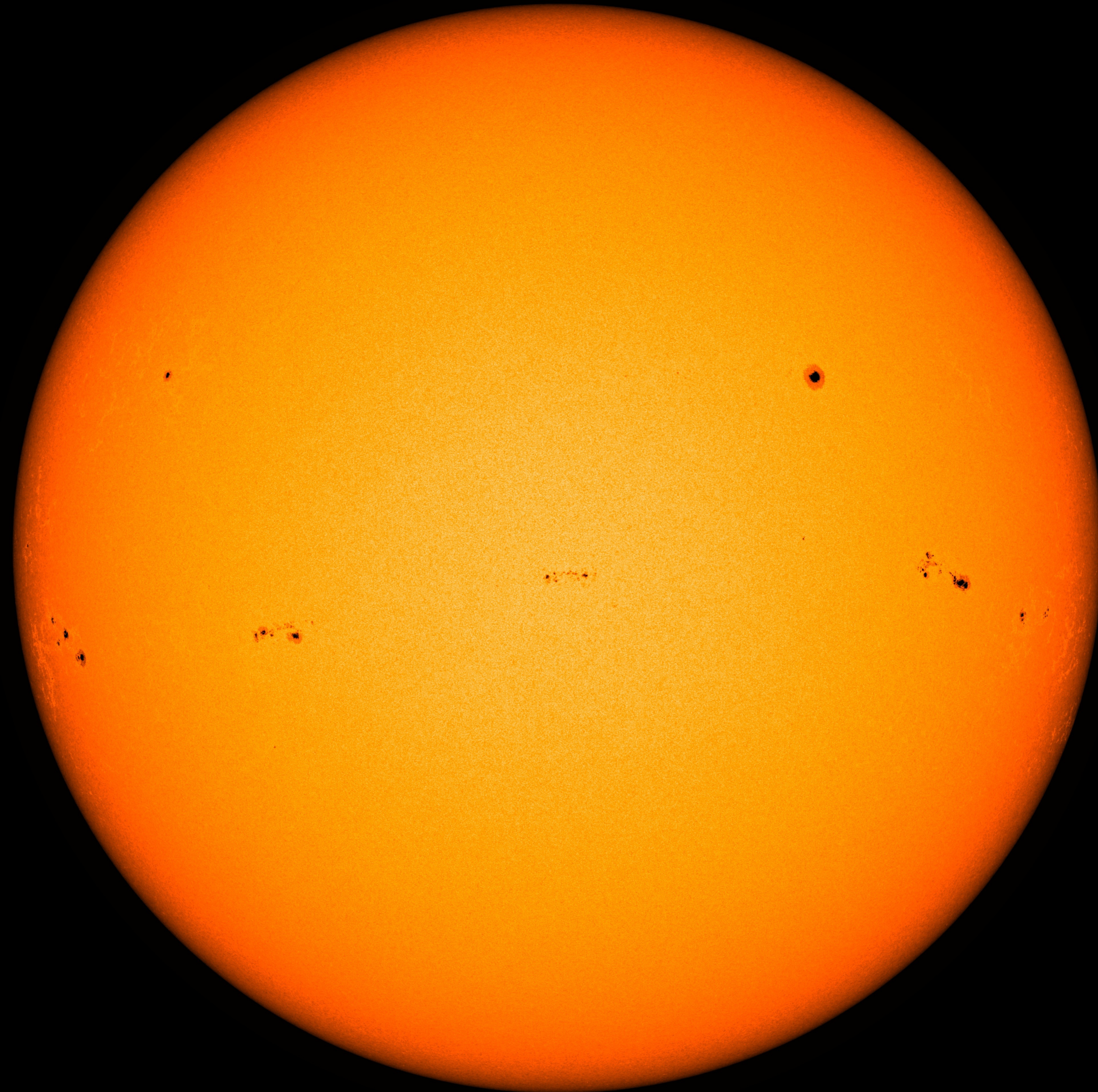


$T$  = Transit Duration

$\tau$  = In/Egress Duration

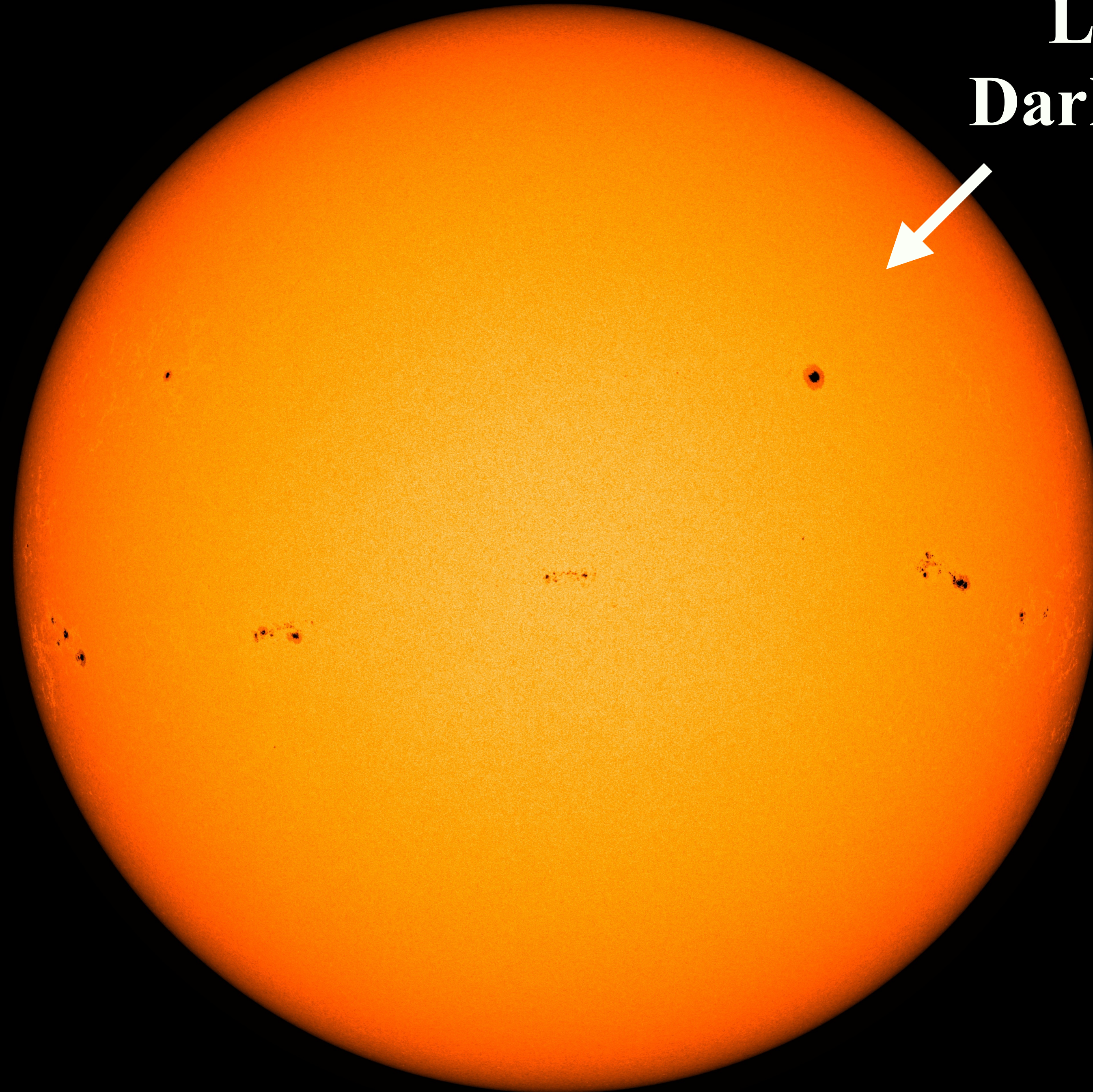
$\delta$  = Transit Depth





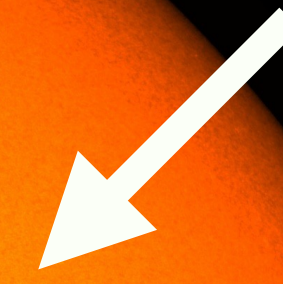


**Limb  
Darkening**



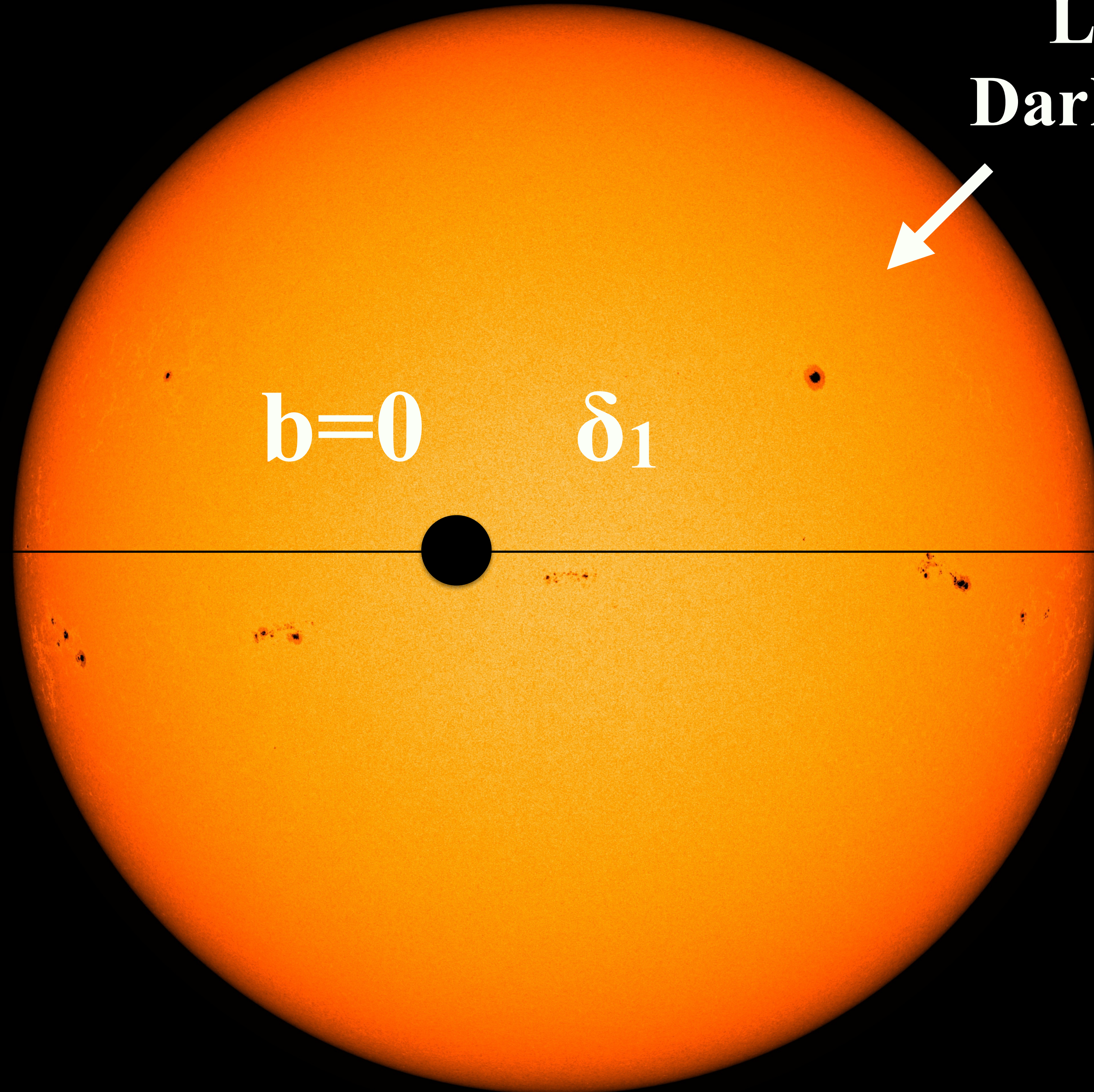


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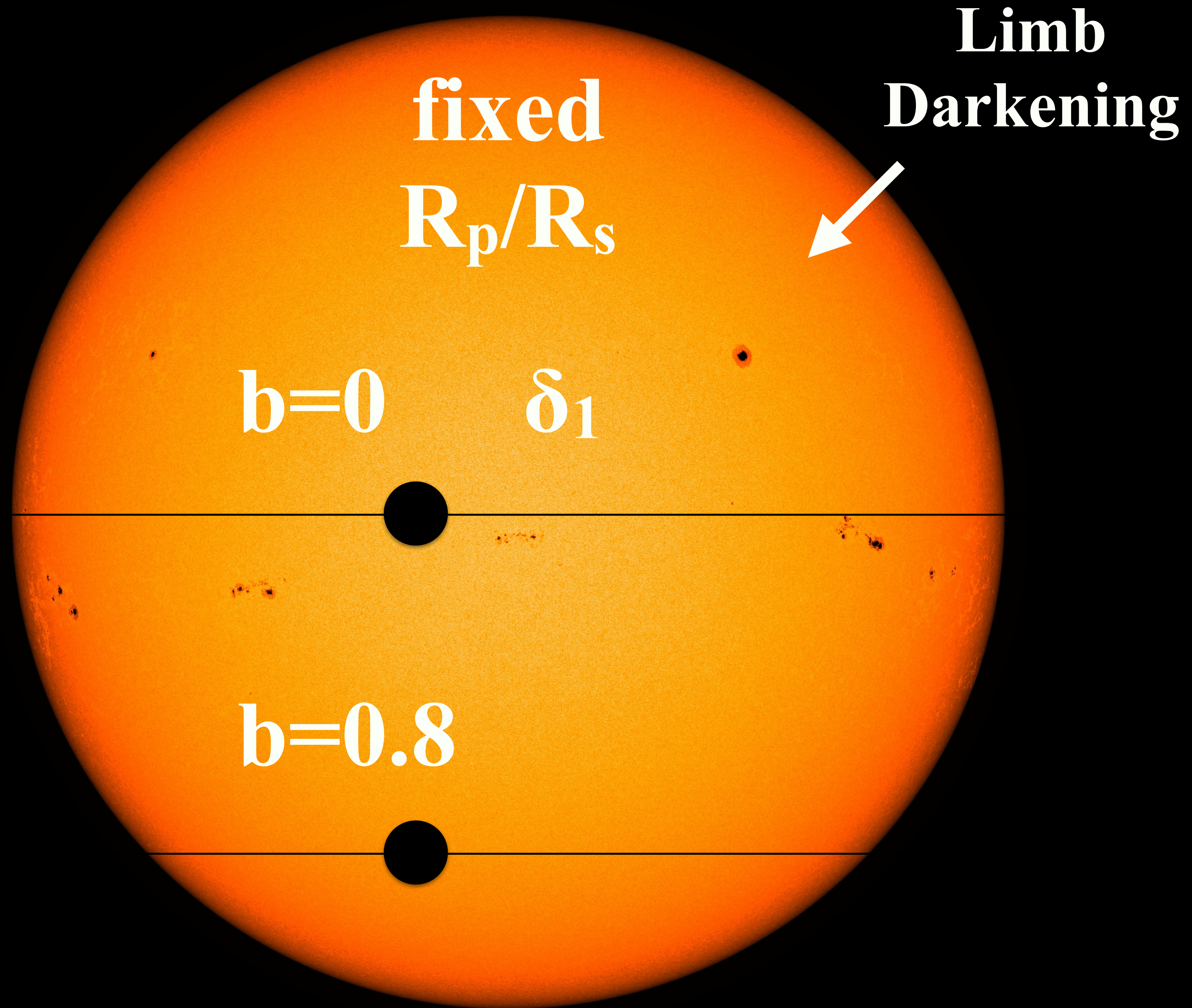


**$b=0$**

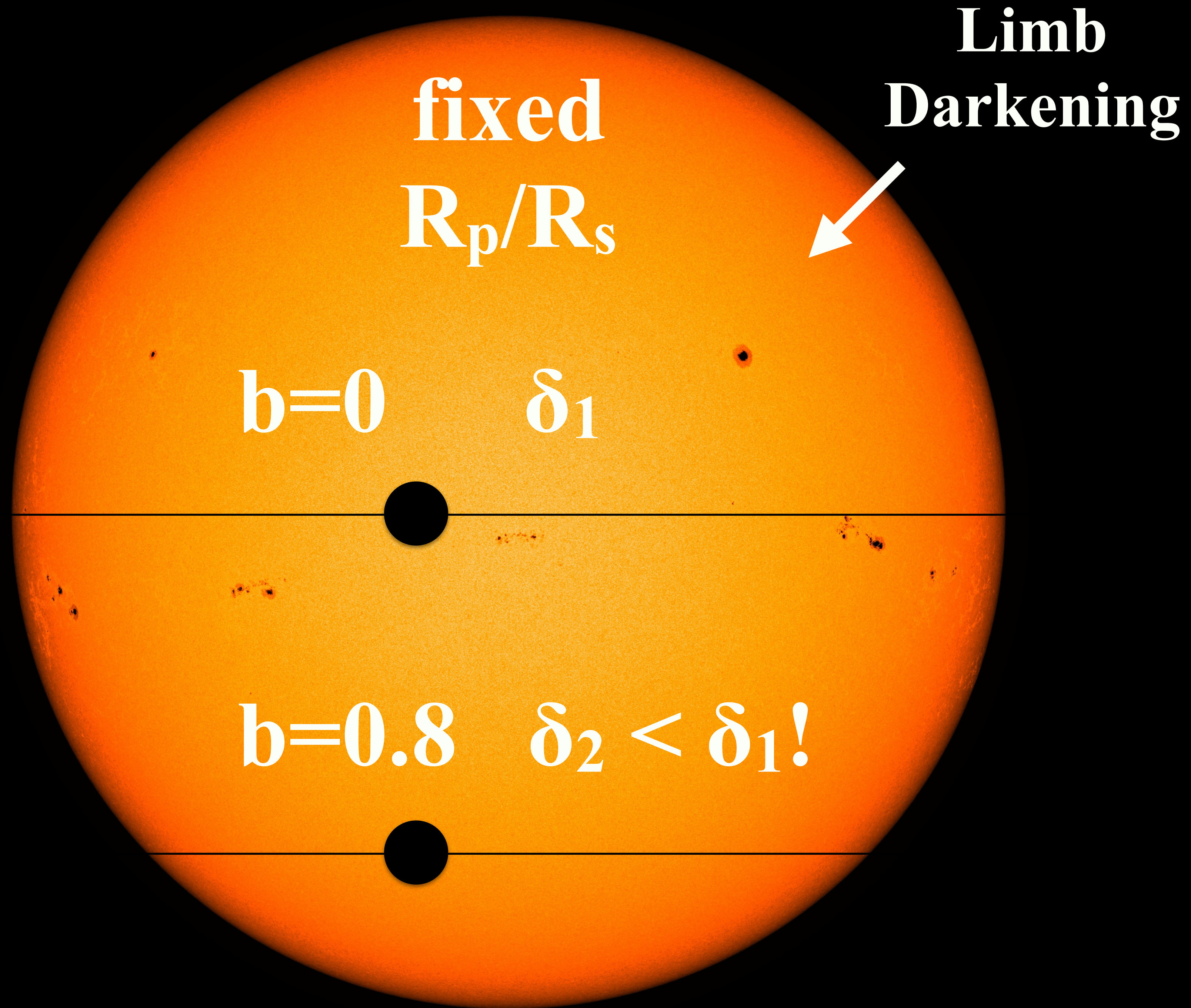
