

Transit Timing Variations: Validation & Characterization

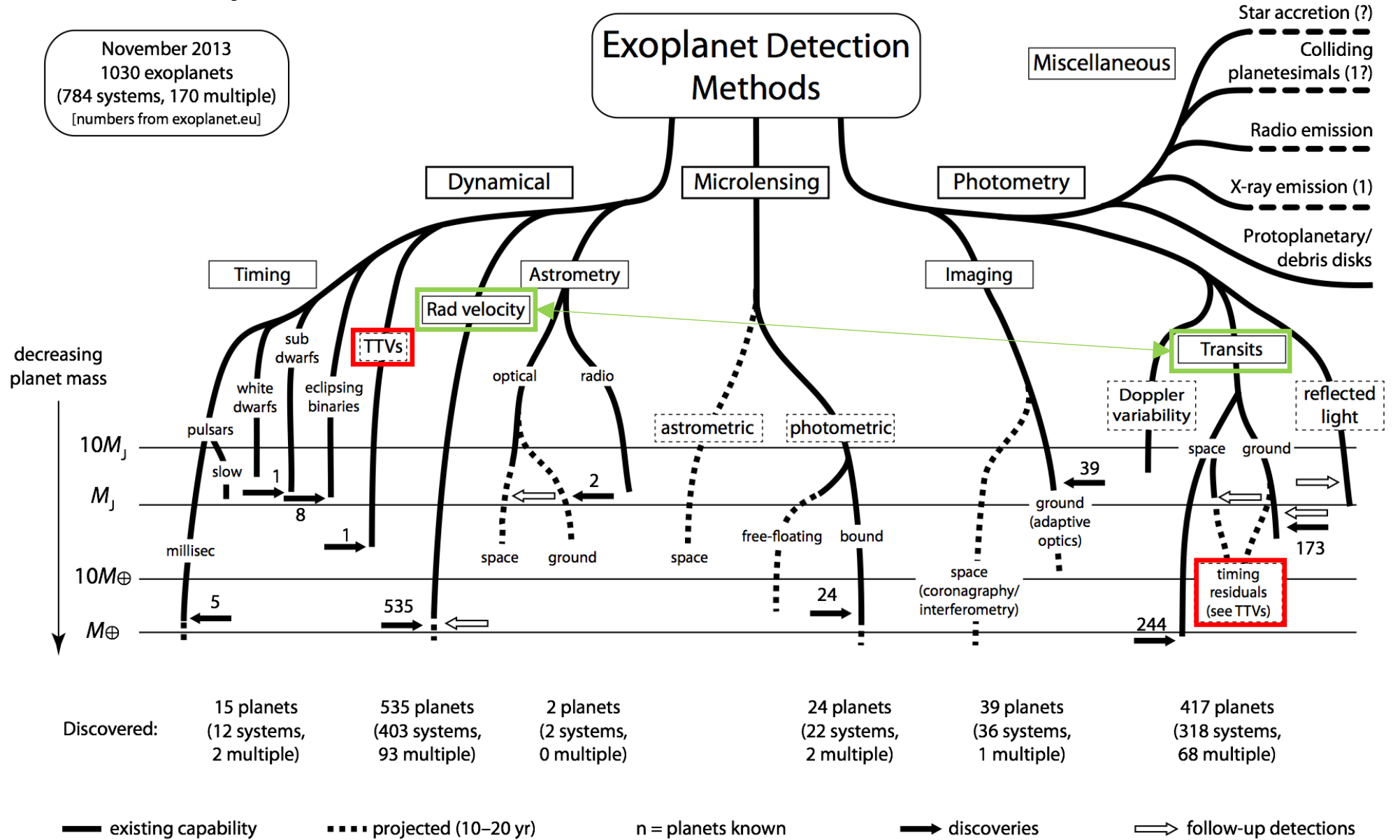


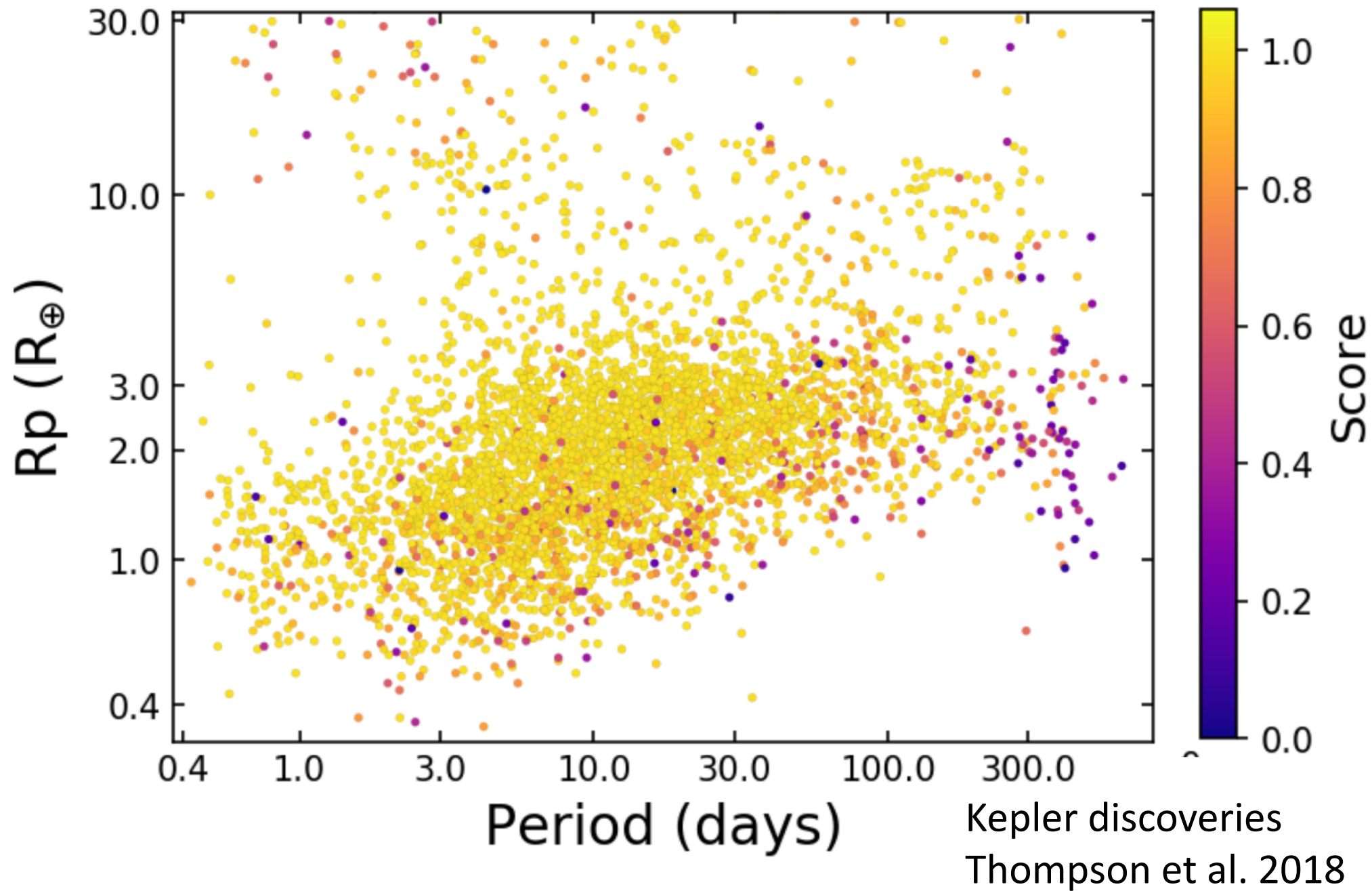
Daniel Fabrycky
University of Chicago

Detlev Van
Ravenswaay
Science Photo Library

Perryman 2013

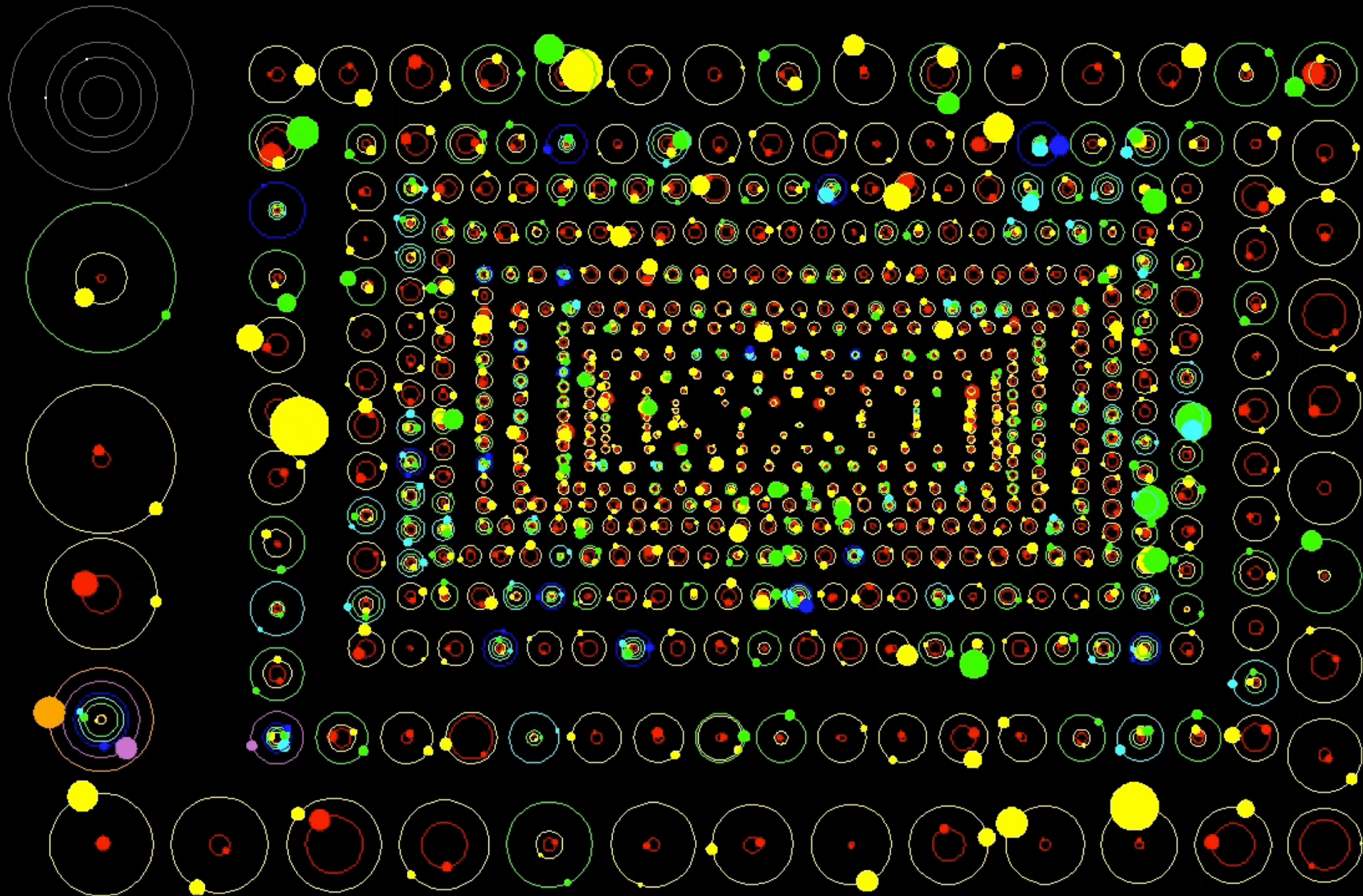
arXiv:1311.2521v1 [astro-ph.EP] 8 Nov 2013



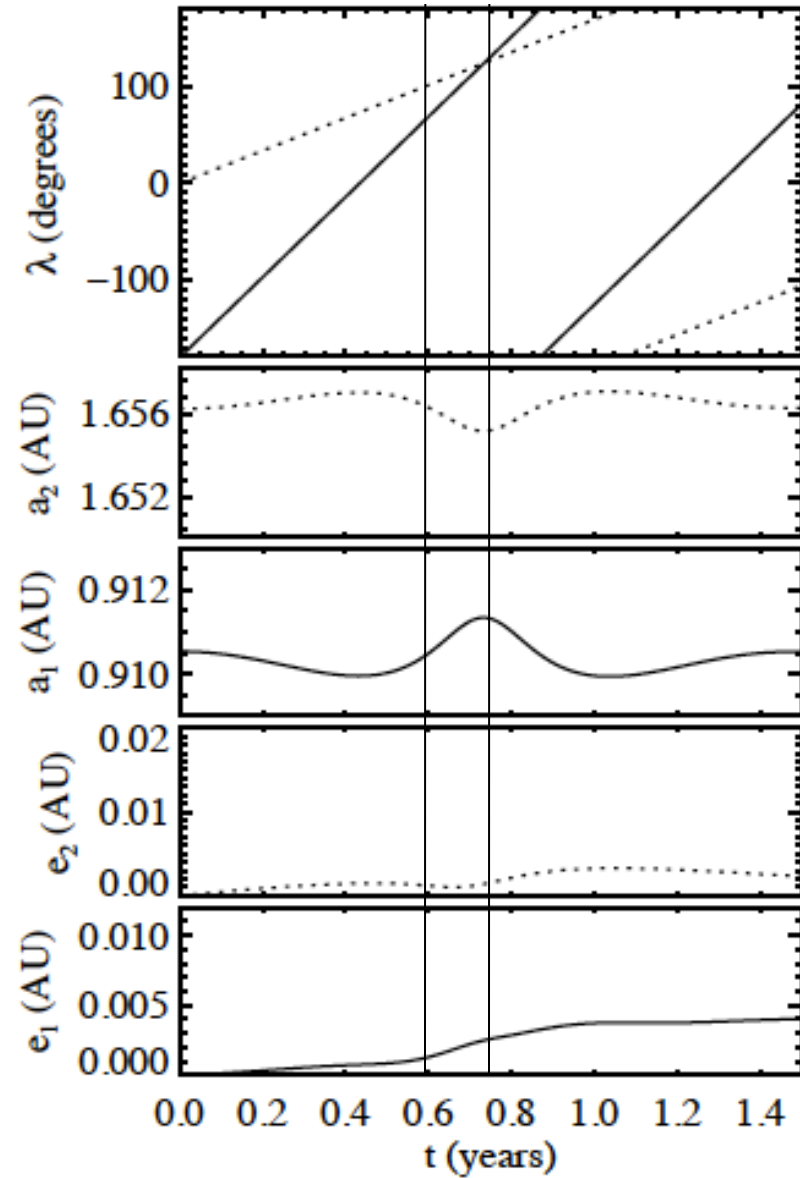
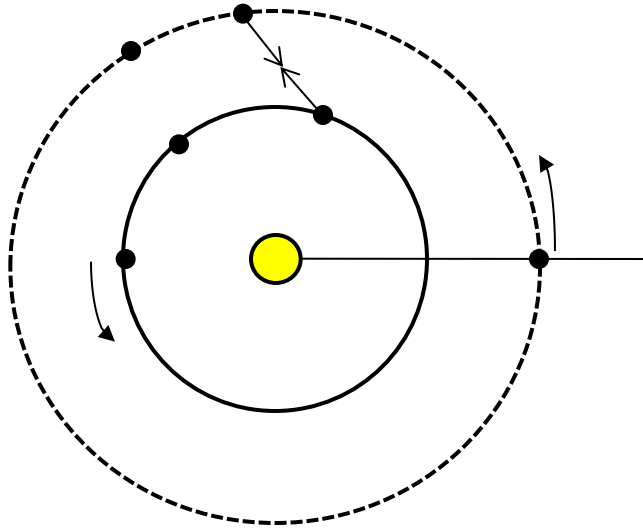