**$\delta_1$**





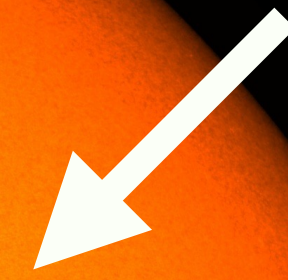






fixed  
 $R_p/R_s$

Limb  
Darkening



$b=0$

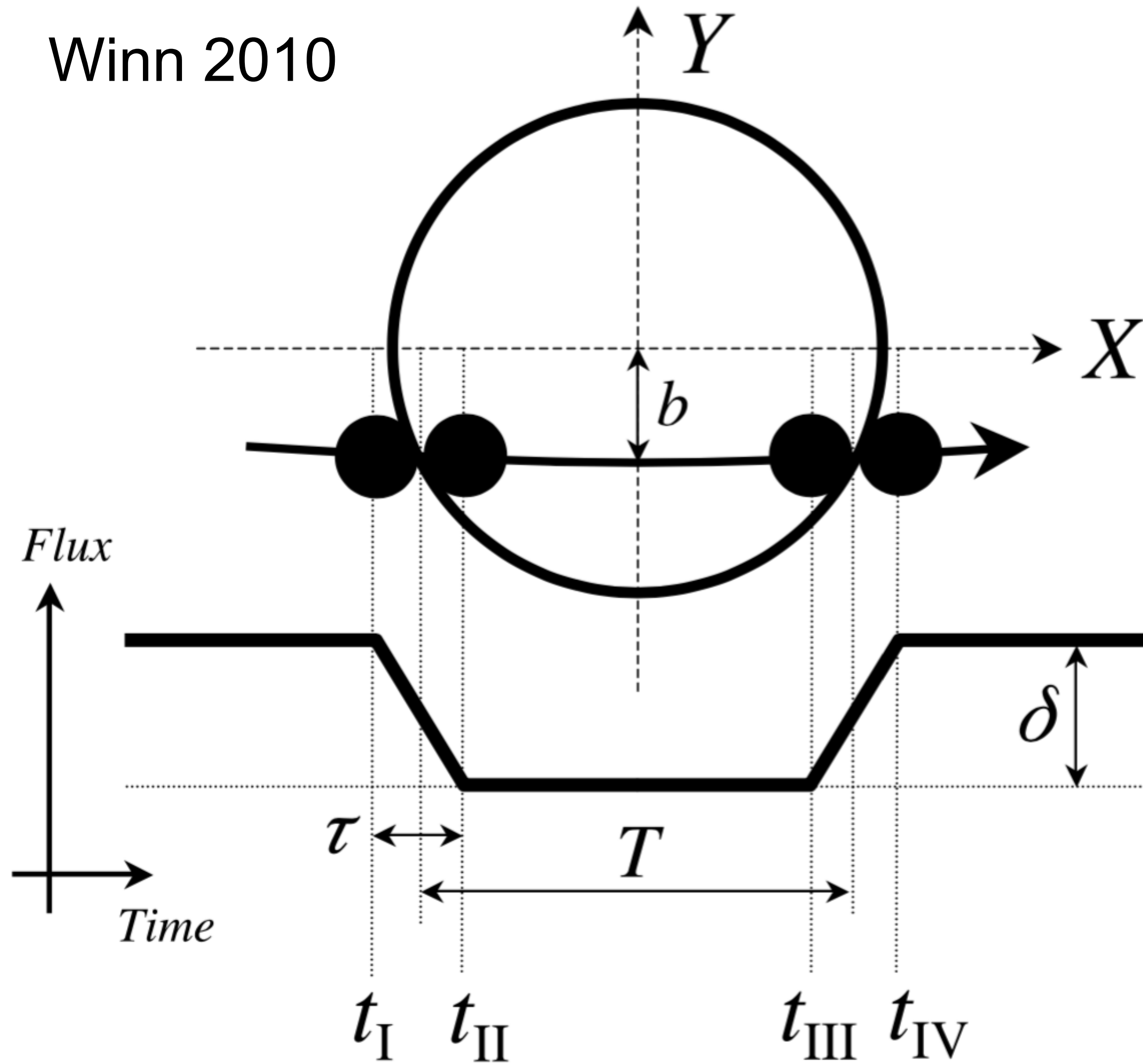
$\delta_1$

$b=0.8$

$\delta_2 < \delta_1!$



Winn 2010



for circular orbits and

$$R_p \ll R_\star \ll a:$$

(see Saeger & Mallen-Ornelas 2003 for a rigorous derivation)

$$T \approx T_0 \sqrt{1 - b^2},$$

$$T_0 \equiv \frac{R_\star P}{\pi a}$$

Can rewrite  $a/R_s$  using Kepler's 3rd law ...