The Kepler Orrery III

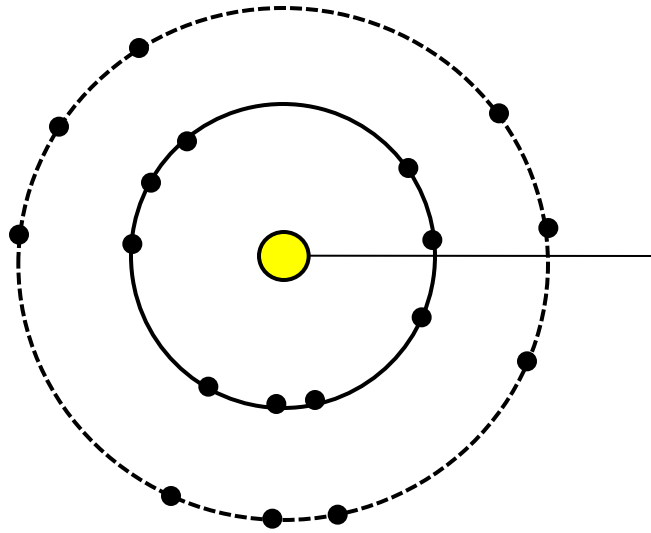
$t[\text{BJD}] = 2455215$



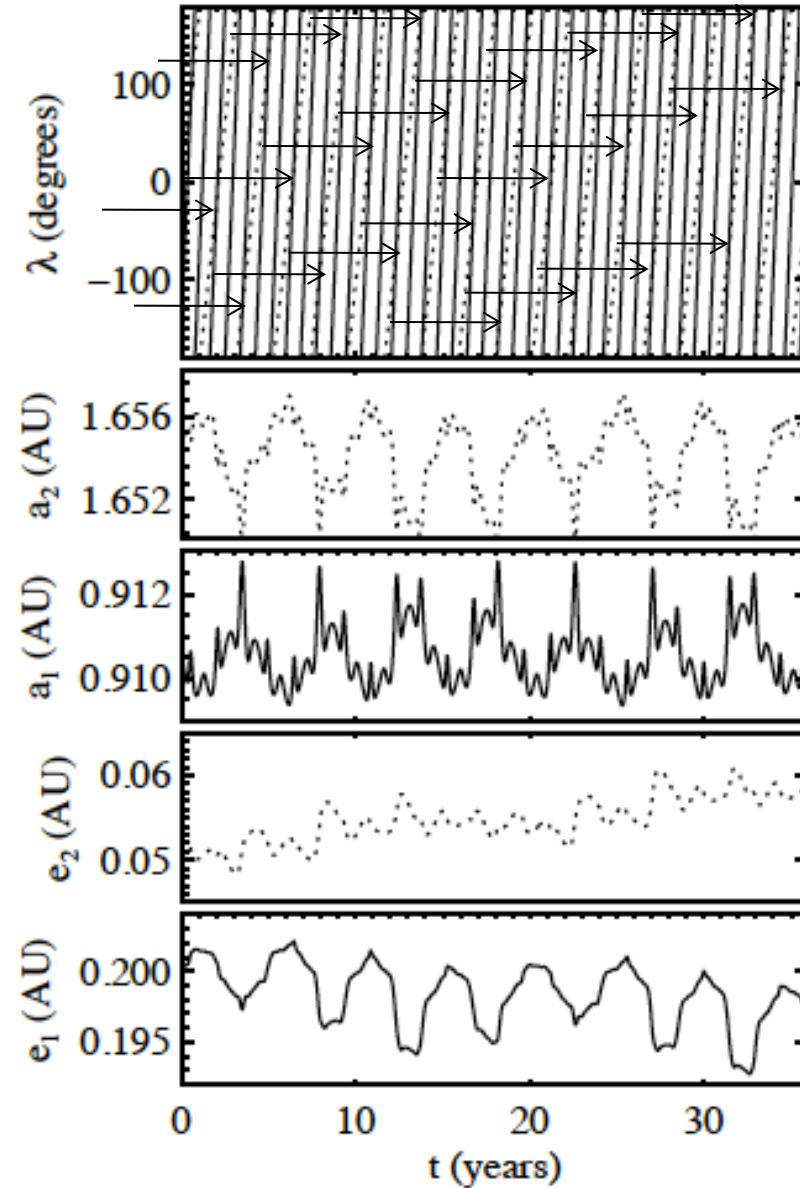
Dynamics: Orbital Timescales



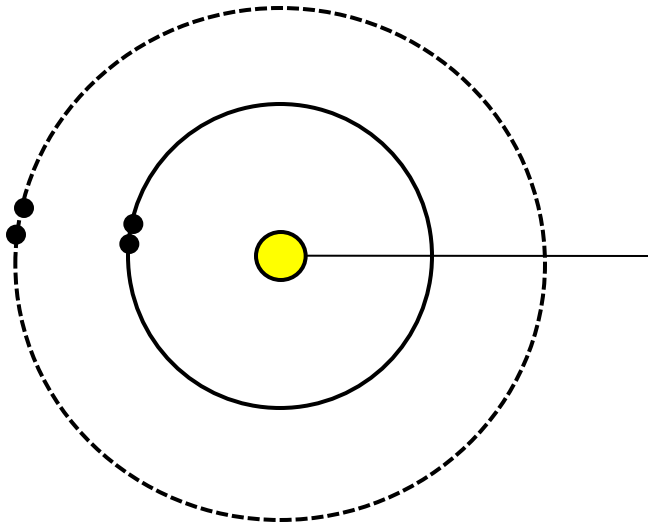
Dynamics: Secular Timescales



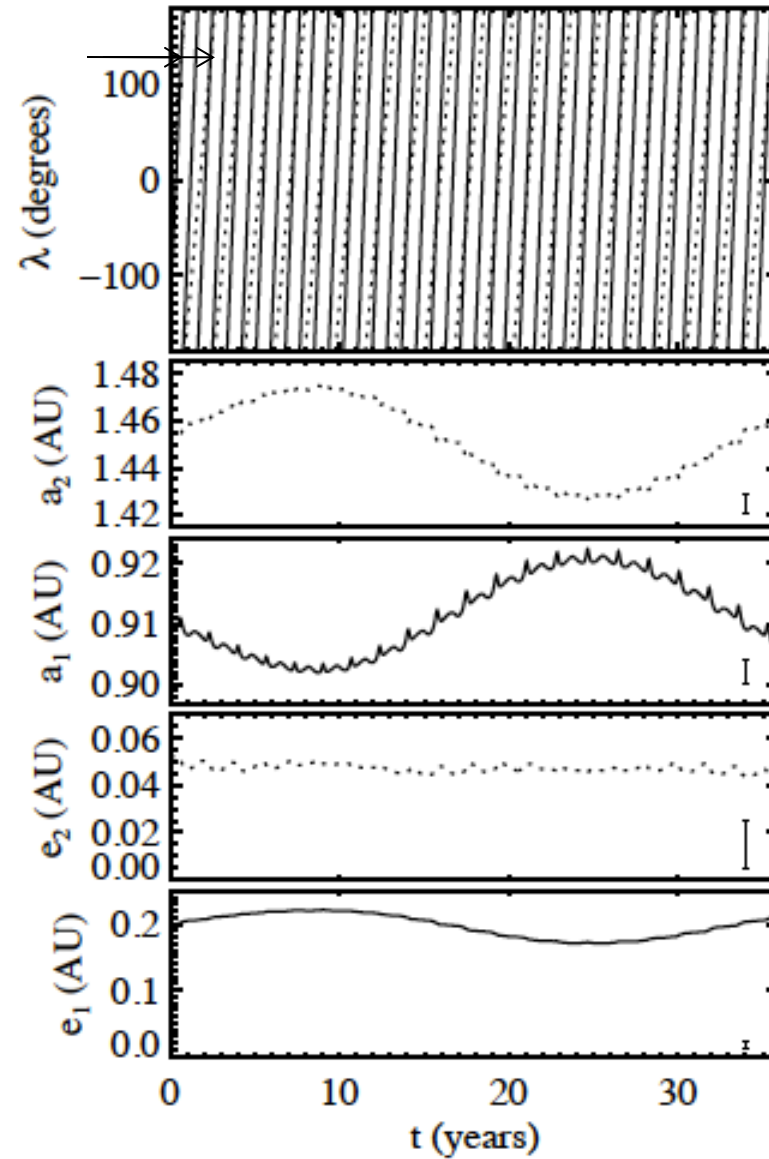
$P_2/P_1 = 2.44$
near 5:2



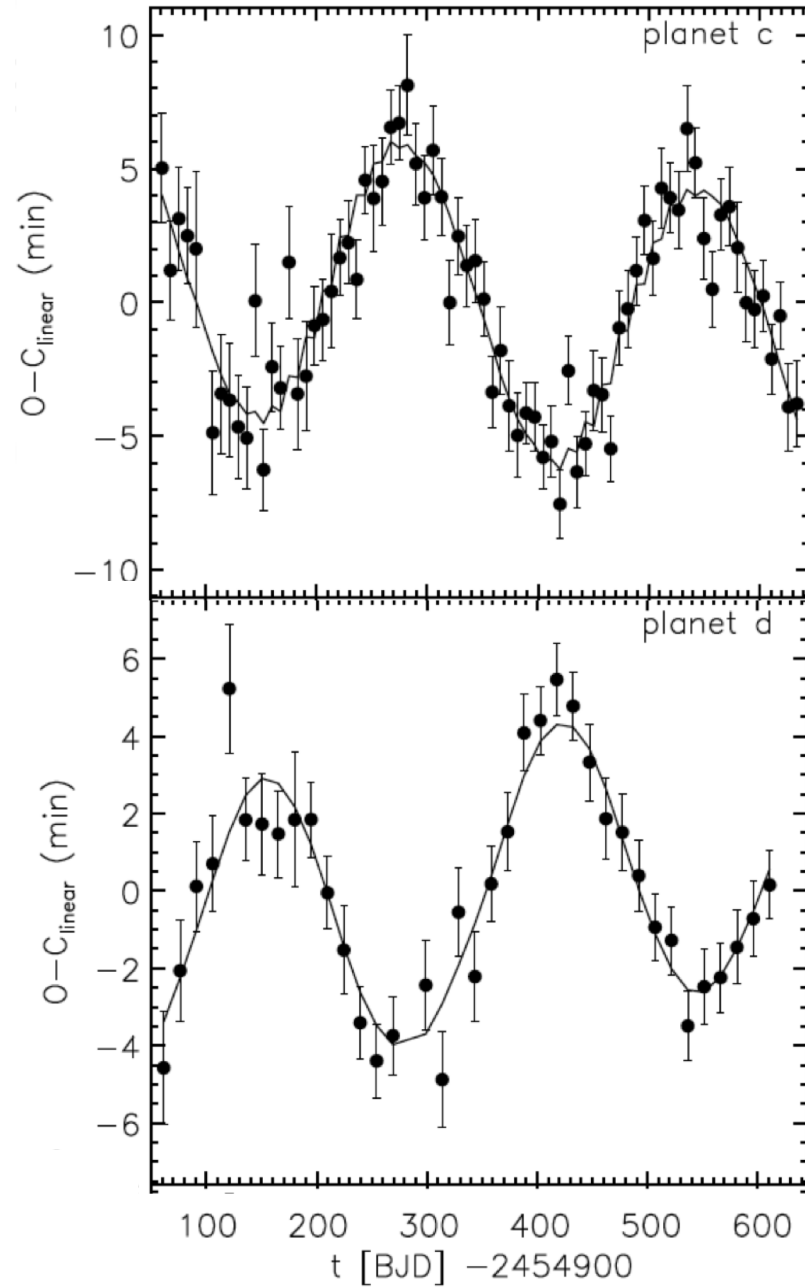
Dynamics: Resonant Orbits



$$P_2/P_1 = 2.00$$



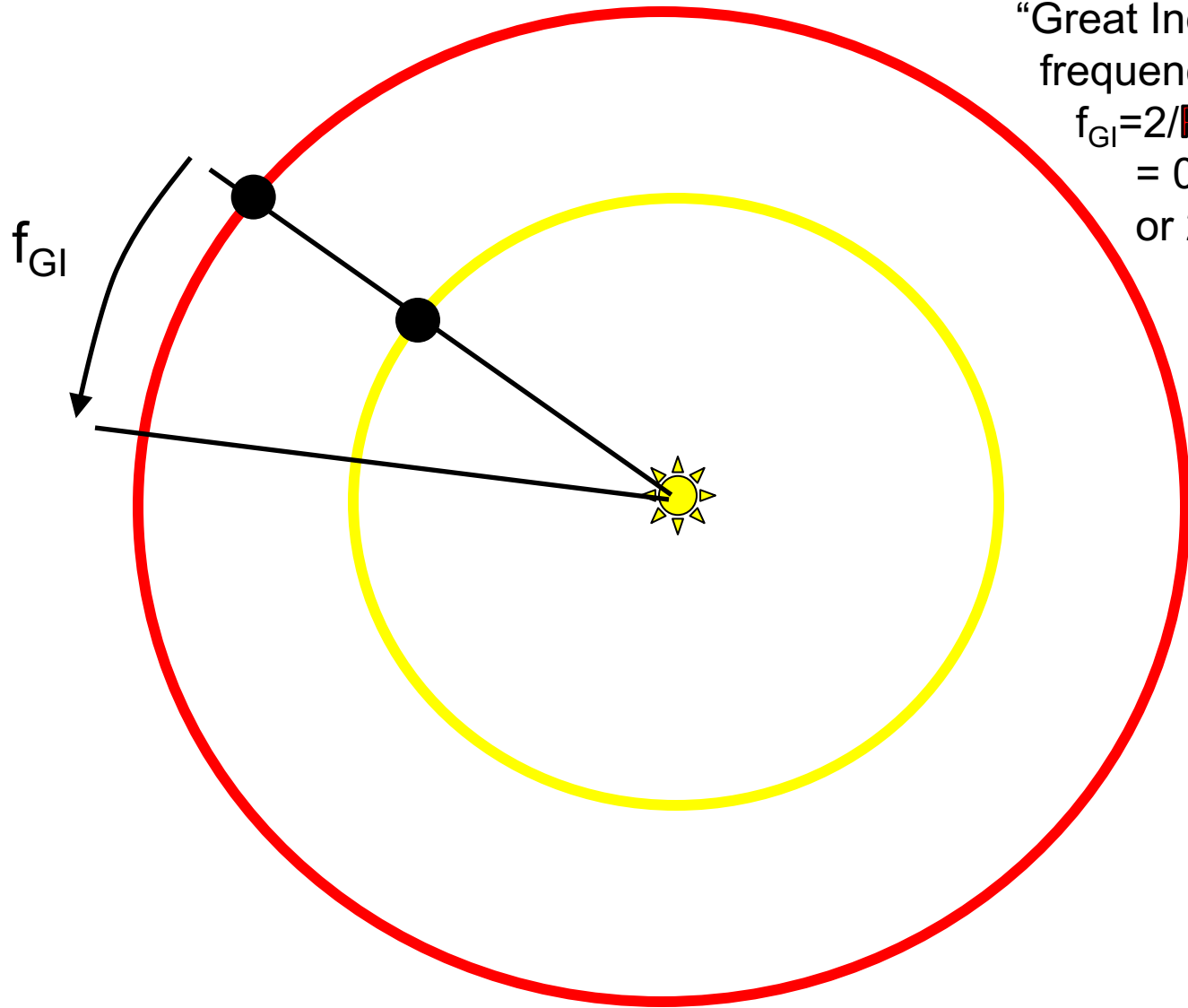
P = 7.6416 days



P = 14.8589 days

P/P = 1.944 \approx 2/1

Kepler-18
Cochran, Fabrycky
et al. 2011



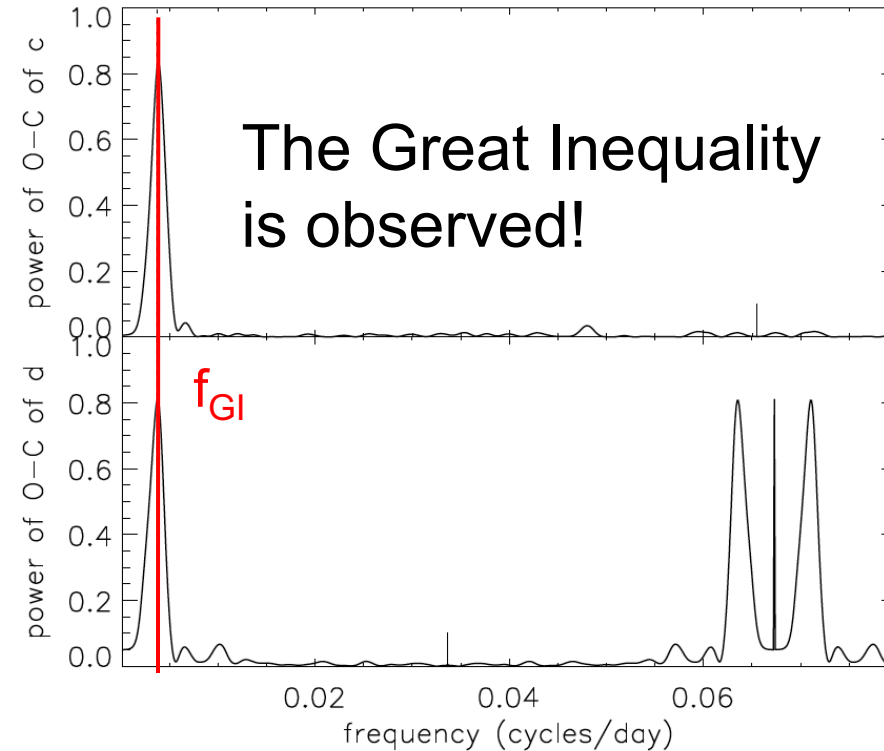
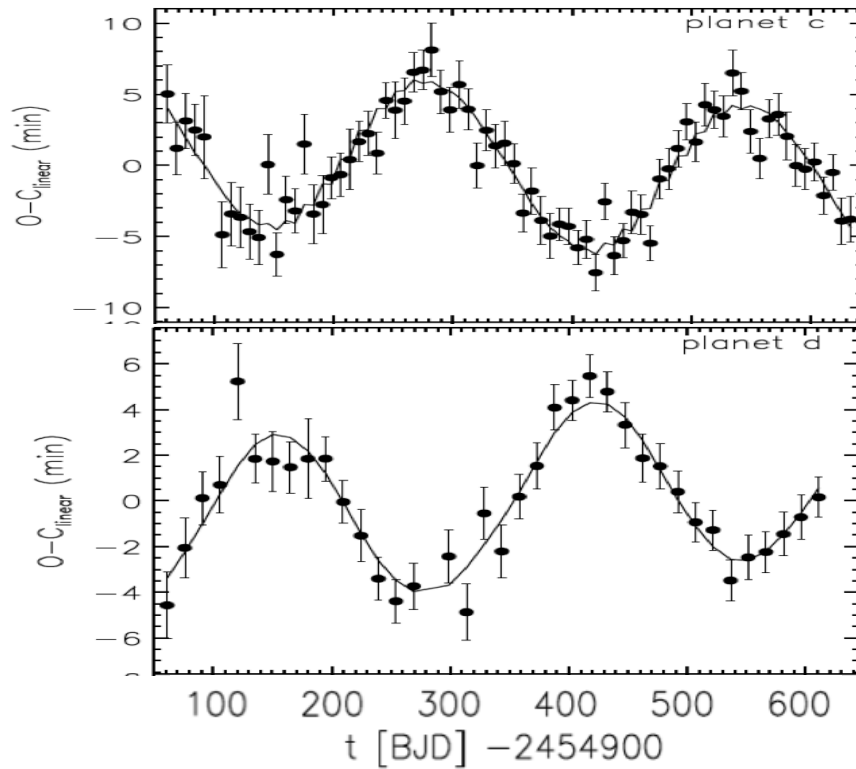
“Great Inequality”

frequency:

$$f_{GI} = 2/P - 1/P$$

$$= 0.0037 \text{ d}^{-1}$$

or 270 days



Planet	Period (days)	RV Mass (M_{Earth})	TTV Mass (M_{Earth})	e
b	3.5	12 ± 5	18 ± 9	n/a
c	7.6	15 ± 5	17.3 ± 1.7	0.00034 ± 0.00014
d	14.9	28 ± 7	15.8 ± 1.3	0.00045 ± 0.00052

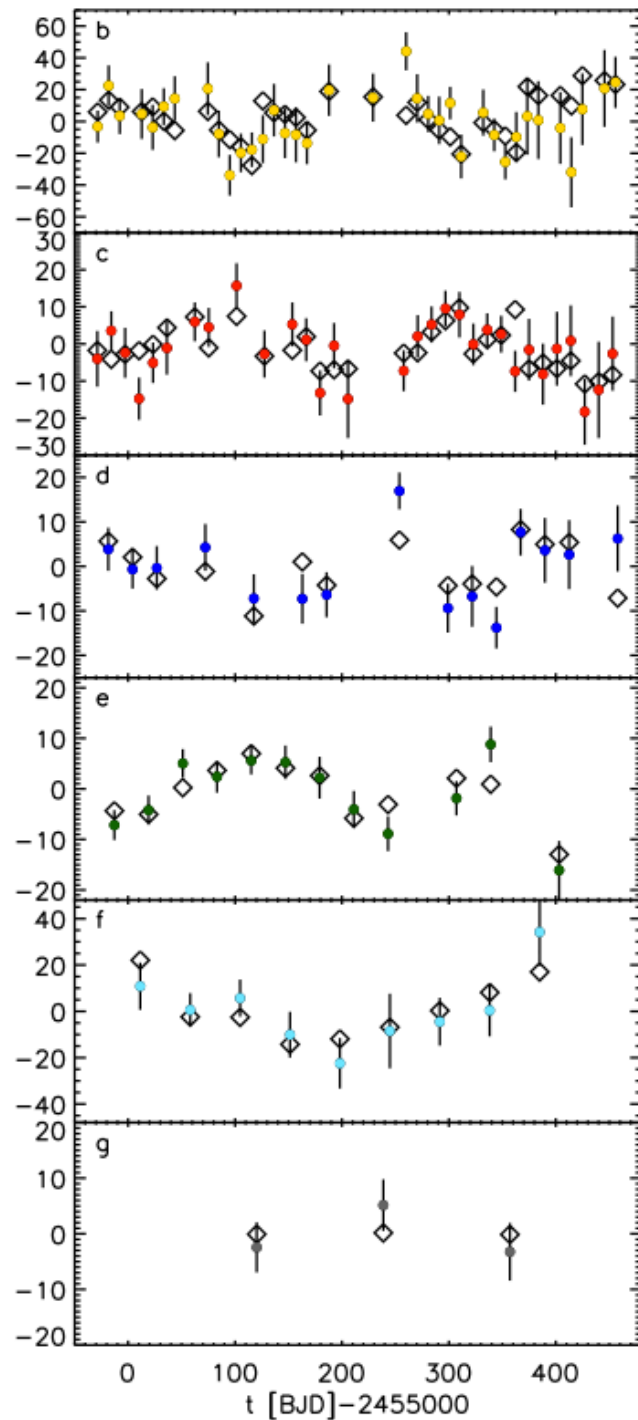
$$P_{\text{TTV}} = 1 / |j/P_2 - k/P_1|$$

Cochran, Fabrycky et al. 2011
 Fabrycky+12: We can use this timescale to be the validating signature of two transiting planets--> Kepler-23-32

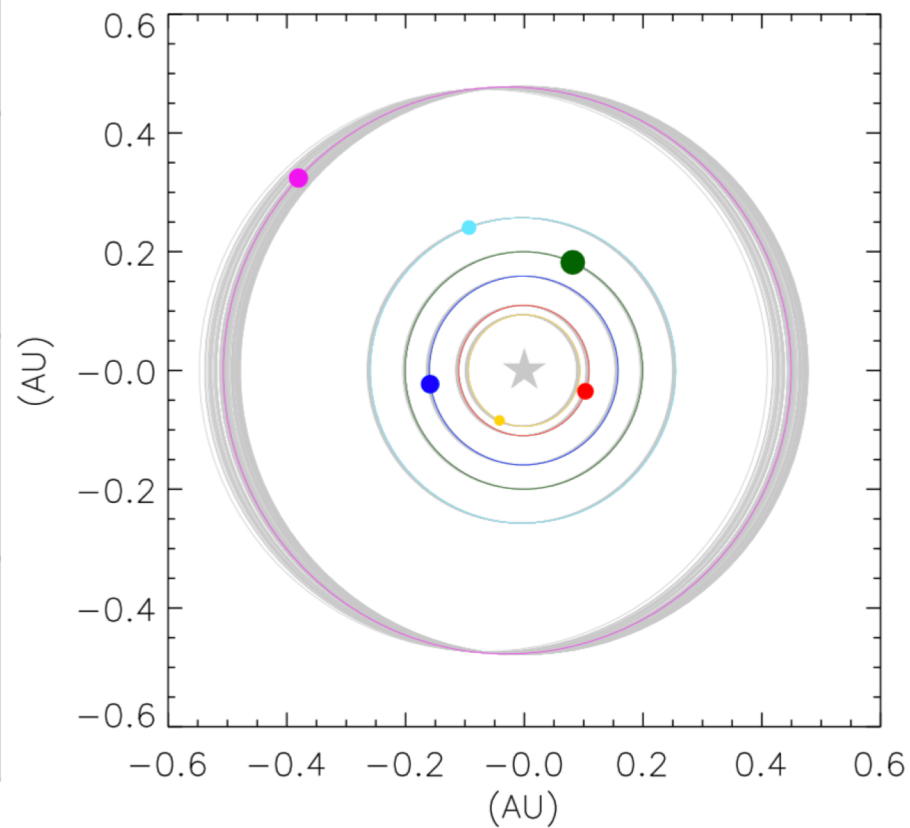
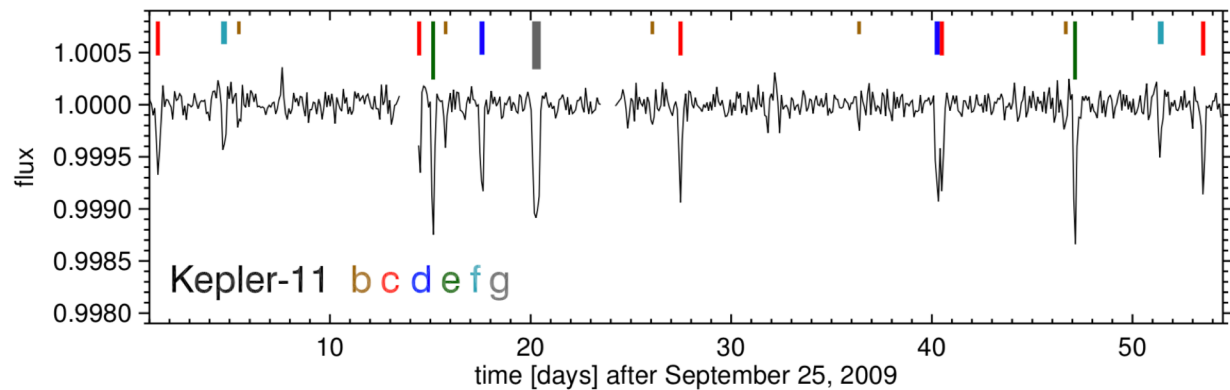
Lissauer, Fabrycky
et al. 2011