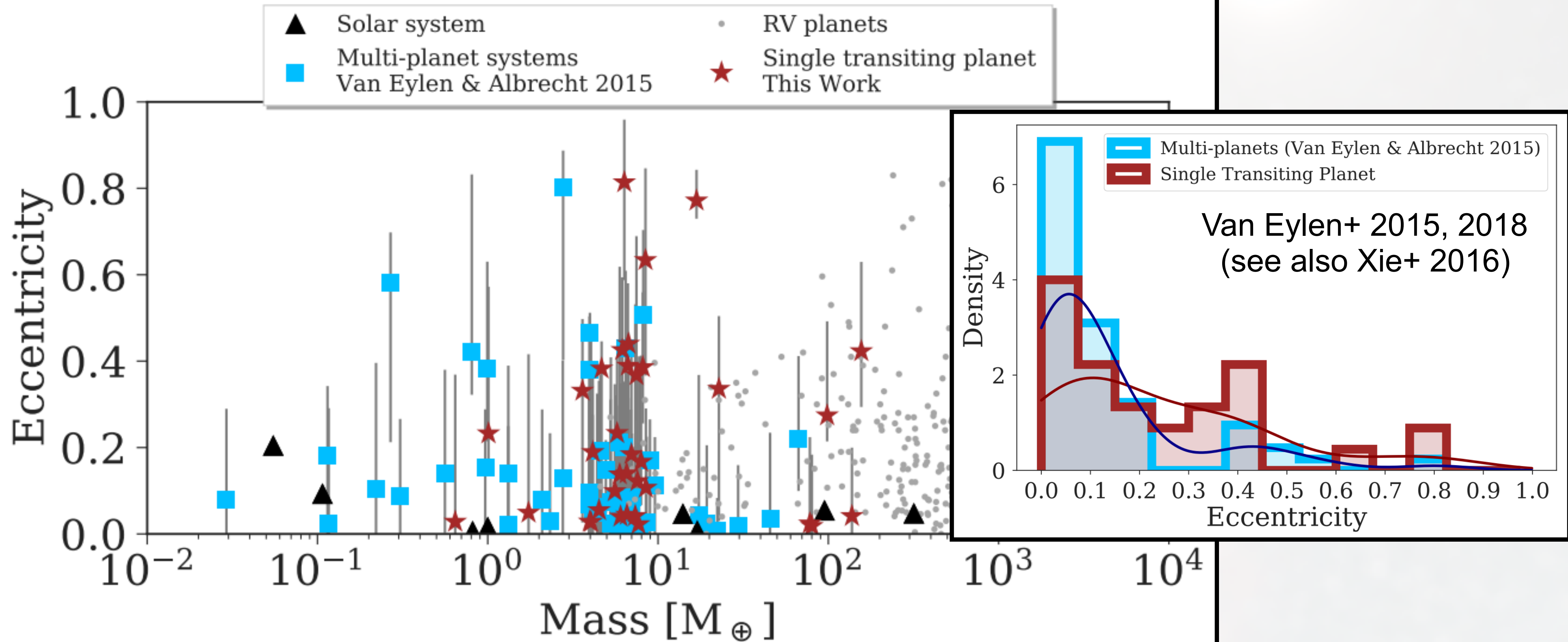


$$T_0 \equiv \frac{R_\star P}{\pi a}$$

$$\rho_{\star, \text{transit}} = \frac{3\pi}{GP^2} \left( \frac{a}{R_\star} \right)^3$$

*Big Result 1: Independent stellar parameters can be used to improve transit parameters!*

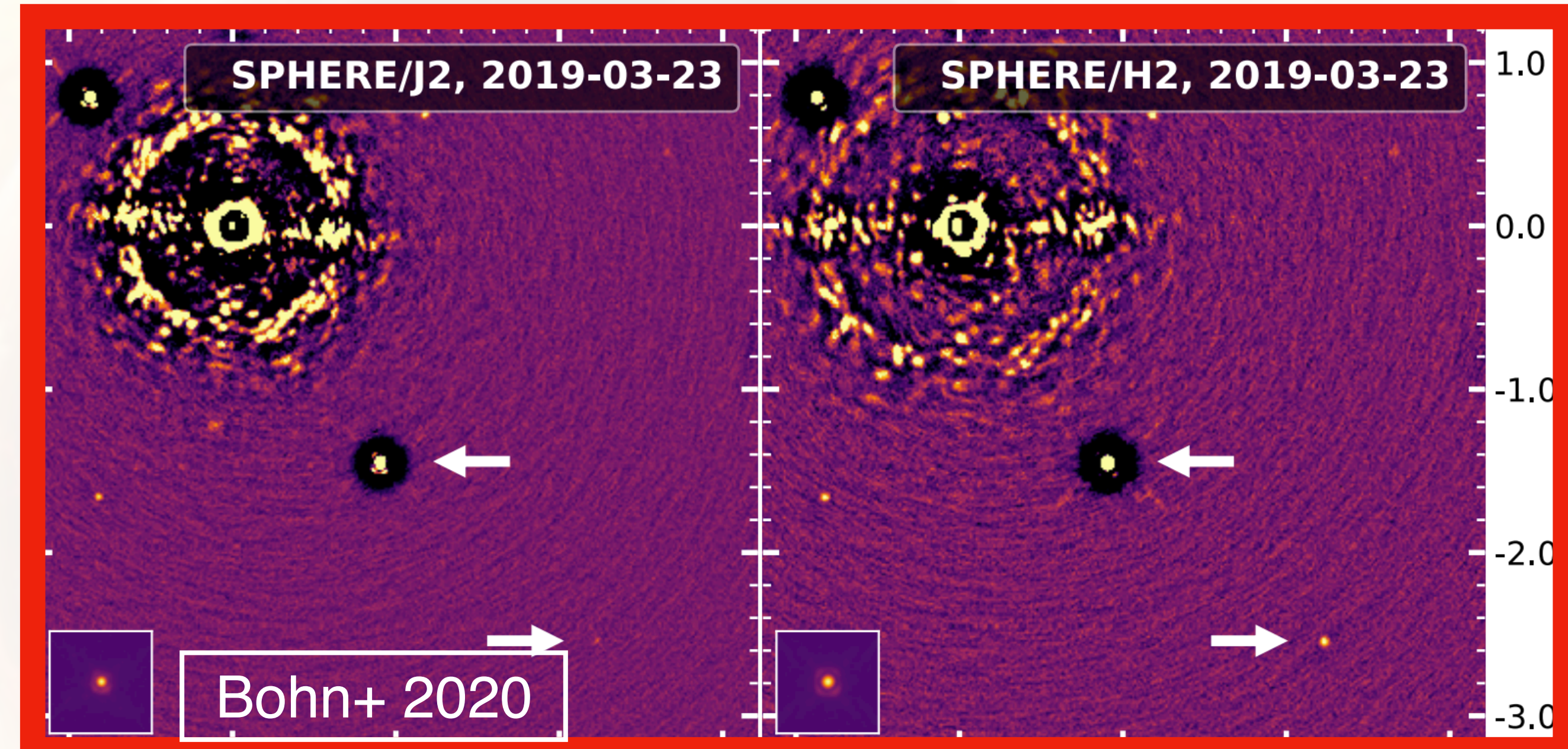
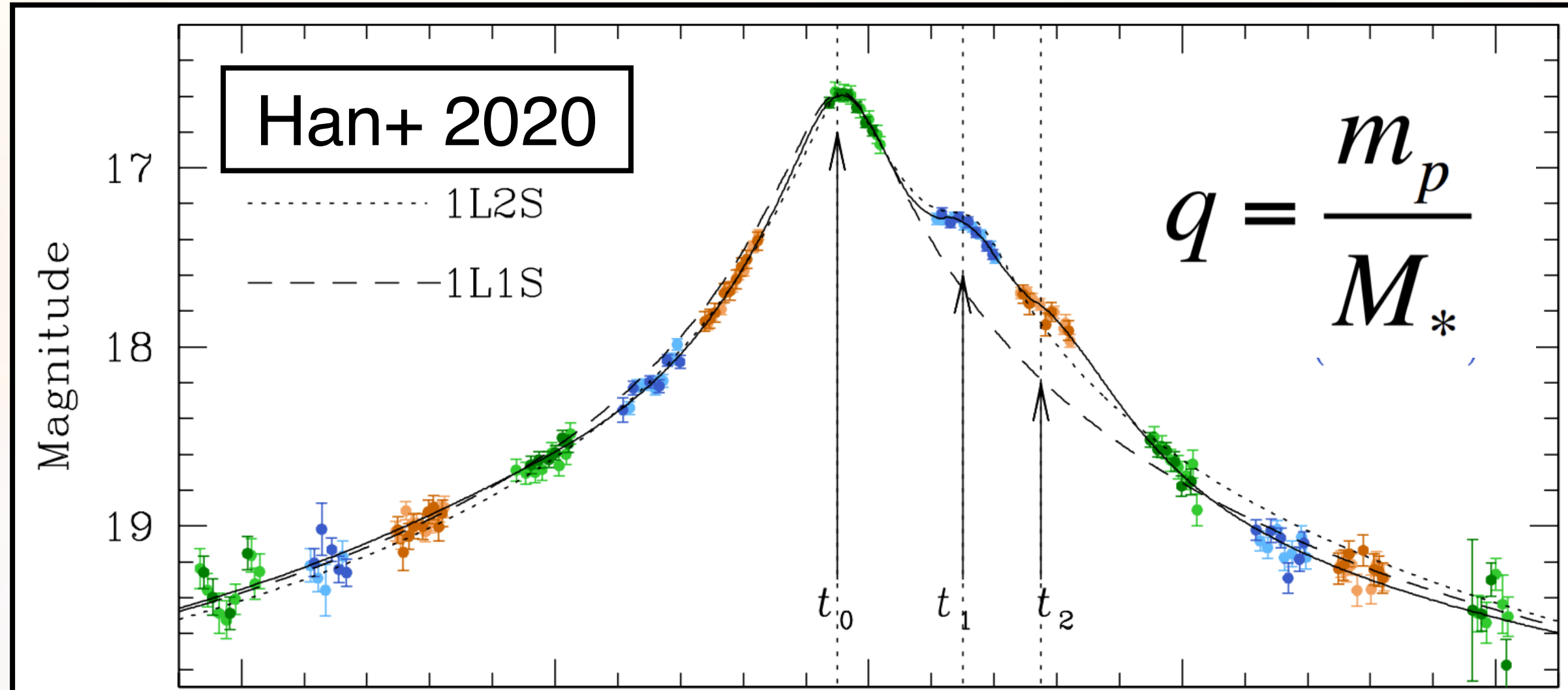
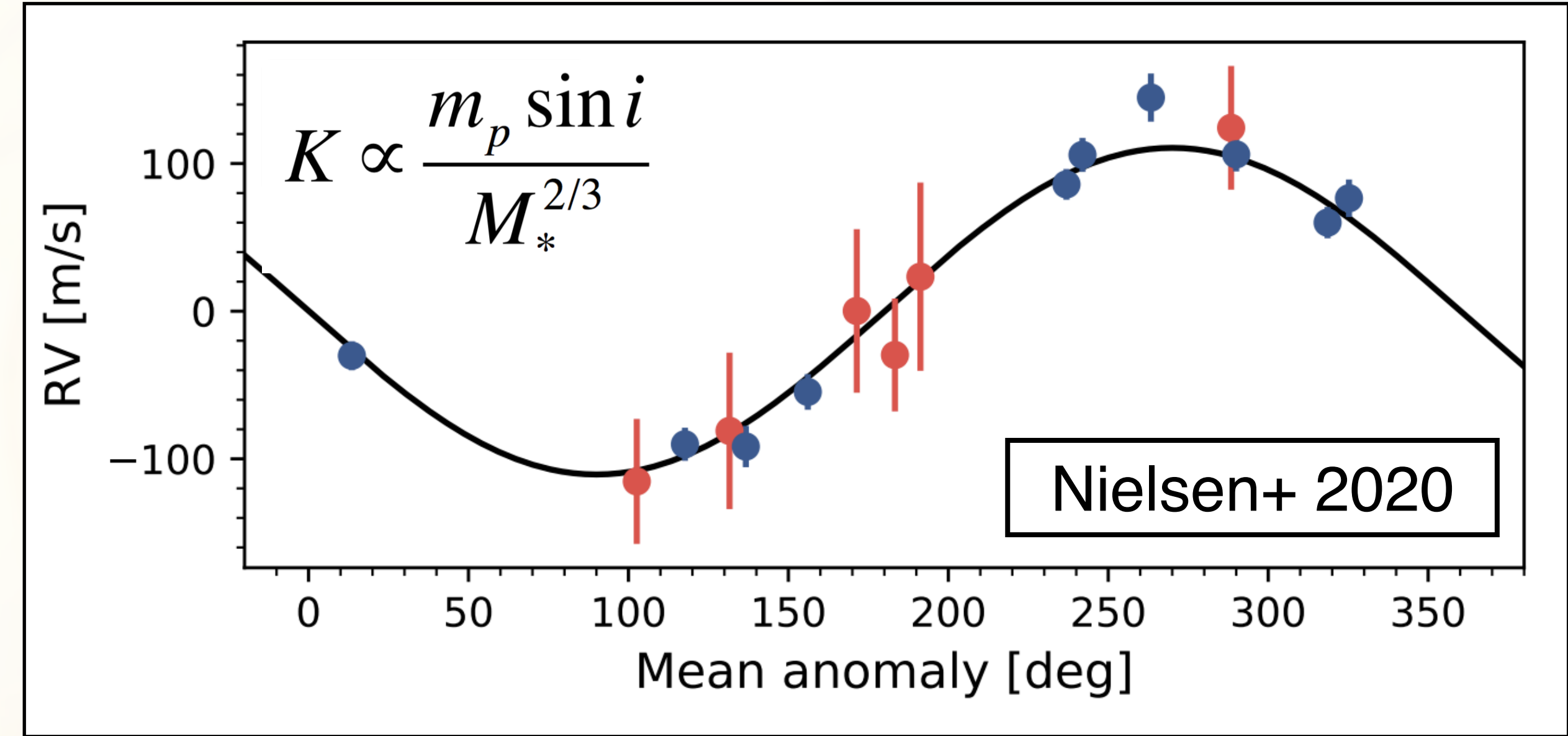
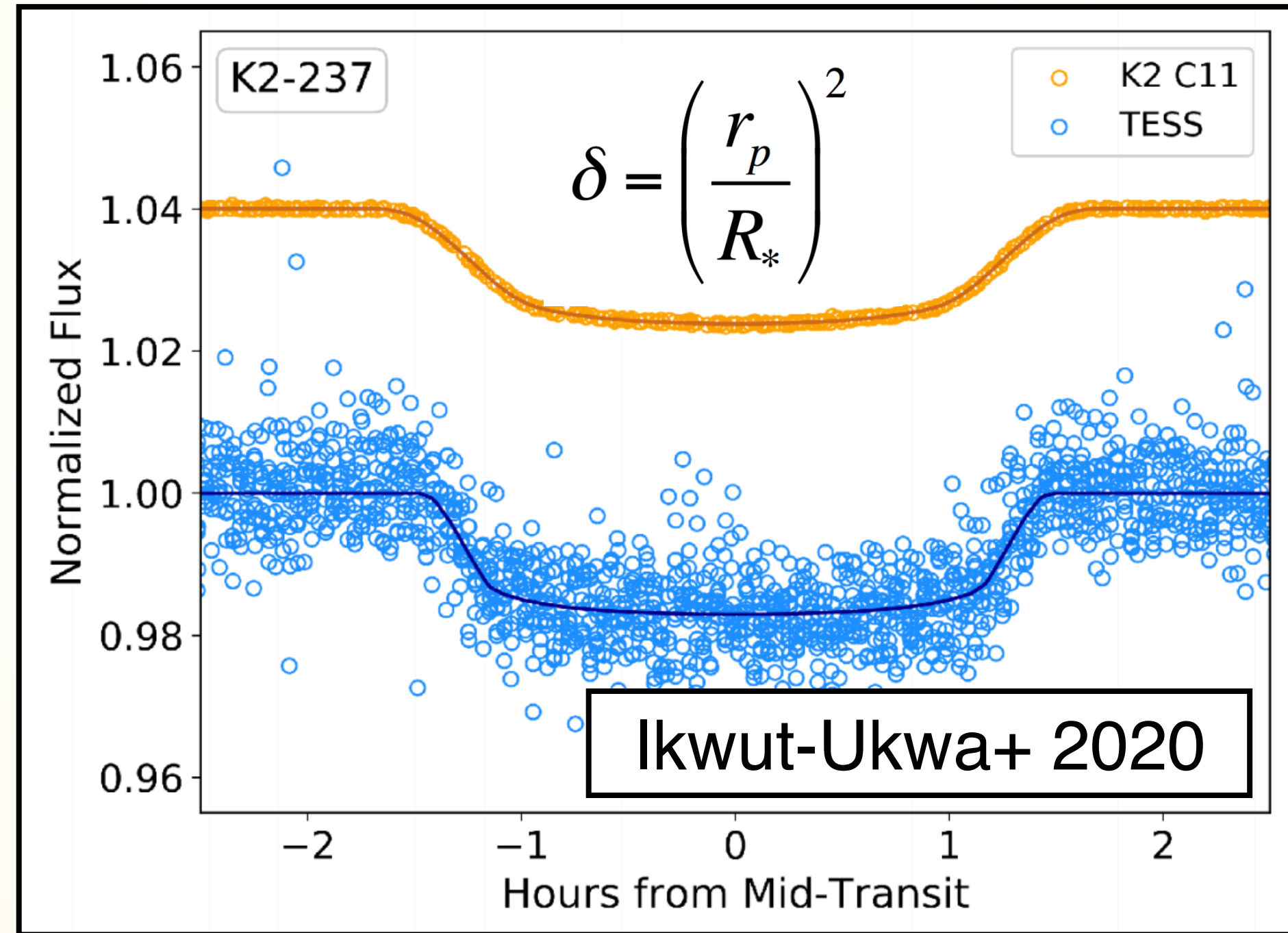
*Big Result 2: Transit observables can be used to measure stellar parameters*