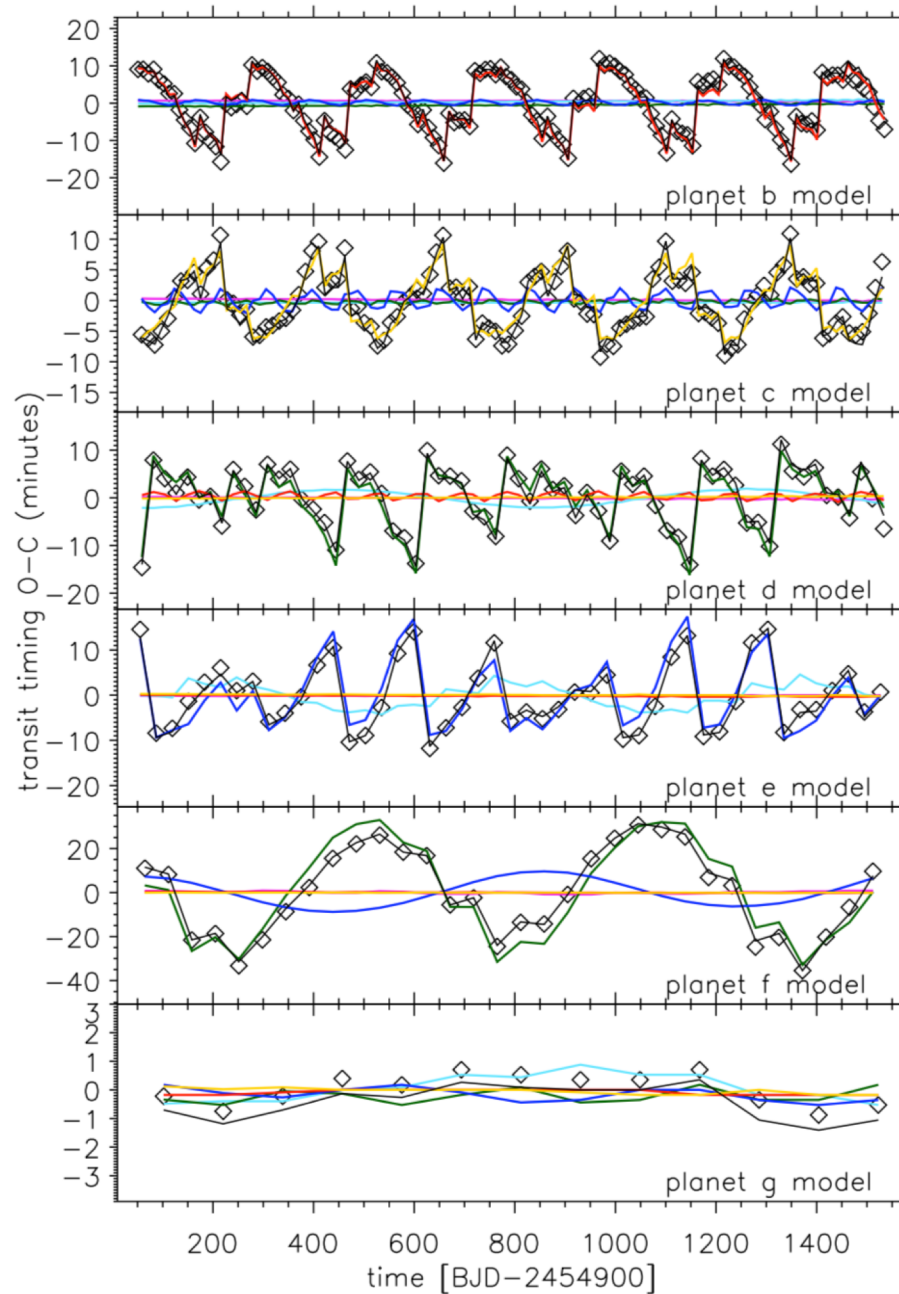
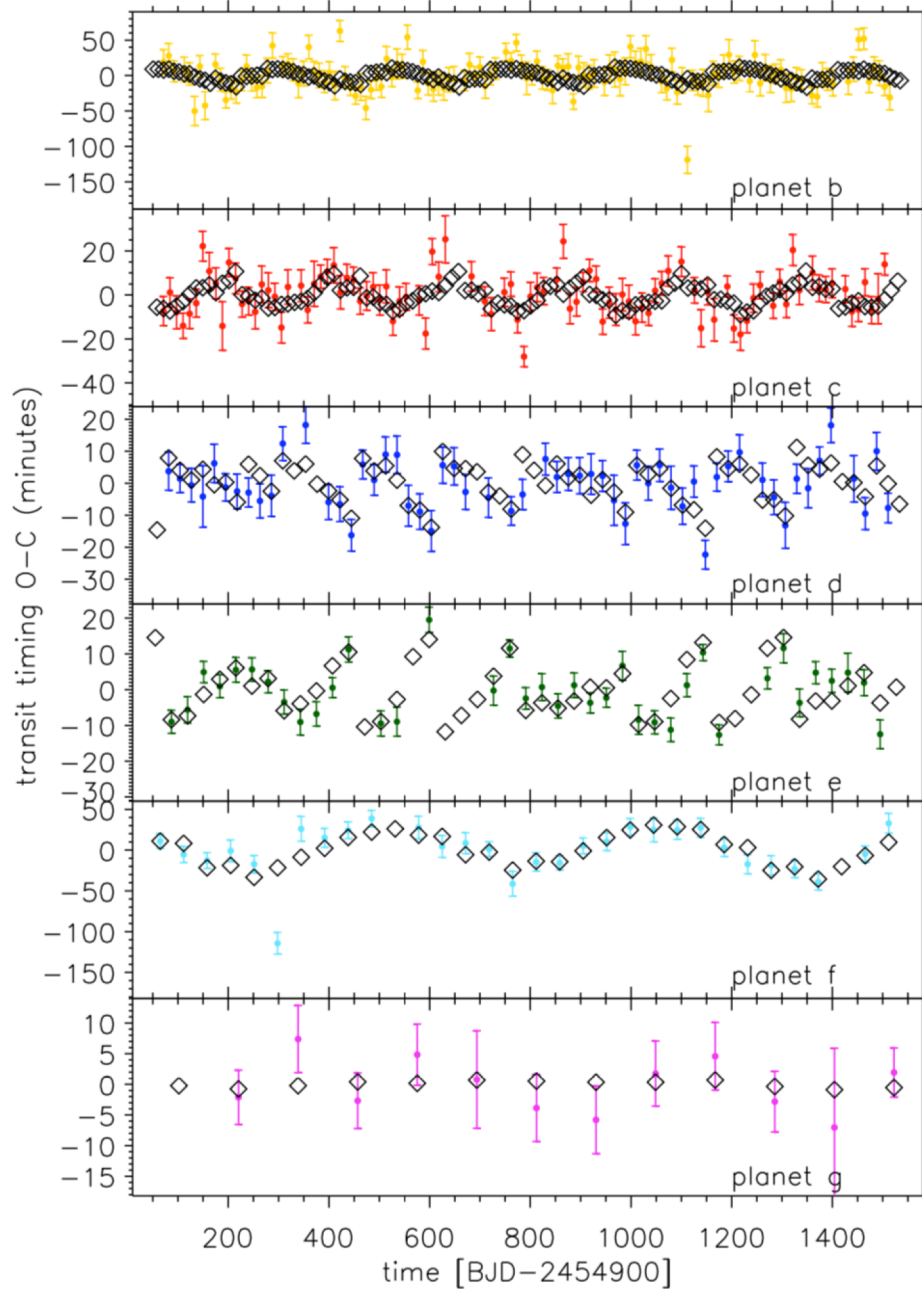
Latest:
Borsato+14
Bedell/Mills/DF+16

O-C (min)



Kepler-11

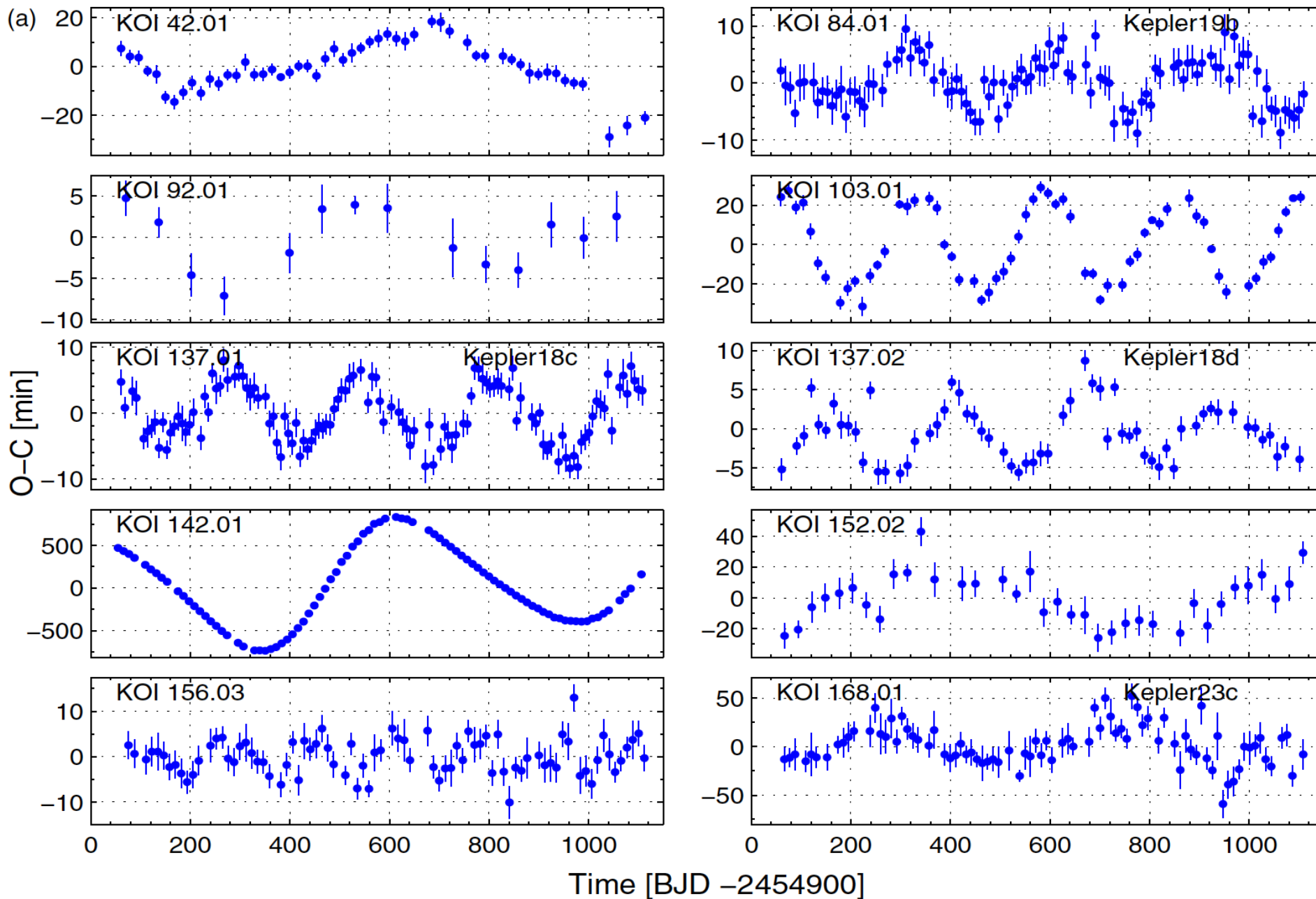




Note linearity of the signal – pairs' effect simply adds up to the 6-planet model.

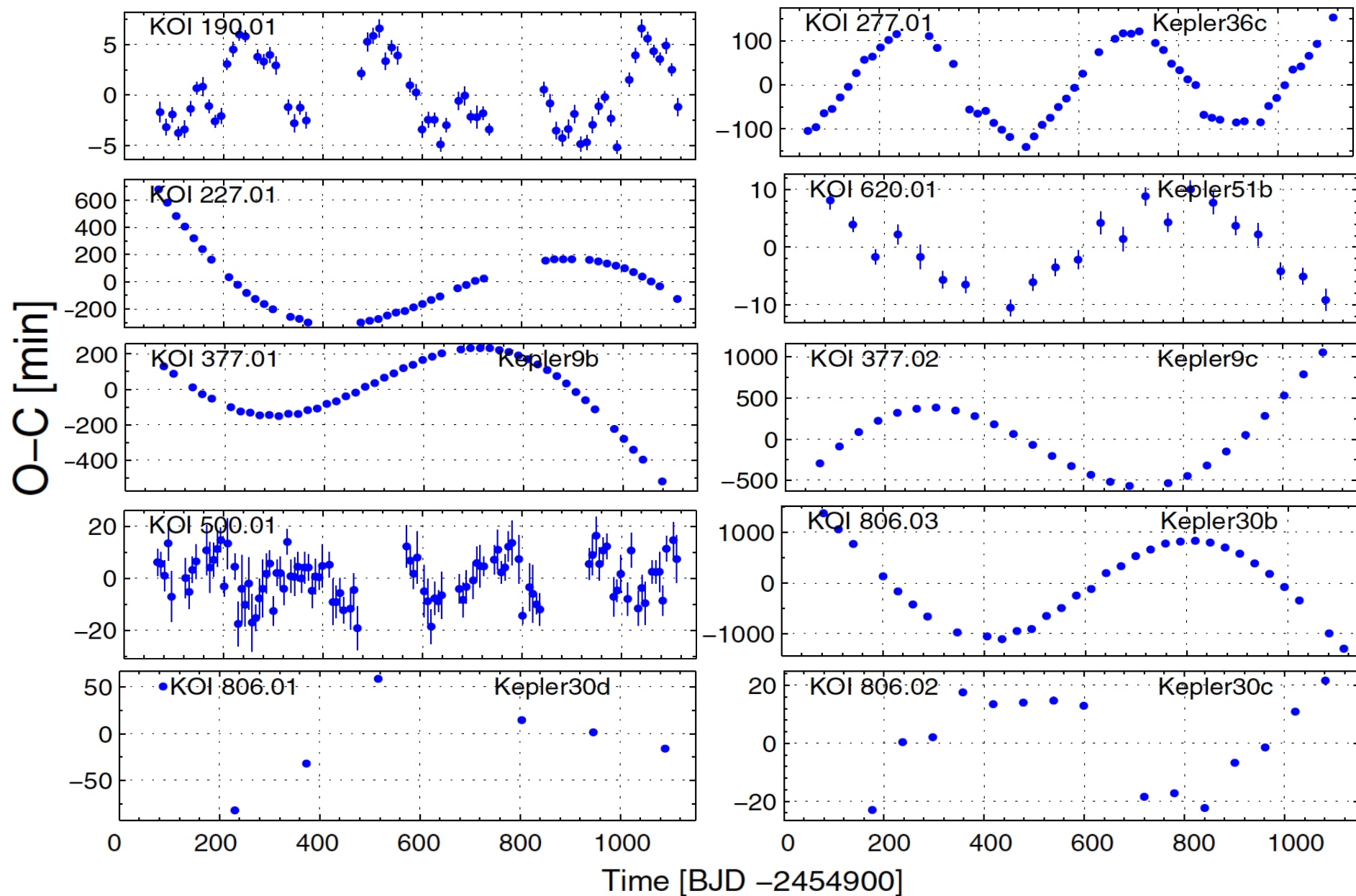
260 TTV detections

Holczer, Mazeh et al. 2013



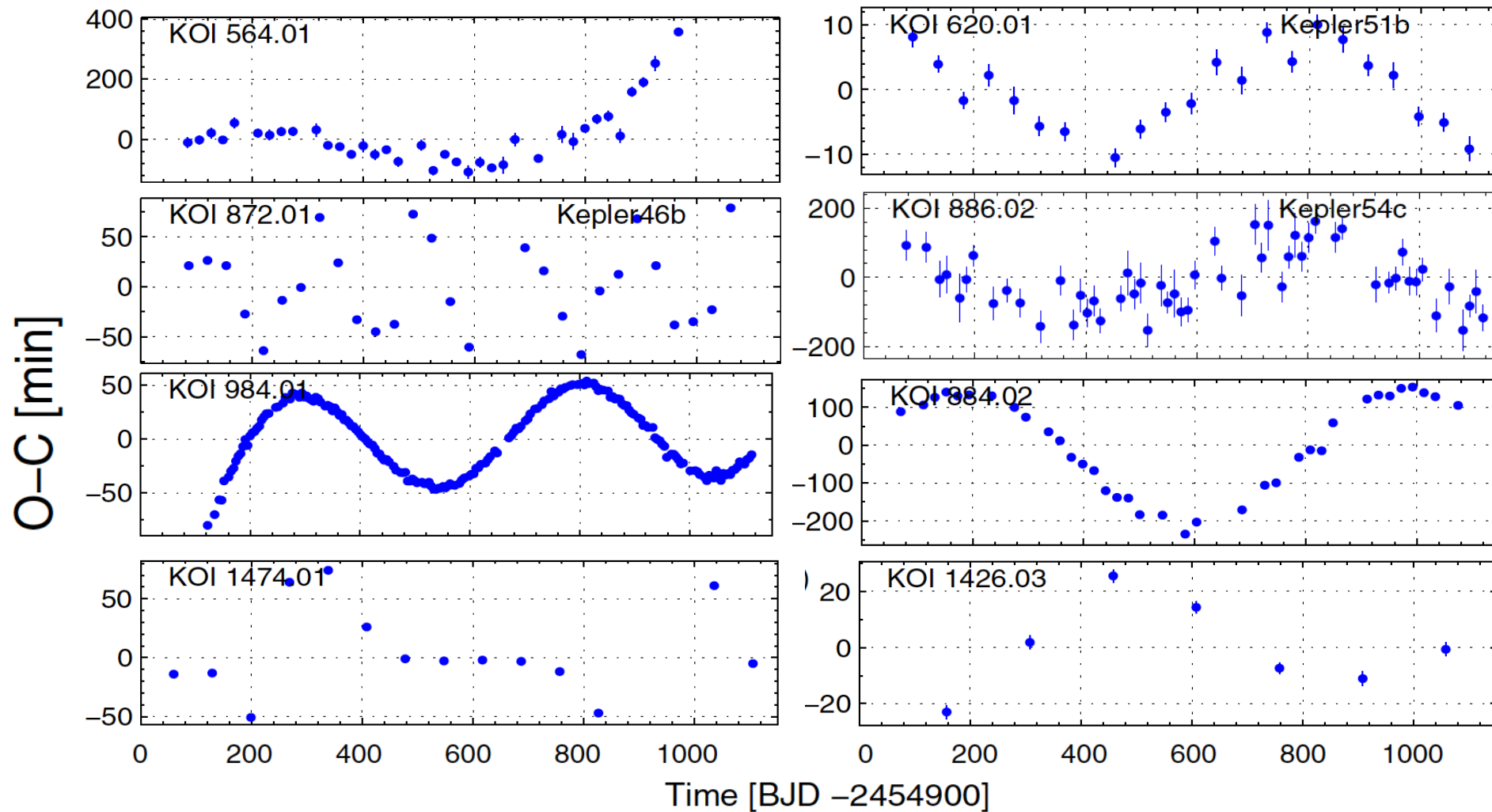
Cont'd

Holczer, Mazeh et al. 2013

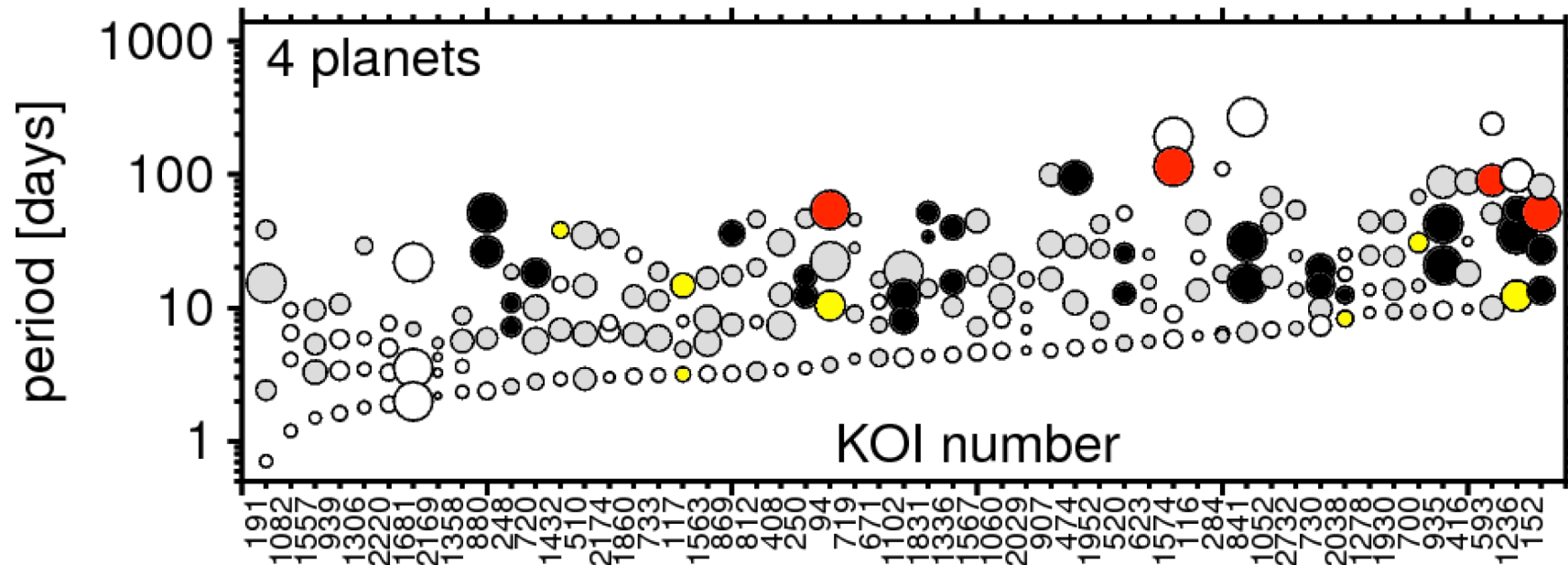


Cont'd...

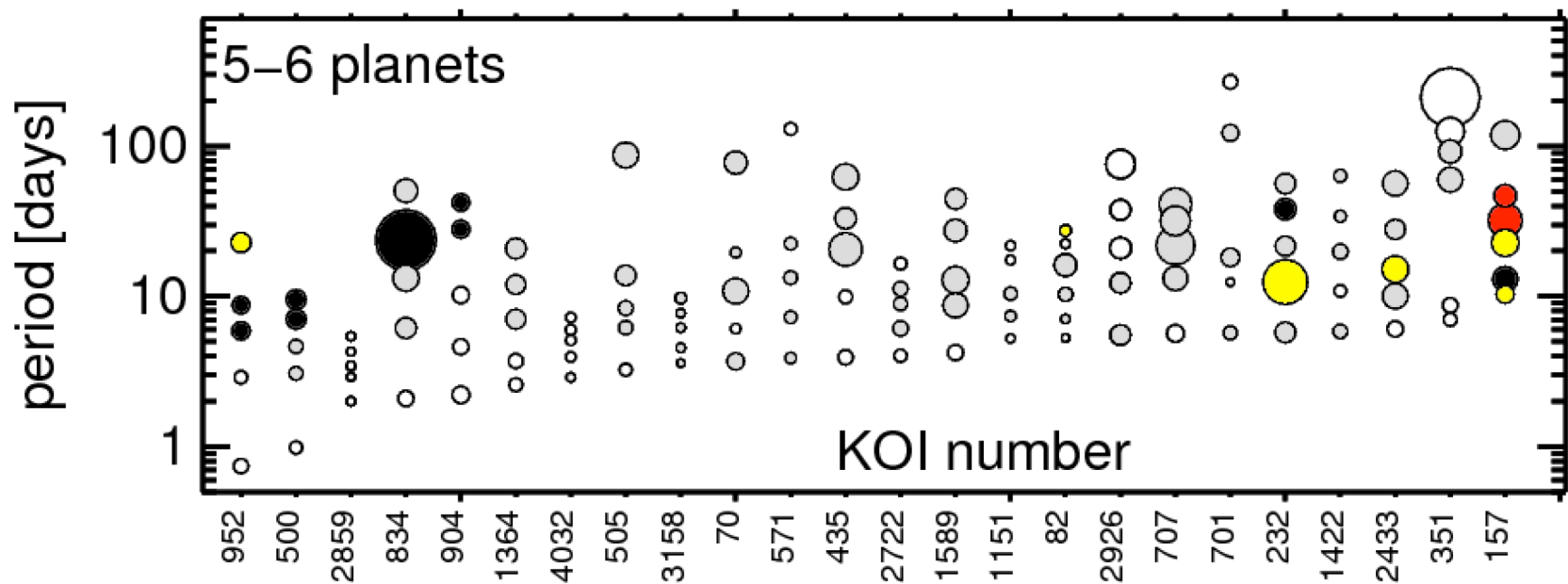
Holczer, Mazeh et al. 2013



.....



Sinusoidal (strong)
 Non-Sinusoidal (strong)
 Either; weak but significant
 Searched, but absent
 Not searched

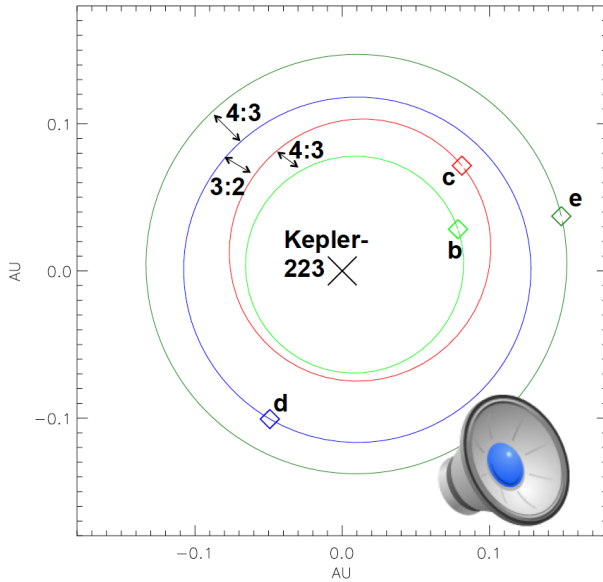


260 TTV detections out of 2599 with large individual transits (Holczer+16)

528 out of 4629 candidates, total (Ofir+18)

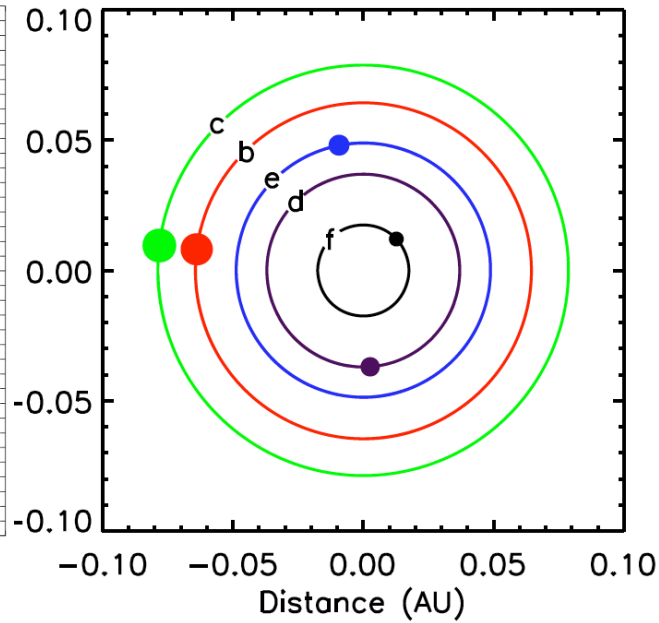
The Resonant Chains

Kepler-223



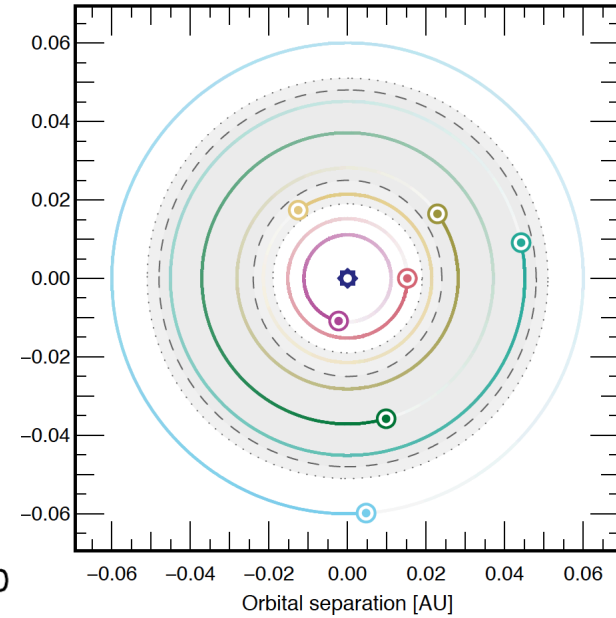
(4:3, 3:2, 4:3)

Kepler-80



(1.518, 1.518, 1.350)

TRAPPIST-1



(1.60293 (8:5), 1.67213 (5:3),
1.50622, 1.50939, 1.34174, 1.5192)

Also transiting:

Kepler-60 (Goździewski et al 2016, Jontof-Hutter et al. 2016)

K2-138 (Christiansen et al. 2017)

Doppler: GJ 876 (Rivera et al. 2010, Nelson et al. 2016)

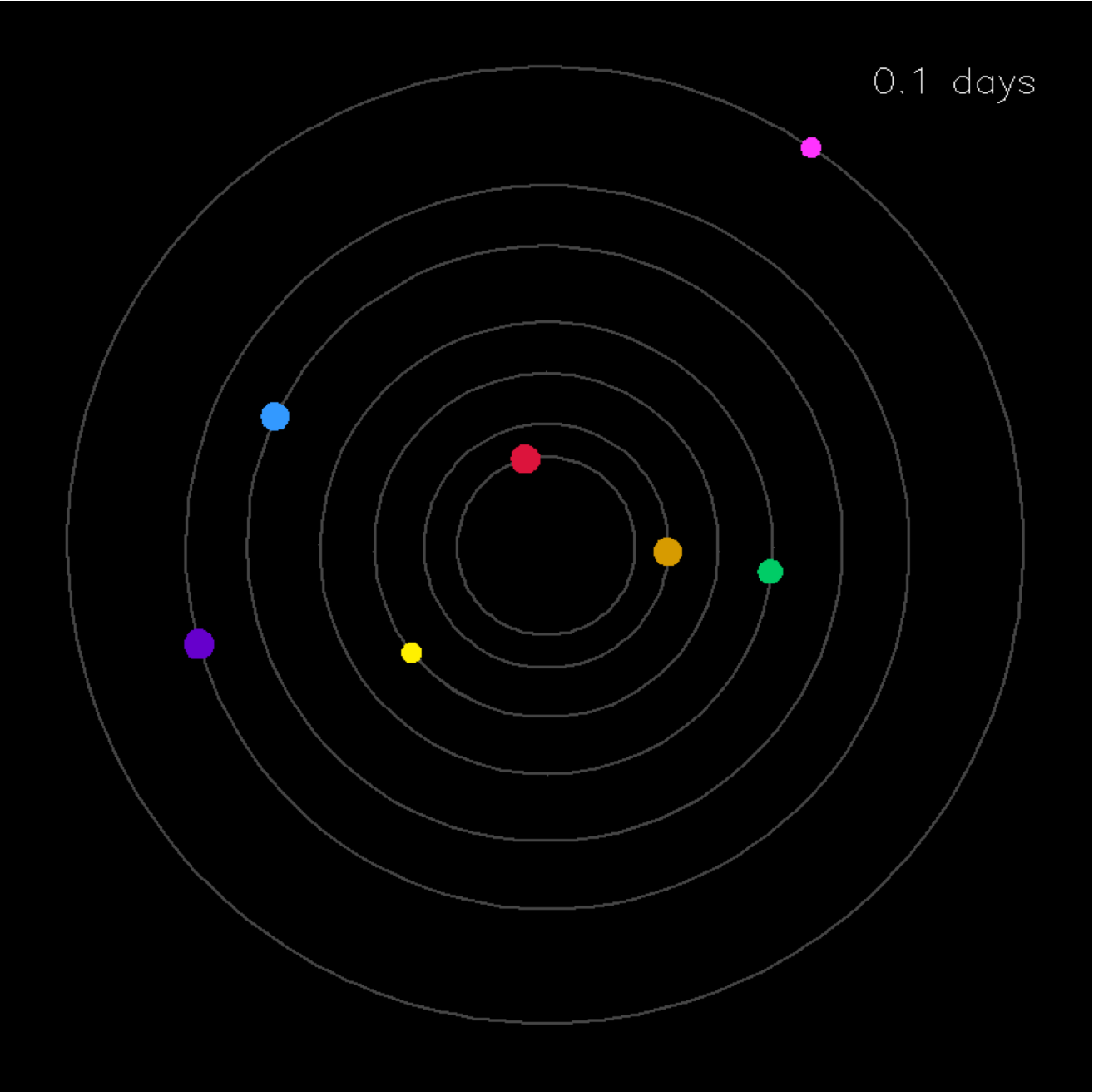
Imaging: HR 8799 (Fabrycky & Murray-Clay 2010, inferred from stability; Goździewski & Migaszewski 2014, migration simulation into correct phases)