Eccentricities from asteroseismic densities + transit durations. Gaia parallaxes ( $\rho \propto M/R^3$ !) should now allow this for many more systems

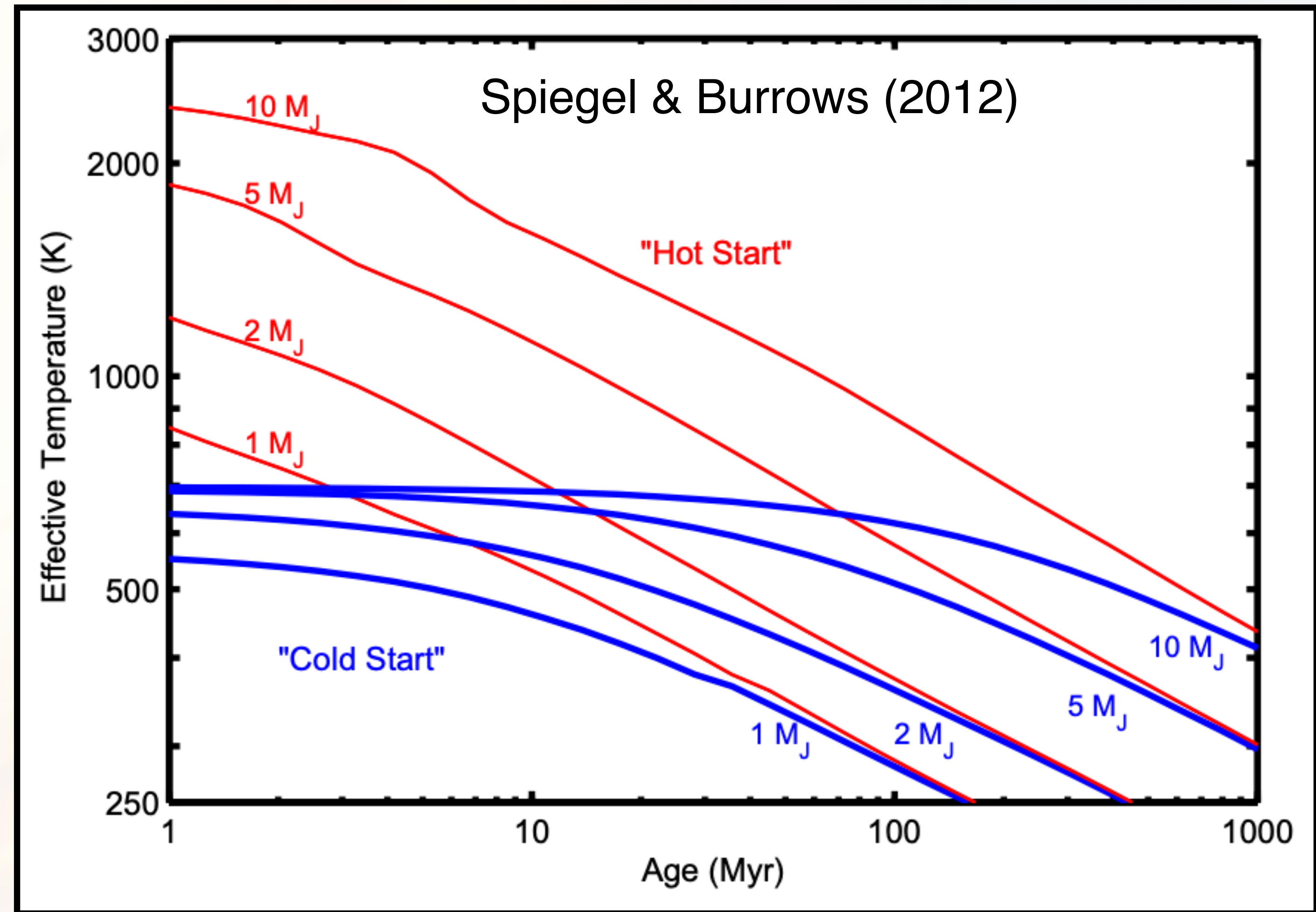
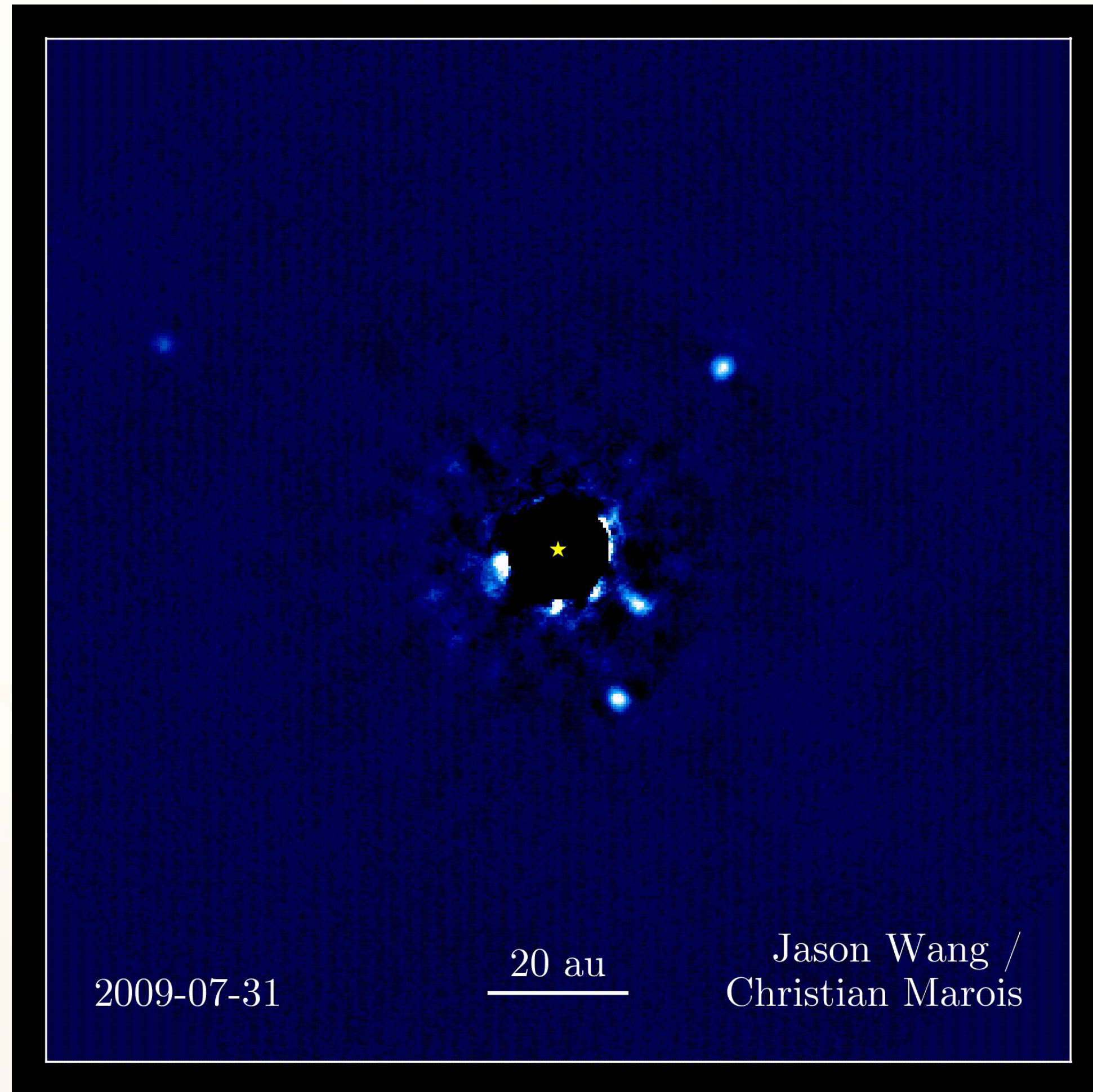