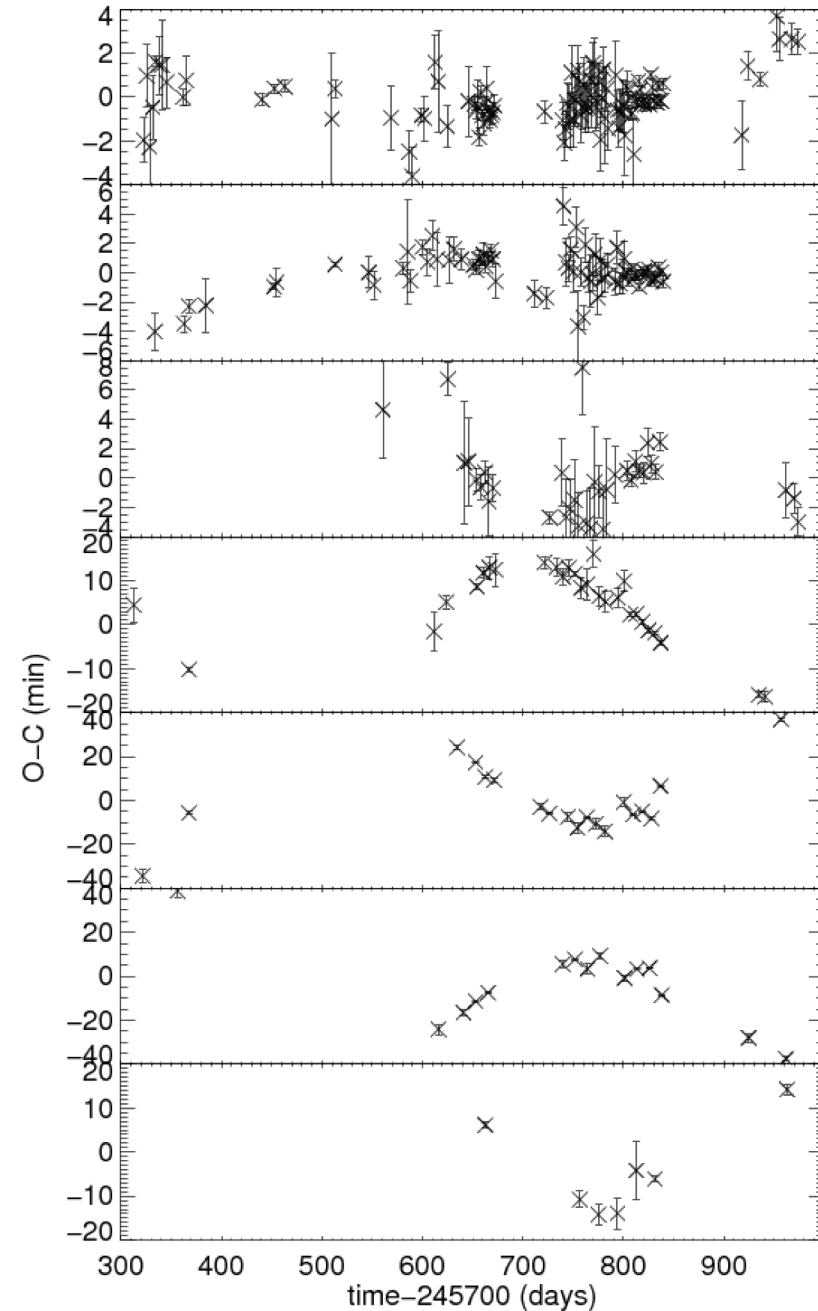
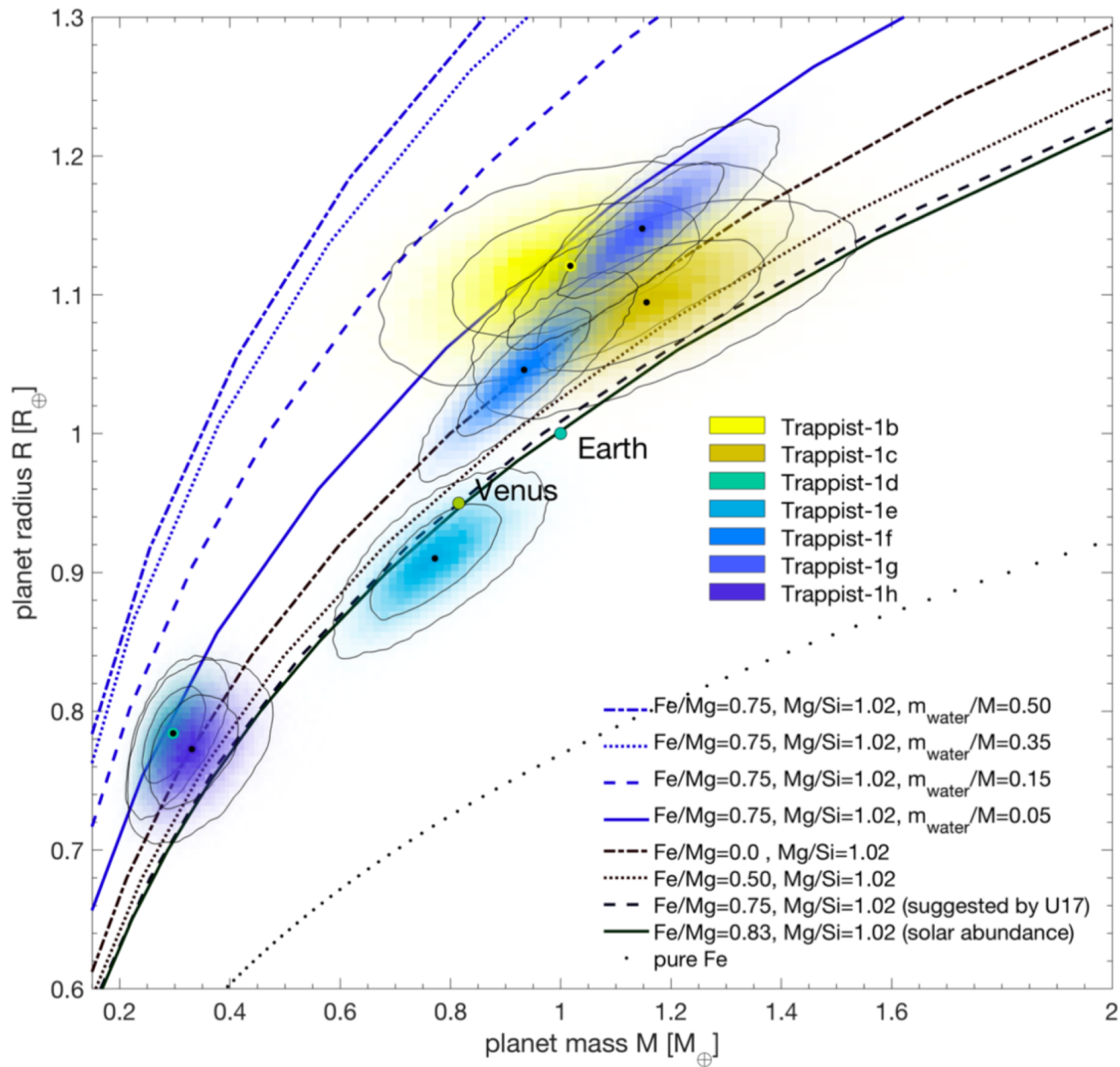
TRAPPIST-1

Planet	P (d)	P_{i+1}/P_i	n:m	$n/P_{i+1}-m/P_i$ (TTV freq., cycles/d)
b	1.51087081	1.60293	8:5	-0.0060535
c	2.4218233	1.67213	5:3	-0.0040494
d	4.049610	1.50622	3:2	-0.0020404
e	6.099615	1.50939	3:2	-0.0020395
f	9.206690	1.34174	4:3	-0.0020405
g	12.35294	1.5192	3:2	-0.002042
h	18.766			

Luger et al. 2017

Near-resonant super-period is 490 days.

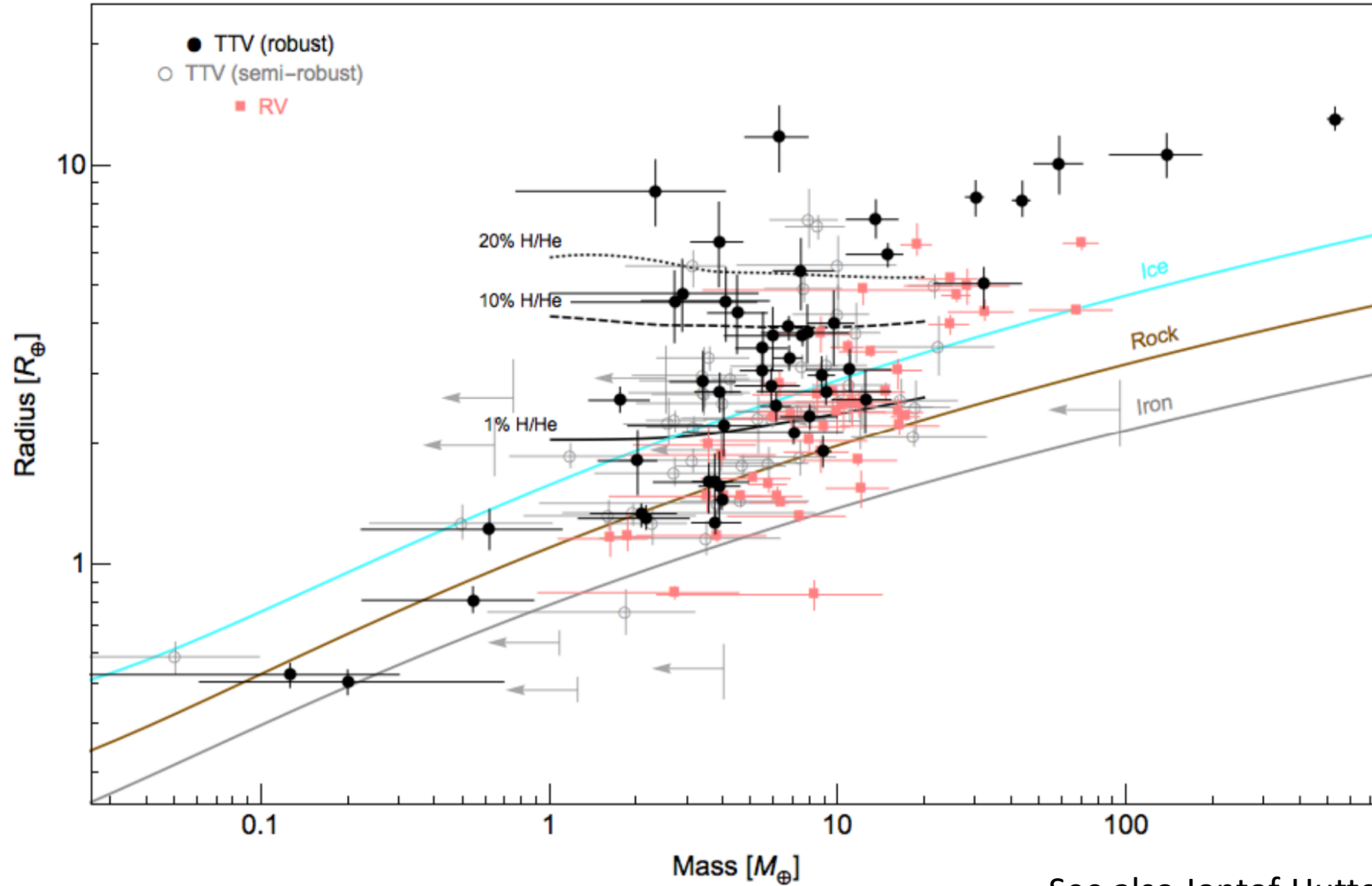




Grimm+18, leveraging Spitzer transit campaign of Delrez+18

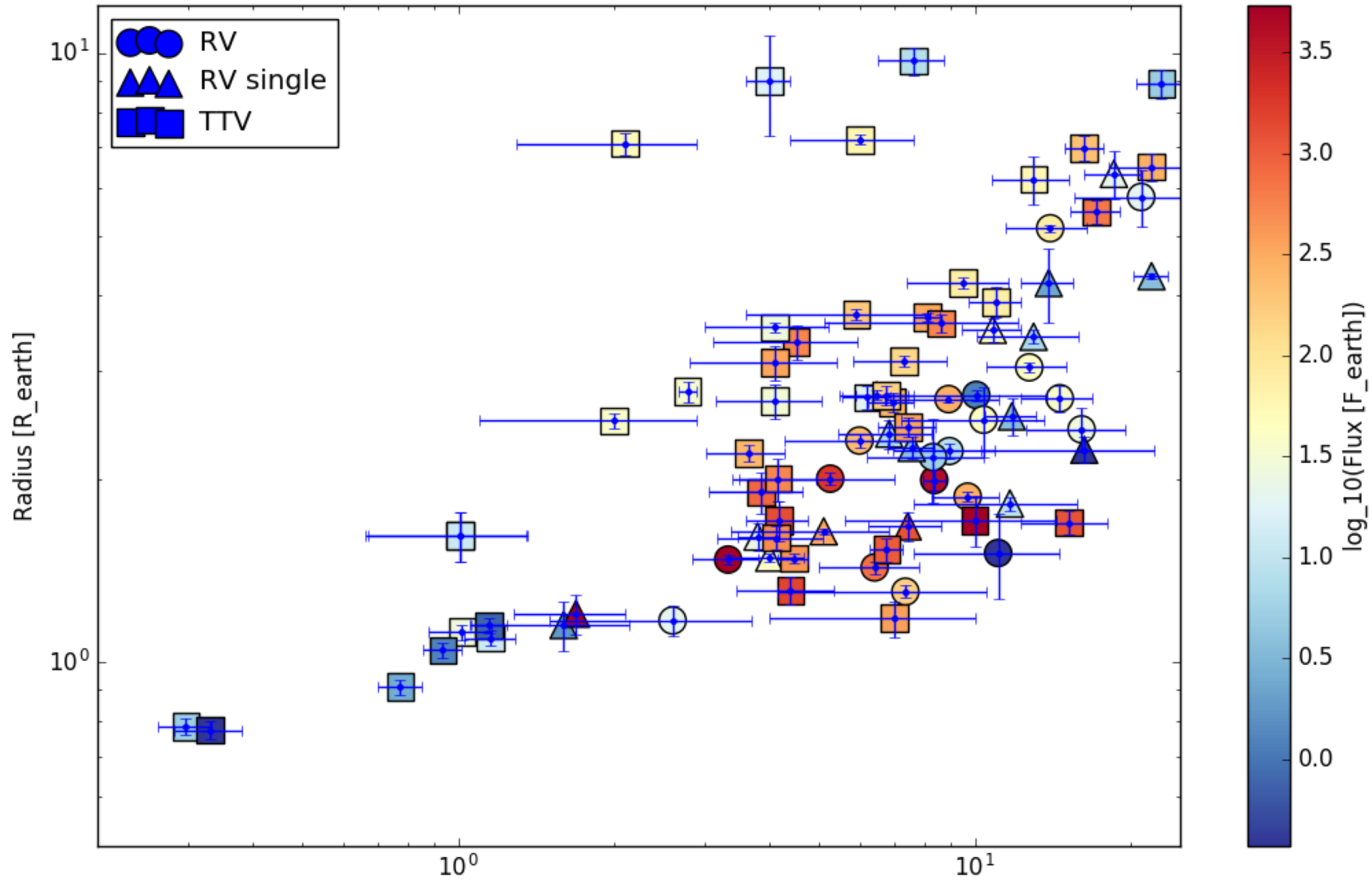
Sub-Neptunes vs. Super-Earths

Hadden & Lithwick 2017



See also Jontof-Hutter et al. 2016

Planet radius versus mass



Scorecard for
 $M < 25 M_{\text{Earth}}$:
TTV: 44
RV: 33

Agol & Fabrycky 2017, updated with TRAPPIST-1

Detection of Exoplanets by TTV

First, a
warning:
m/e degeneracy
(Lithwick+12).

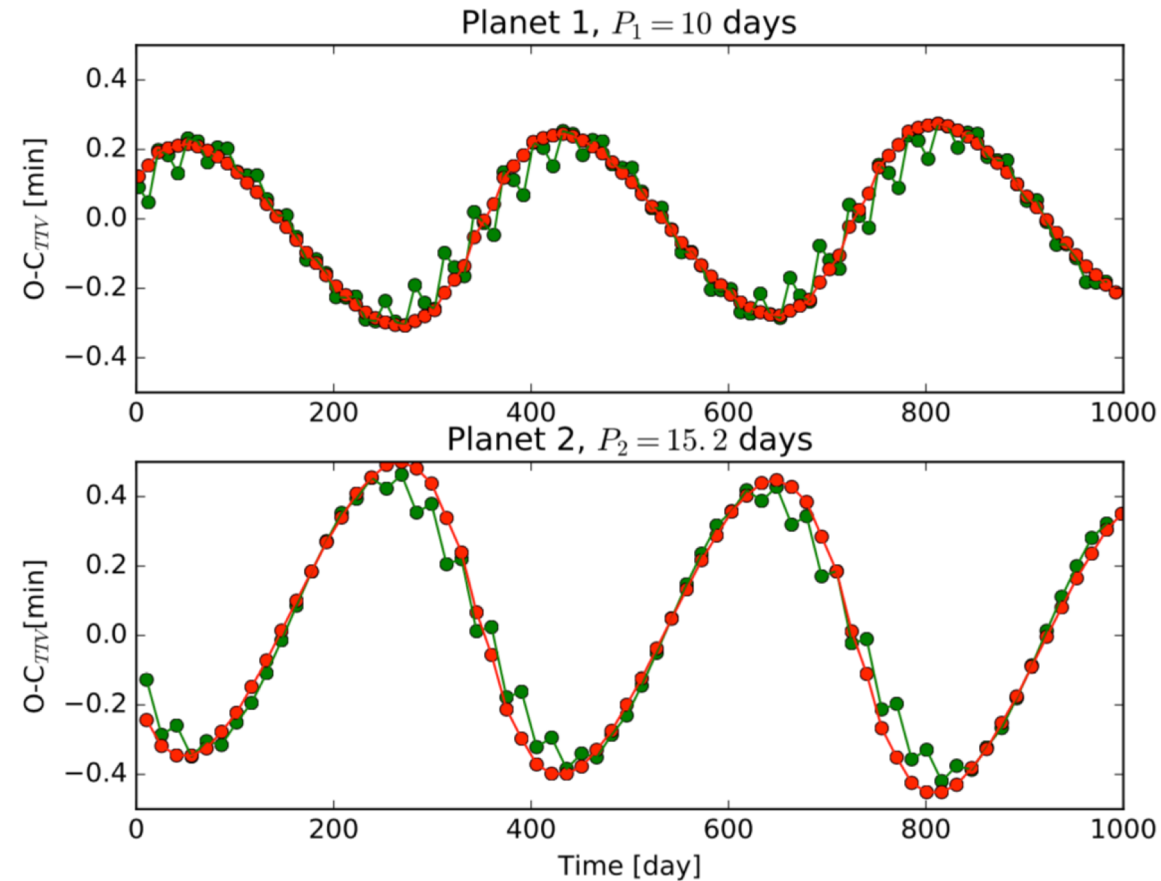
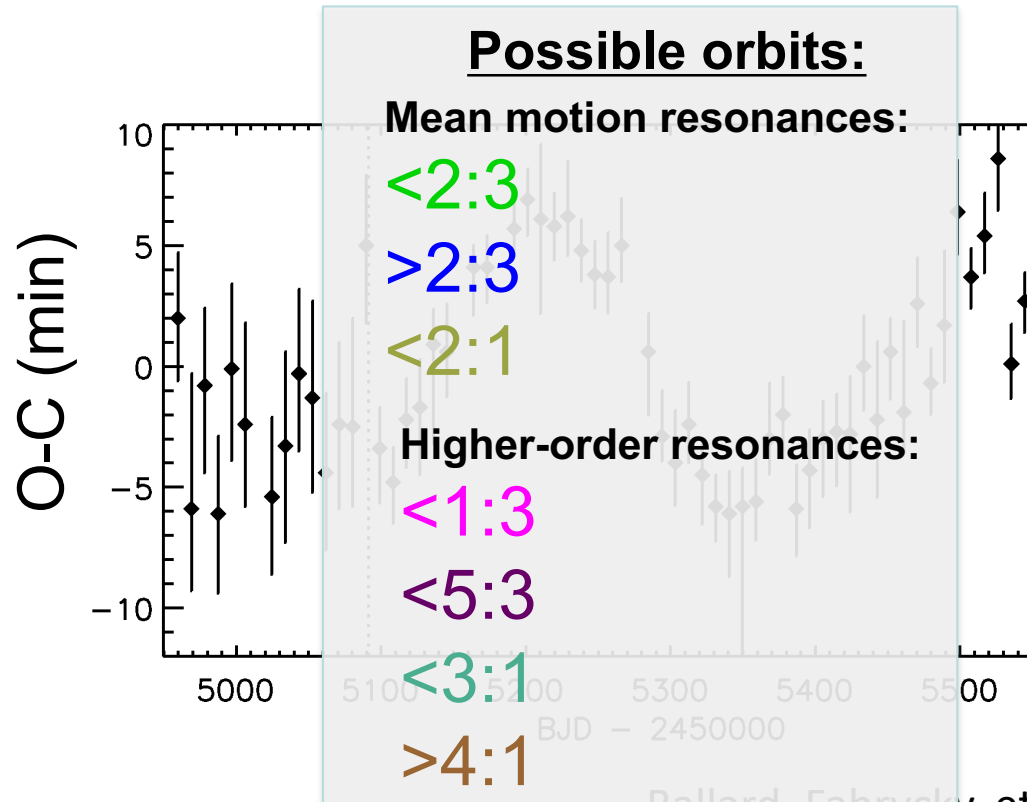


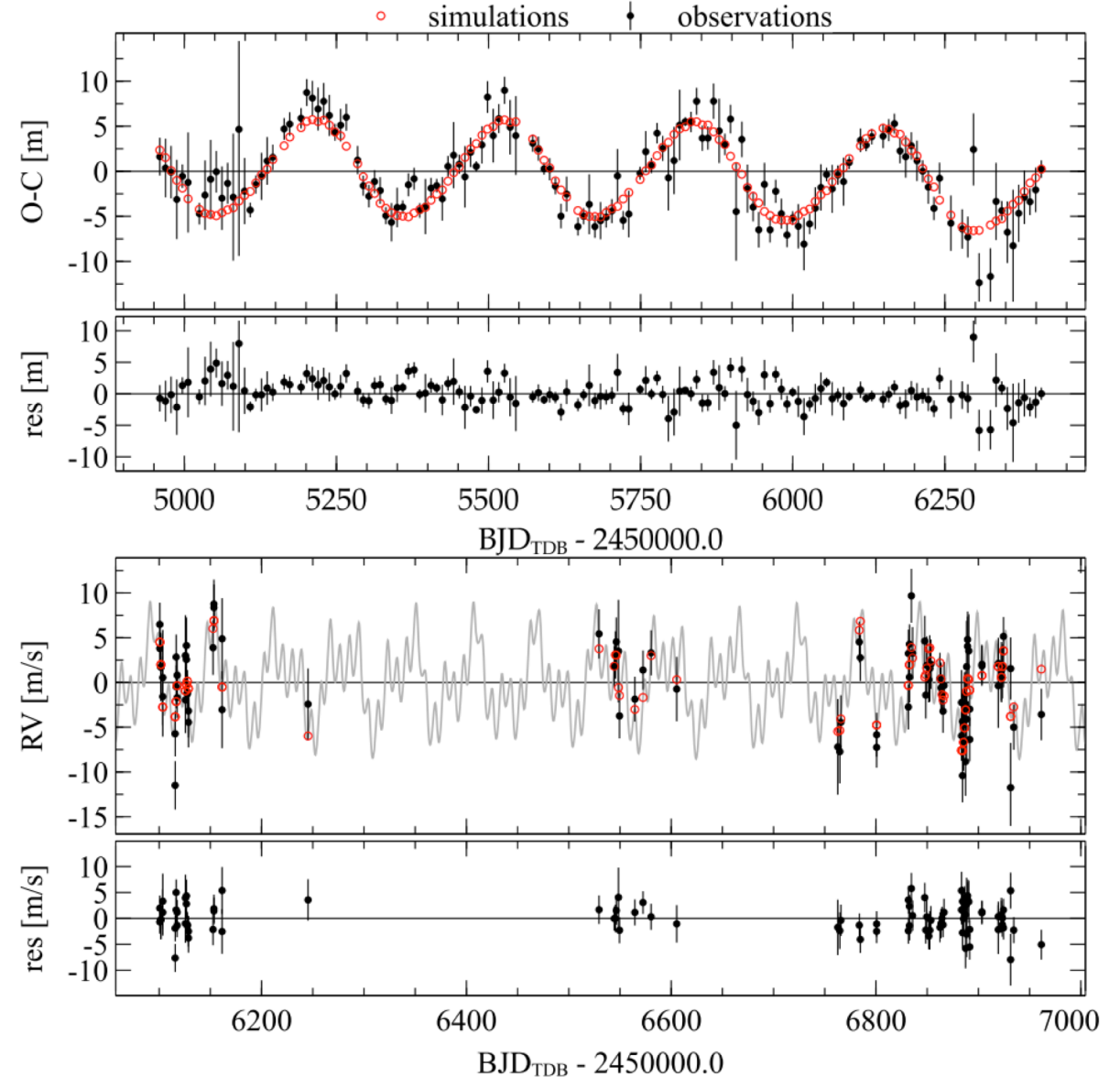
Fig. 2 Transit-timing variations of two low-eccentricity planets with larger mass ratios, $m_1 = m_2 = 10^{-6}m_*$ (green) compared with two higher eccentricity planets ($e_1 = e_2 = 0.04$) with smaller mass ratios $m_1 = m_2 = 10^{-7}m_*$. The zig-zag chopping component is apparent in the high-mass/low-eccentricity case, while less apparent in the low-mass/high-eccentricity case.

First successes: Kepler-19, first planet *apparent* through TTV



Planet	Period (days)	Mass [M_{\oplus}]
K19b	$9.28716^{+0.00004}_{-0.00006}$	$8.4^{+1.6}_{-1.5}$
>3:1 K19c	$28.731^{+0.012}_{-0.005}$	$13.1^{+2.7}_{-2.7}$
K19d	$62.95^{+0.04}_{-0.30}$	$22.5^{+1.2}_{-5.6}$

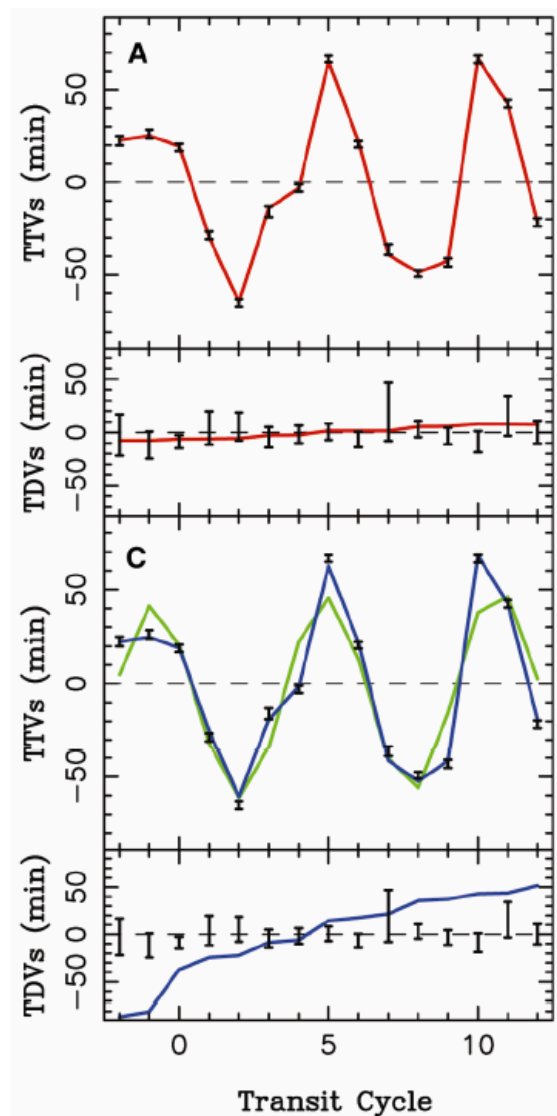
Note: A red arrow labeled 'x3.09' points from K19c to K19b.