# "Know Thy Star, Know Thy Planet"





# Ages of Directly Imaged Planet Hosts



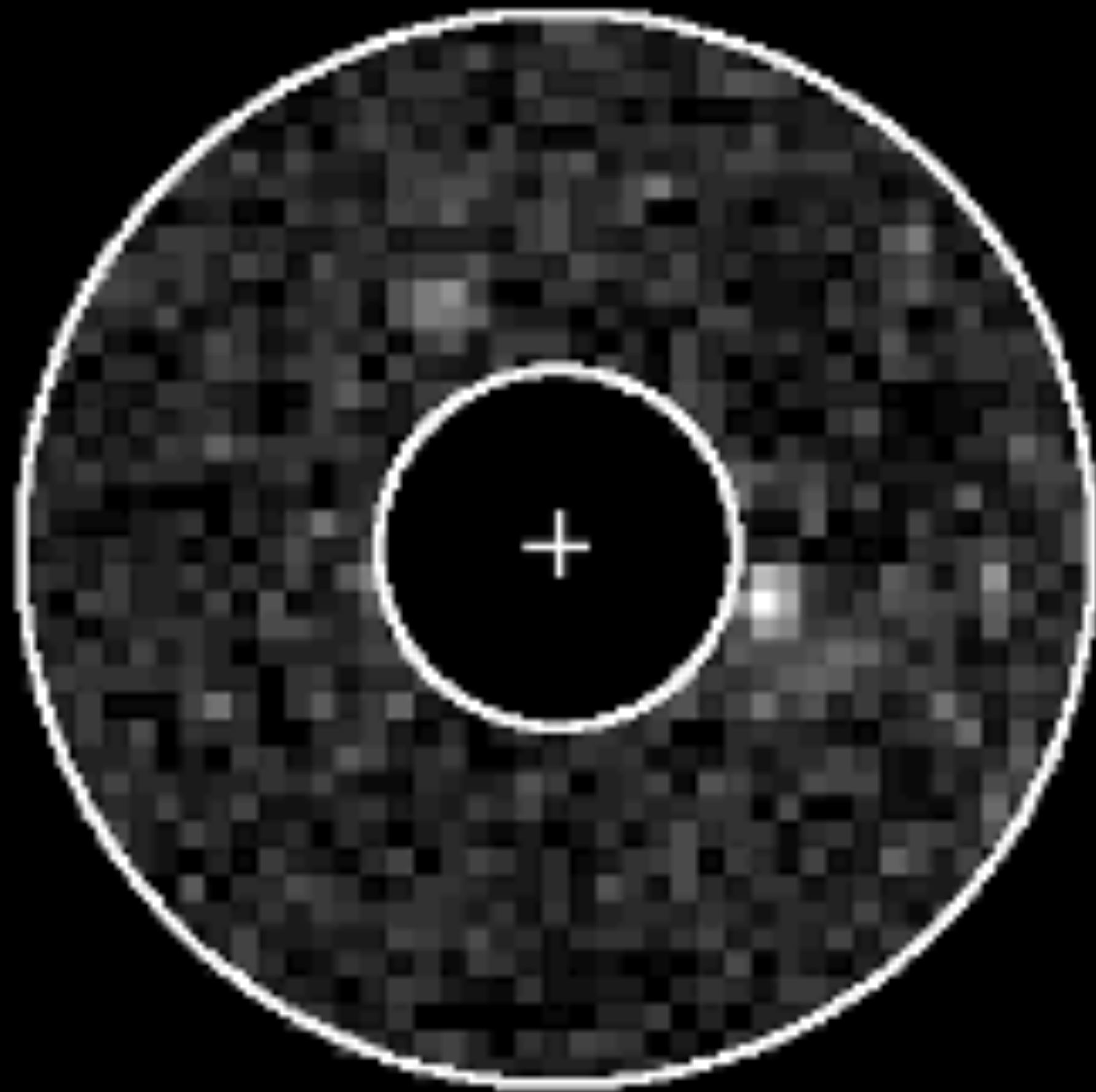
Ages are important for masses of young planets & to test formation models



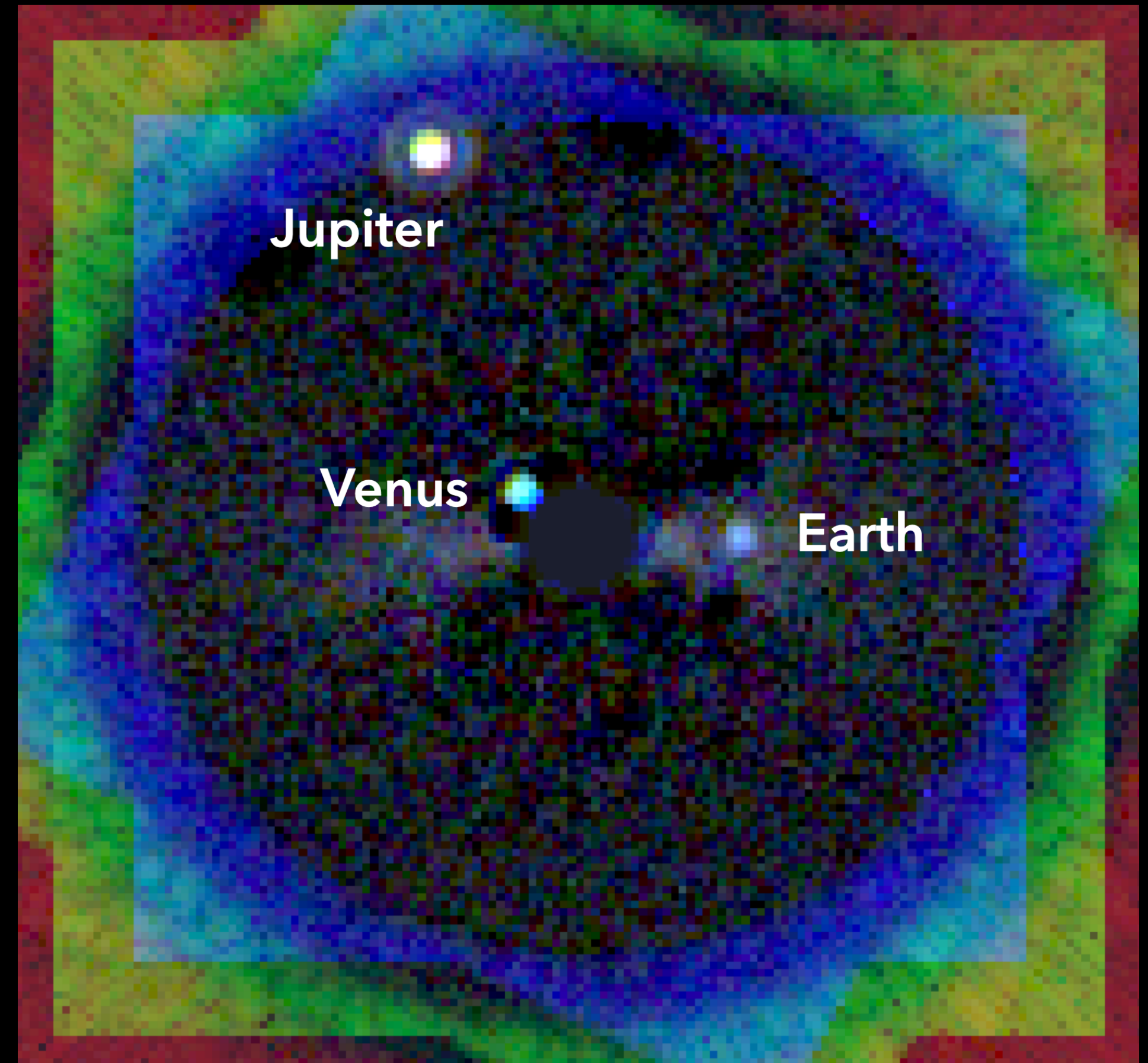
# Host Stars of Directly Imaged Earth-like Planets