Maltavolta+2017

First successes: KOI-872 = Kepler-46

First planet *discovered* through TTV/TDurationV

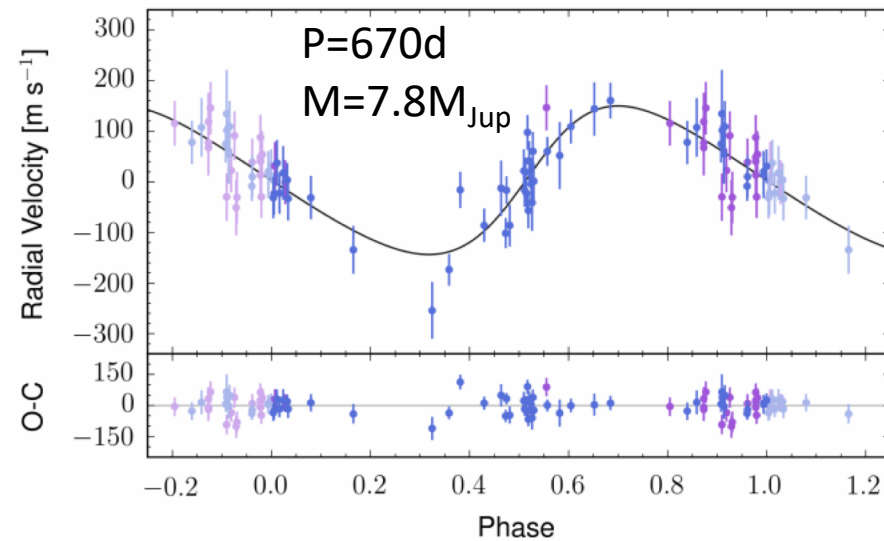
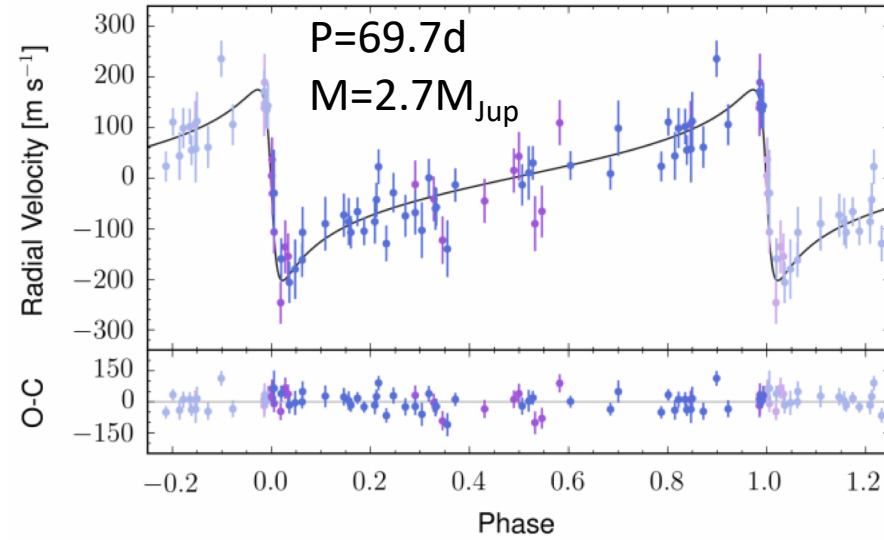
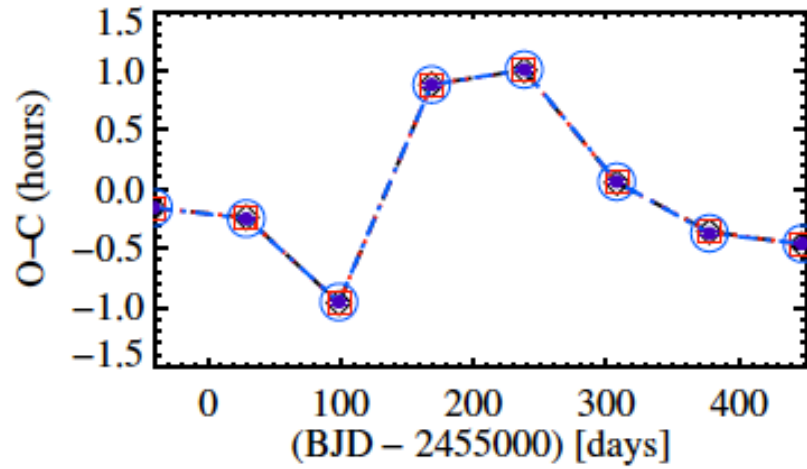


	KOI-872b	KOI-872c
τ_0 [BJD _{UTC}]	2455053.2826 ^{+0.0013} _{-0.0014}	—
P_P [days]	33.60134 ^{+0.00021} _{-0.00020}	57.004 ^{+0.091} _{-0.100}
R_P/R_*	0.0887 ^{+0.0011} _{-0.0012}	—
b_P	0.759 ^{+0.022} _{-0.027}	3.1 ^{+1.1} _{-1.9}
a_P/R_*	44.9 ^{+2.1} _{-1.8}	63.9 ^{+2.9} _{-2.5}
i_P [°]	89.033 ^{+0.076} _{-0.069}	87.25 ^{+1.70} _{-0.95}
a_P [AU]	0.1967 ^{+0.0029} _{-0.0028}	0.2799 ^{+0.0041} _{-0.0040}
e_P	0.01 ^{+0.01} _{-0.01}	0.0145 ^{+0.0035} _{-0.0039}
Ω_P [°]	270	303 ⁺²⁰ ₋₃₄
ϖ_P [°]	—	329.4 ⁺¹¹ _{-9.2}
λ_P [°]	0	338.3 ^{+1.3} _{-1.4}
M_P/M_*	$<6.4 \times 10^{-3}$	$3.97^{+0.17}_{-0.14} \times 10^{-4}$
M_P [M _J]	<6	0.376 ^{+0.023} _{-0.020}
R_P [R _J]	0.812 ^{+0.043} _{-0.043}	—

Nesvorny et al. 2012

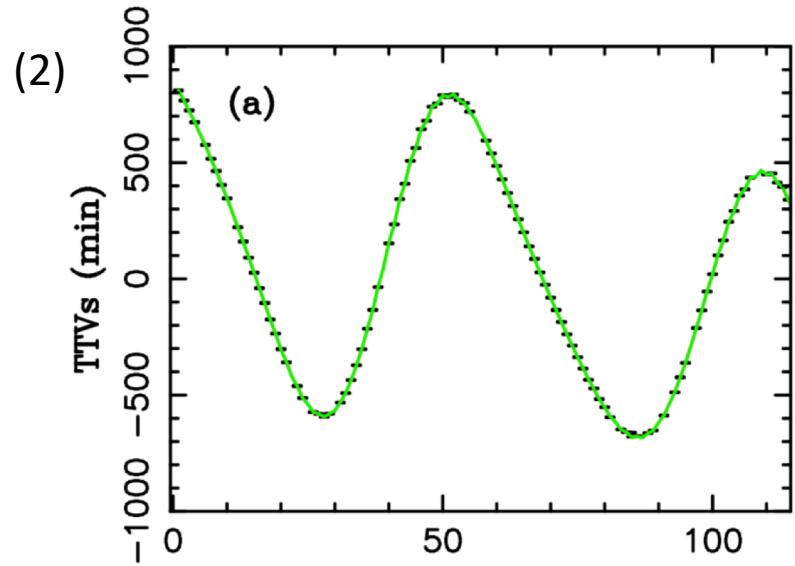
Two more examples:

(1)



RV detection:
Almenara+18

Two more examples:



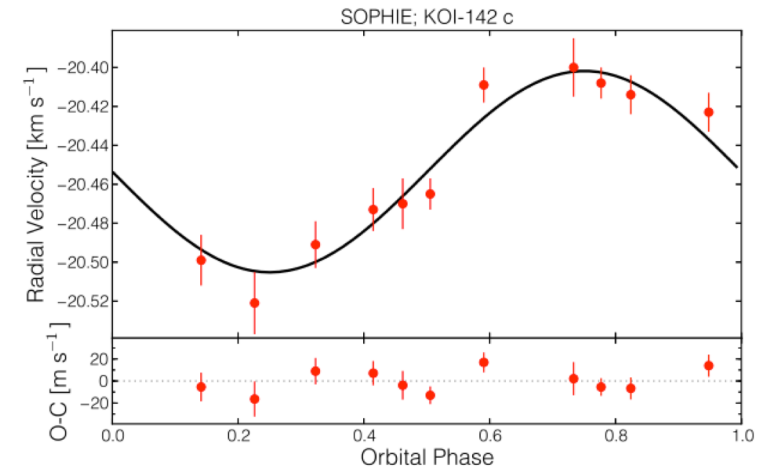
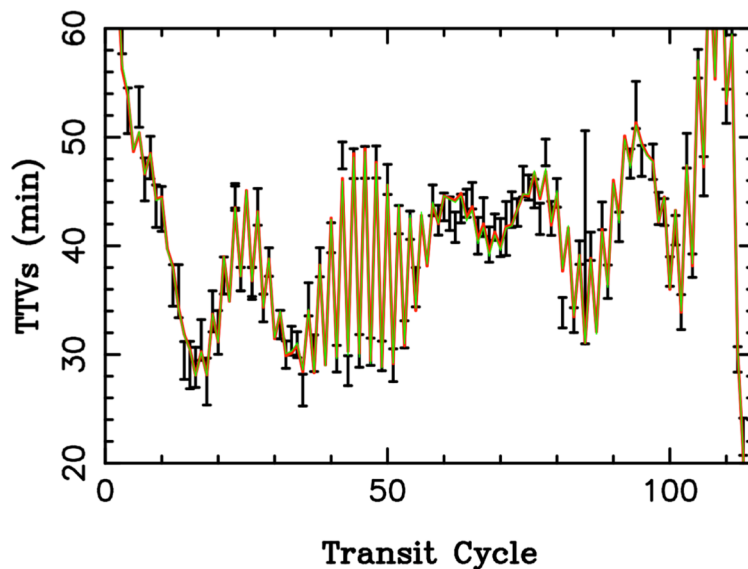
KOI-142

Nesvorny et al. (2012)

Neptune-size transiting planet strongly perturbed by a giant, resonant companion:

$$M_p = 0.675(+0.020/-0.013) M_{\text{jup}}$$

$$P = 22.338 \pm 0.003 \text{ days}$$



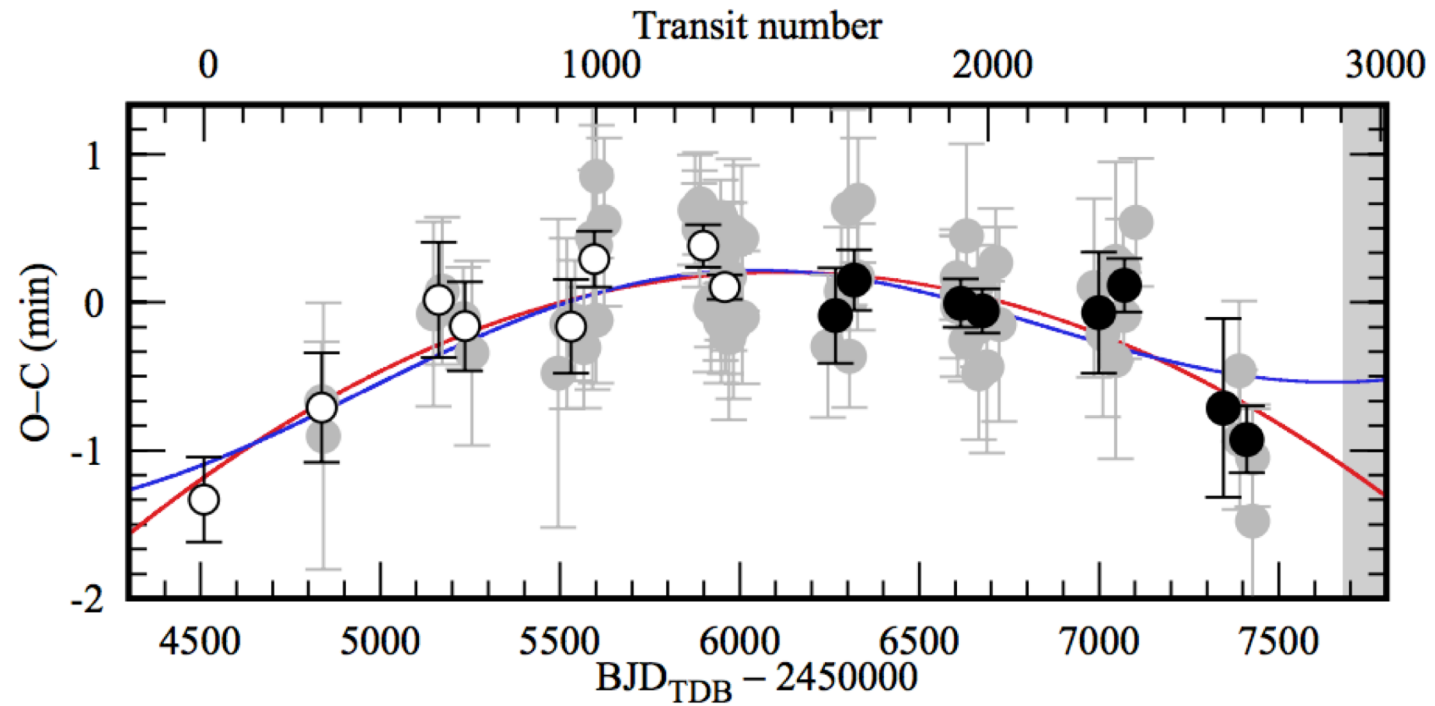
Barros et al. (2014)

$$0.76^{+0.32}_{-0.16}$$

$$22.10 \pm 0.25$$

A frontier: Tidal Decay

- Would characterize the *star*, not the planet. TTV of WASP-12b:



$$dP/dt = (-2.56 \pm 0.40) \times 10^{-2} \text{ s yr}^{-1}$$
$$Q = 2.5 \times 10^5$$

P=1.09days; M_p=1.41M_{Jup}

Maciejewski+16

TTV – a characterization tool

- Several dozen transiting pairs have masses & eccentricities characterized, including a system of a few habitable planets (TRAPPIST-1)
- About 100 transit discoveries have been validated, but with only rough characterization
- The mass/radius results show a lack of atmospheres with higher effective temperature, leading to the differentiation of sub-Neptunes and super-Earths
- Tidal decay may be the next big discovery from TTV

TTV Bibliography

- First, inspiring papers:
 - Agol et al. 2005
 - Holman & Murray 2005
- A nice toolkit
 - Deck, Agol, Holman, Nesvorny 2014 (TTVFast)
- Largest batch analyses
 - Rowe et al. 2015
 - Holczer et al. 2016
 - Hadden & Lithwick 2017