Roman Coronagraph Instrument

6-m Class Astro2020 Flagship

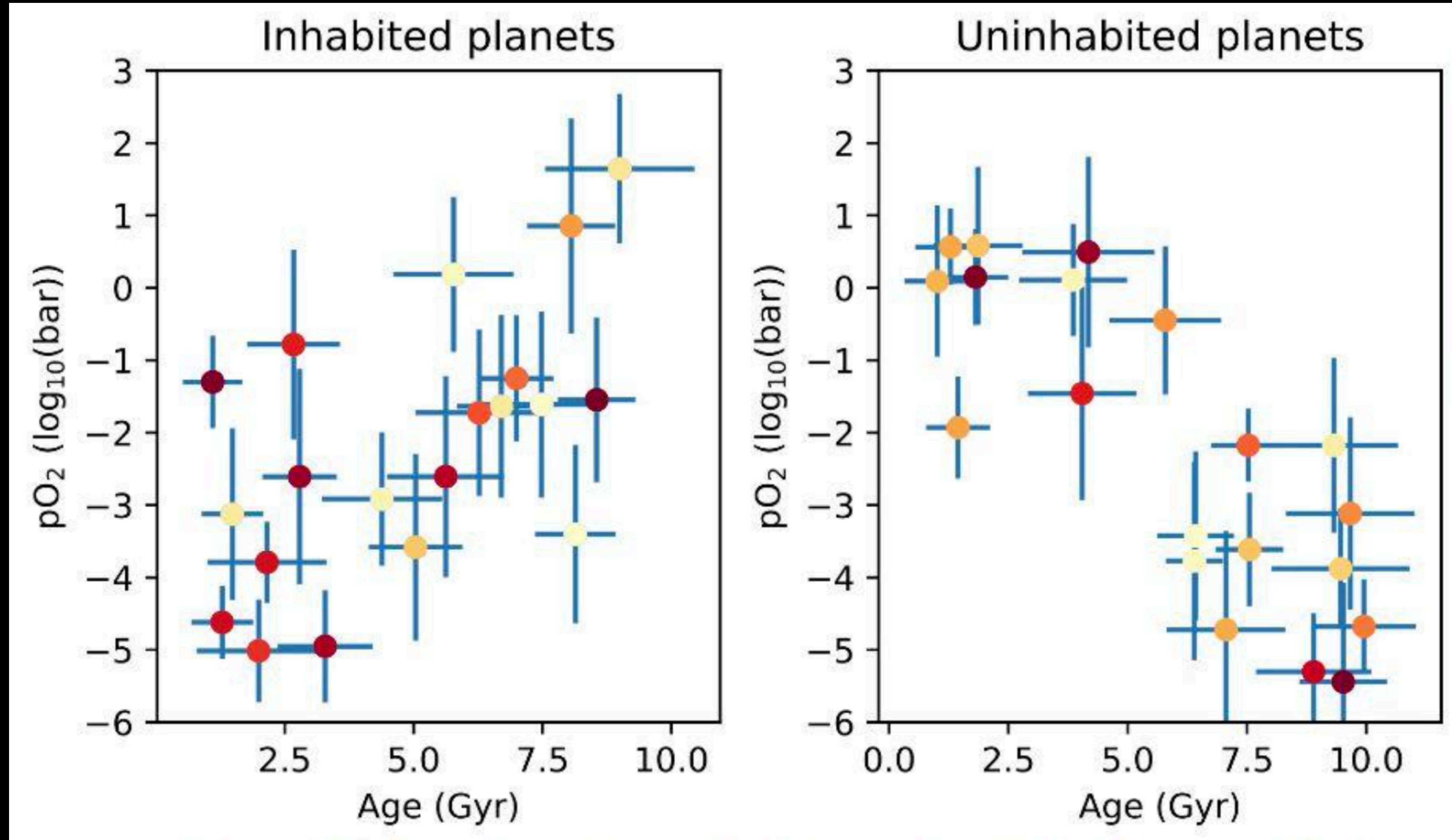


John Krist (NASA JPL)



Juanola Parramon, Zimmerman, Roberge (NASA GSFC)





Krissansen-Totton, Huber, MacGregor & O'Rourke (see also Bixel & Apai 2021)

*Ages of nearby bright stars may be critical for interpreting biosignatures on (future) directly imaged exoplanets*



# Summary

- **Astrometry from Gaia has revolutionized our ability to derive fundamental properties of stars:** Luminosities and radii to  $<\sim 5\%$ (!) are now routinely possible.  $F_{\text{bol}}$  and  $T_{\text{eff}}$  are the new bottlenecks!
- **Masses and ages of stars remain challenging:** Binaries from Gaia will be critical to calibrate models that are required for most field stars
- **Stellar properties are important for virtually all fields of exoplanet science,** ranging from improving transit fits to interpreting biosignatures in (future) directly imaged planets. Much more on this tomorrow!

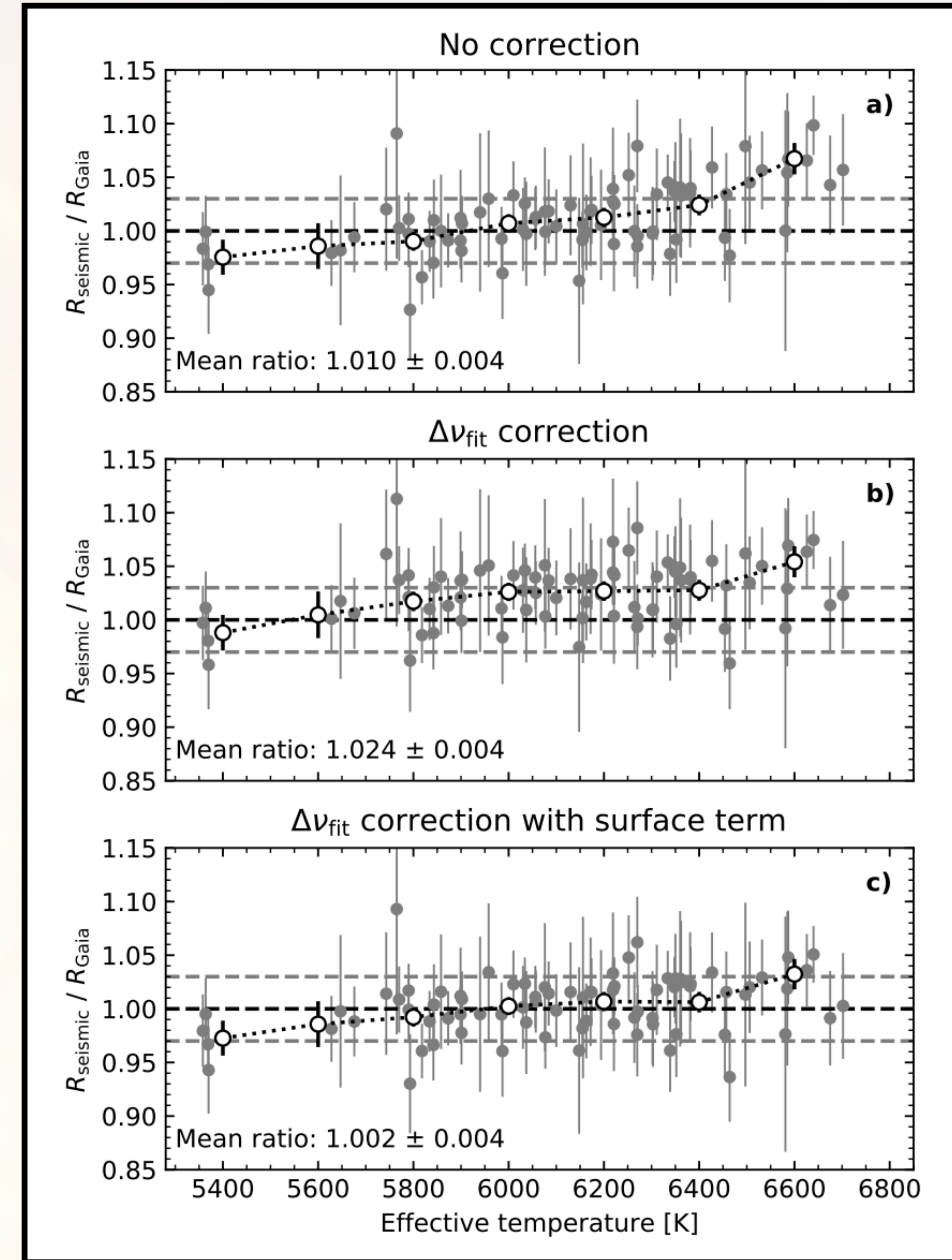
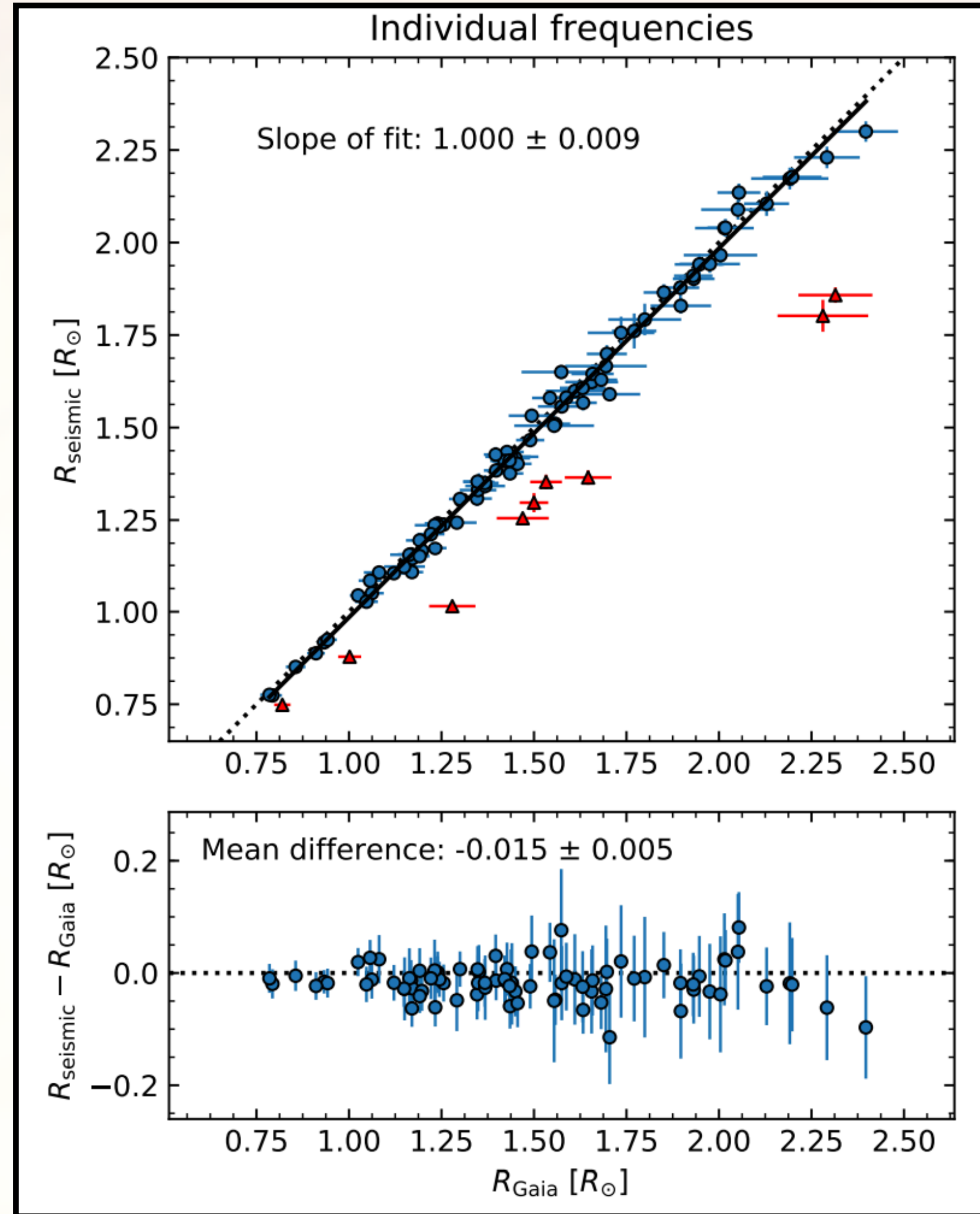
*... and a big thank you to the Gaia team for these amazing astrometric datasets!*



# *Extra Slides*

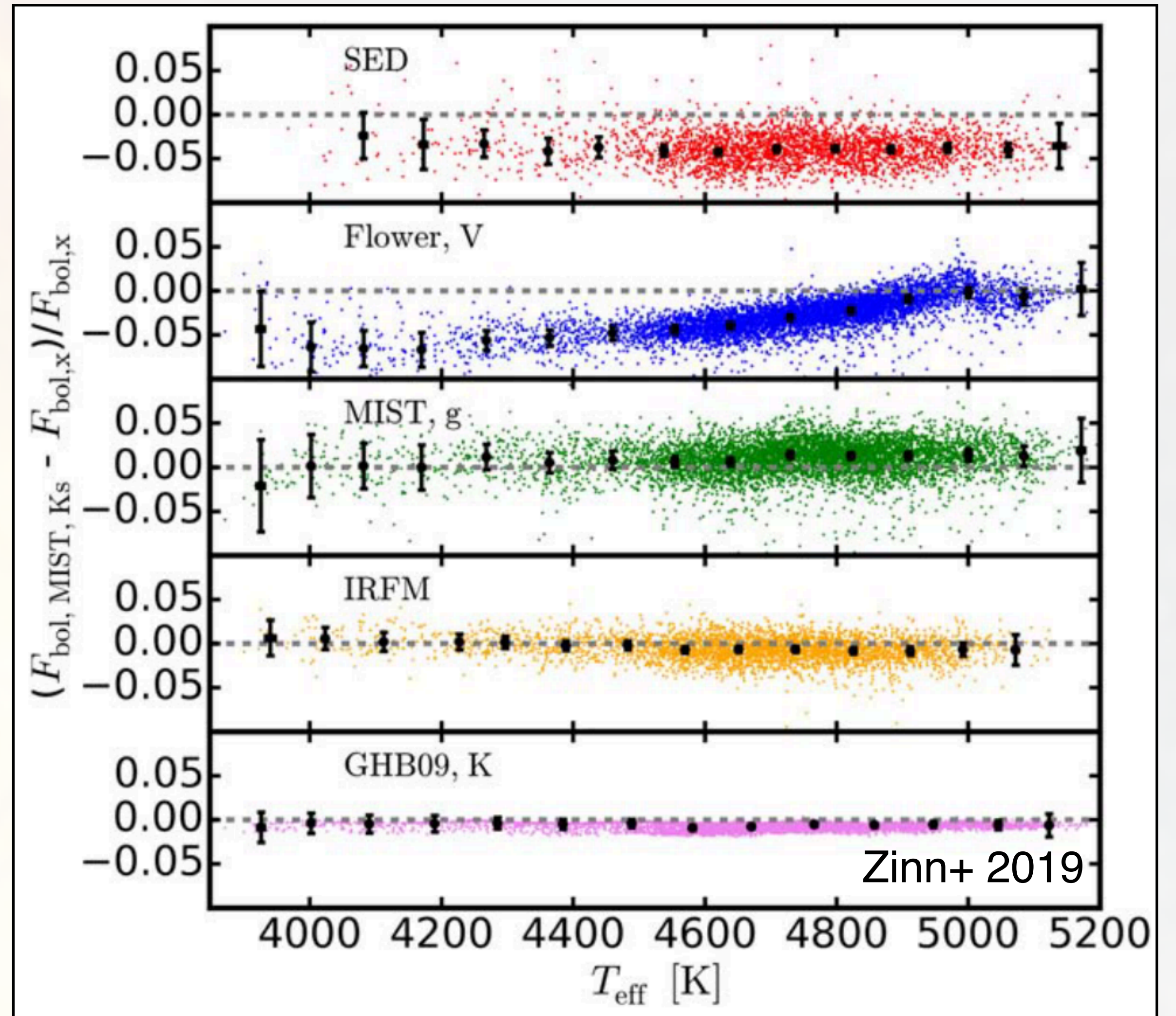
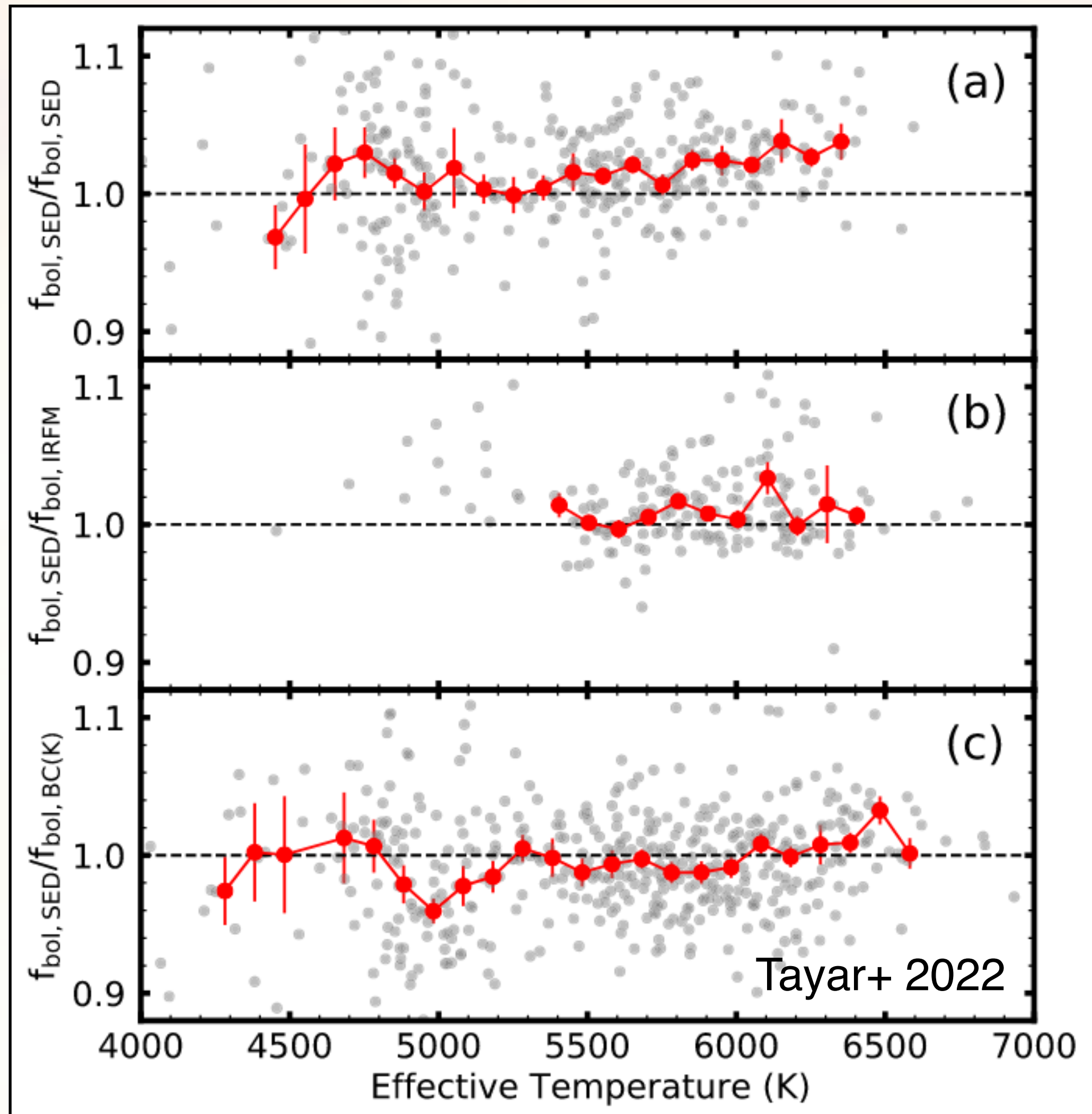


# Asteroseismology versus Gaia





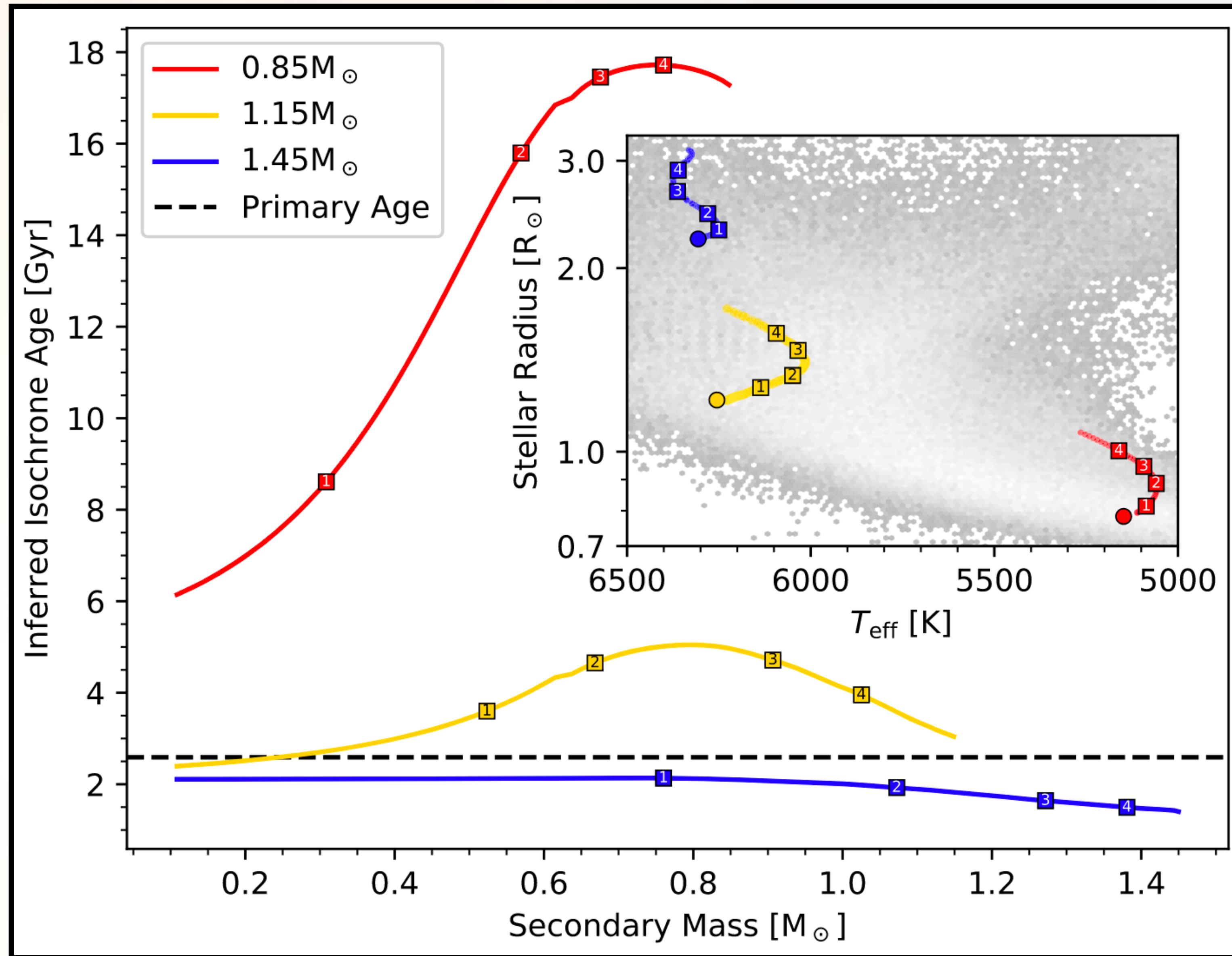
# Bolometric Fluxes: Systematic Errors



~2-4% offsets not uncommon. Can dominate the error budget on  $L \propto f_{\text{bol}} d^2$ !



# Effects of Unresolved Binaries

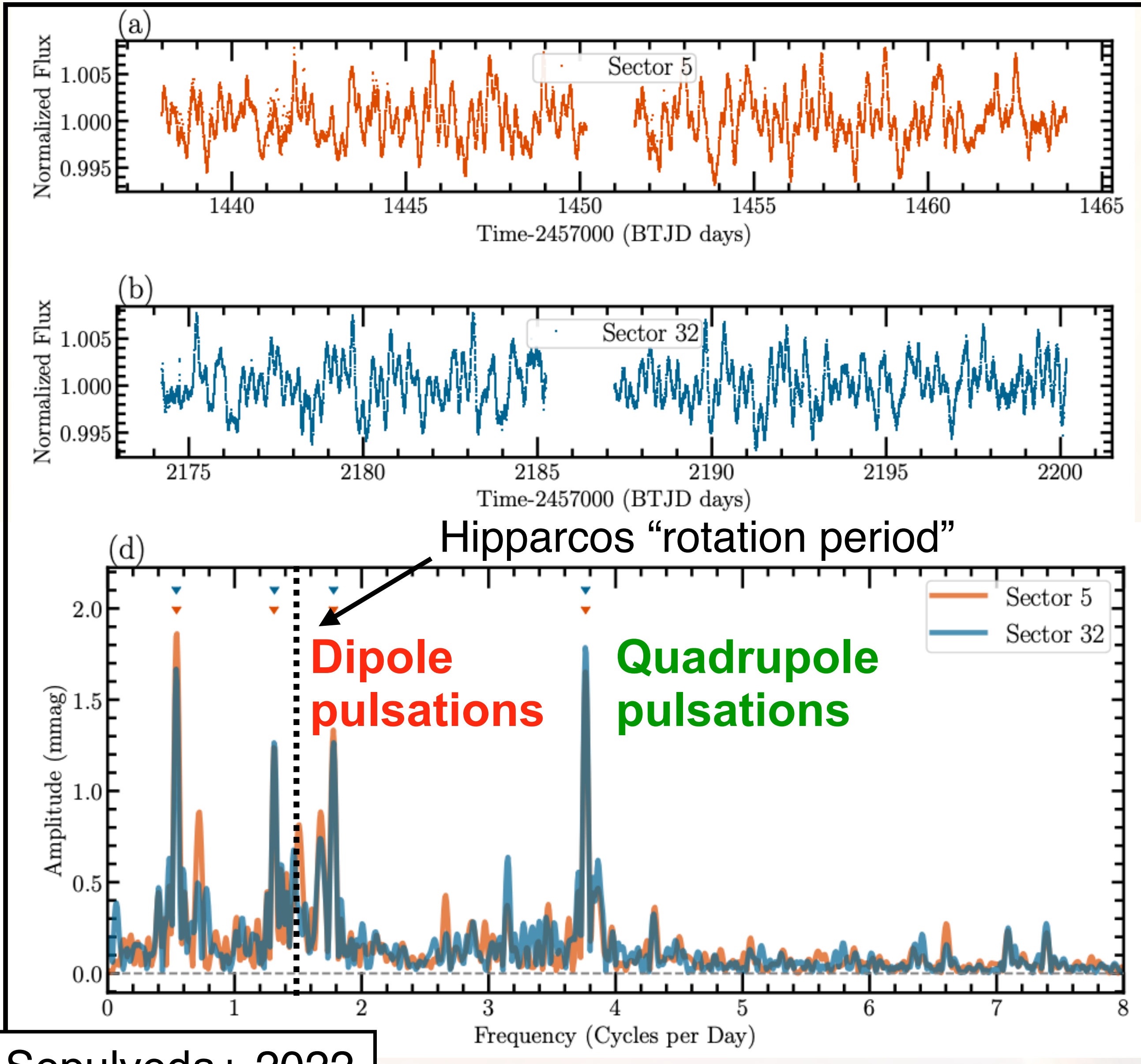
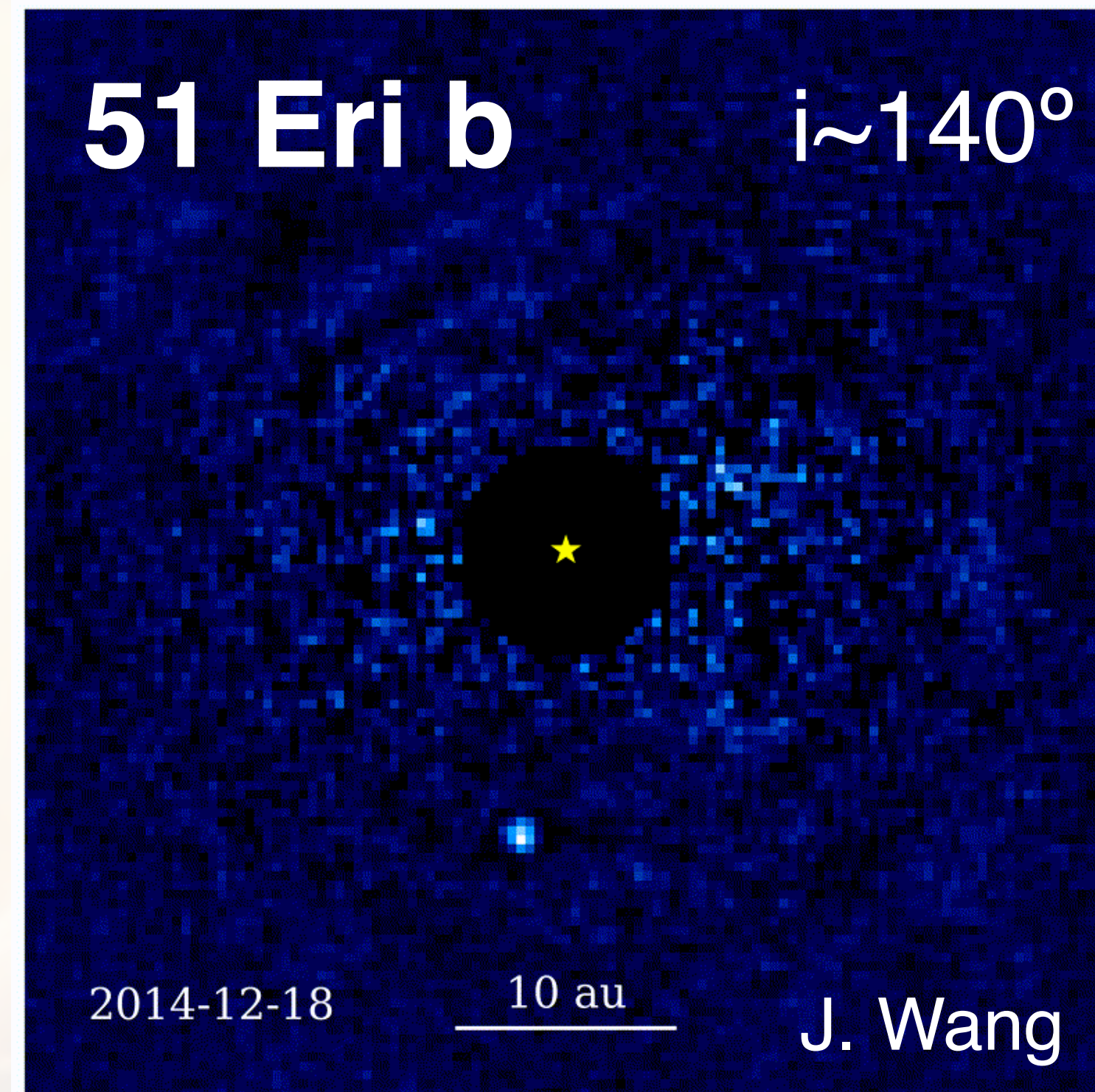




# Architectures of Imaged Planets



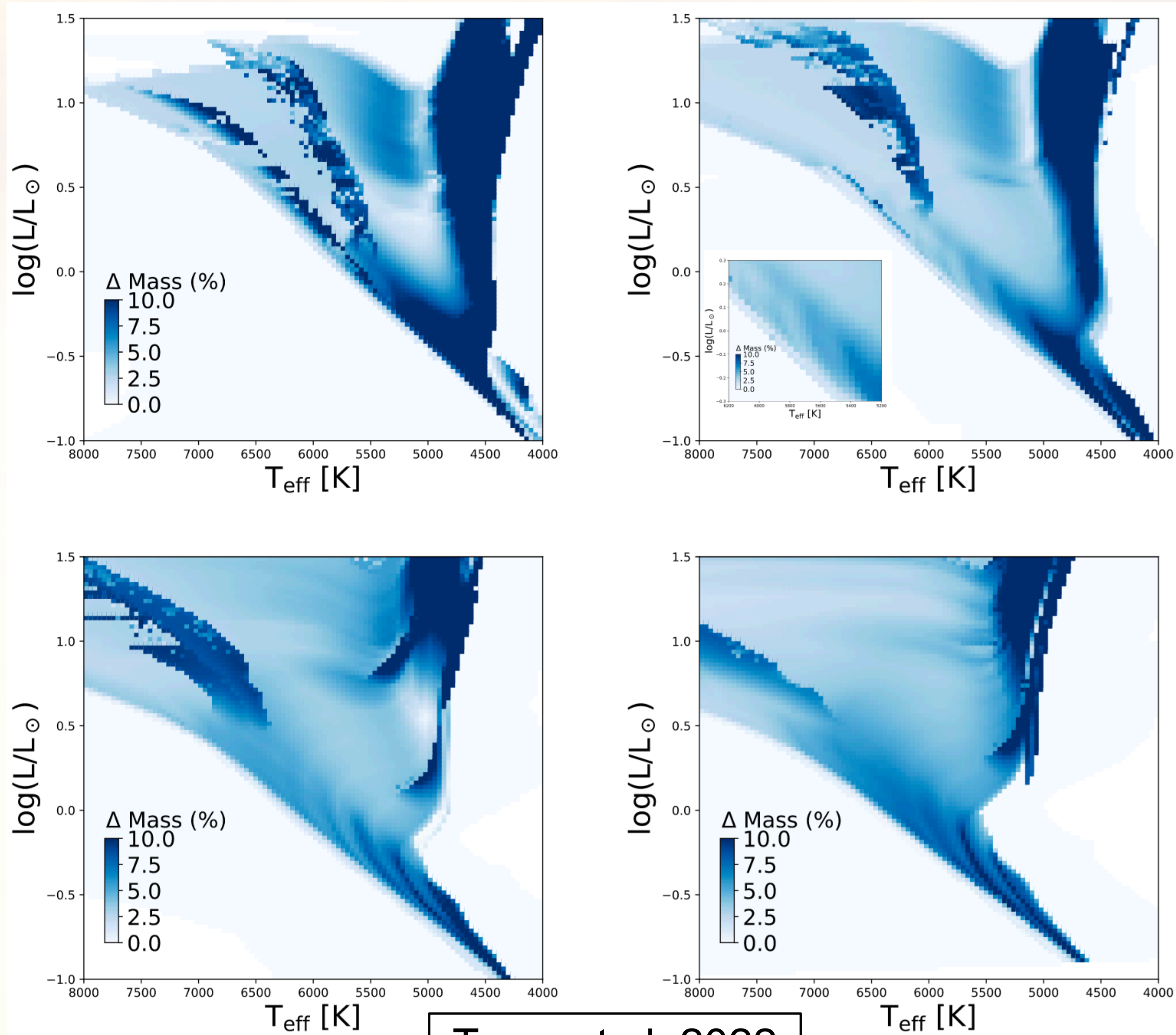
Aldo Sepulveda



Asteroseismic rotation period constrains line-of-sight inclination to  $i \sim 60^\circ$  ( $i \sim 120^\circ$ ). Consistent with planetary orbit alignment?



# Caveat: Stellar models have systematic errors



Tayar et al. 2022

## Source of systematics:

uncertain input physics such as convection, atmospheric boundary conditions, rotation, opacities and overshoot

Sets **error floor of ~5% in mass and ~20% in age** for solar-type stars, with variation across HRD

Always a good idea to establish systematic errors by using **different model grids!**