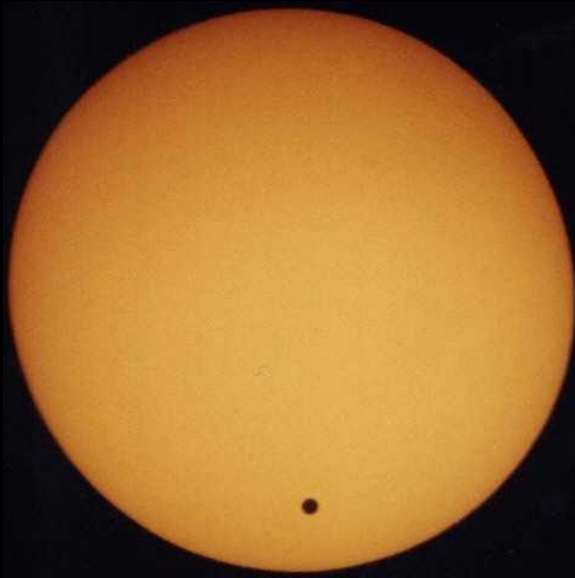
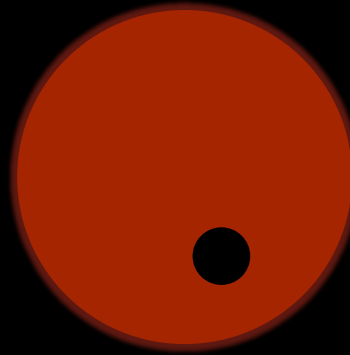


# Determining Physical Parameters of M Dwarf Planet-Hosts



G2V  
[Sun]



M1V  
[Kepler 45/KOI 254]



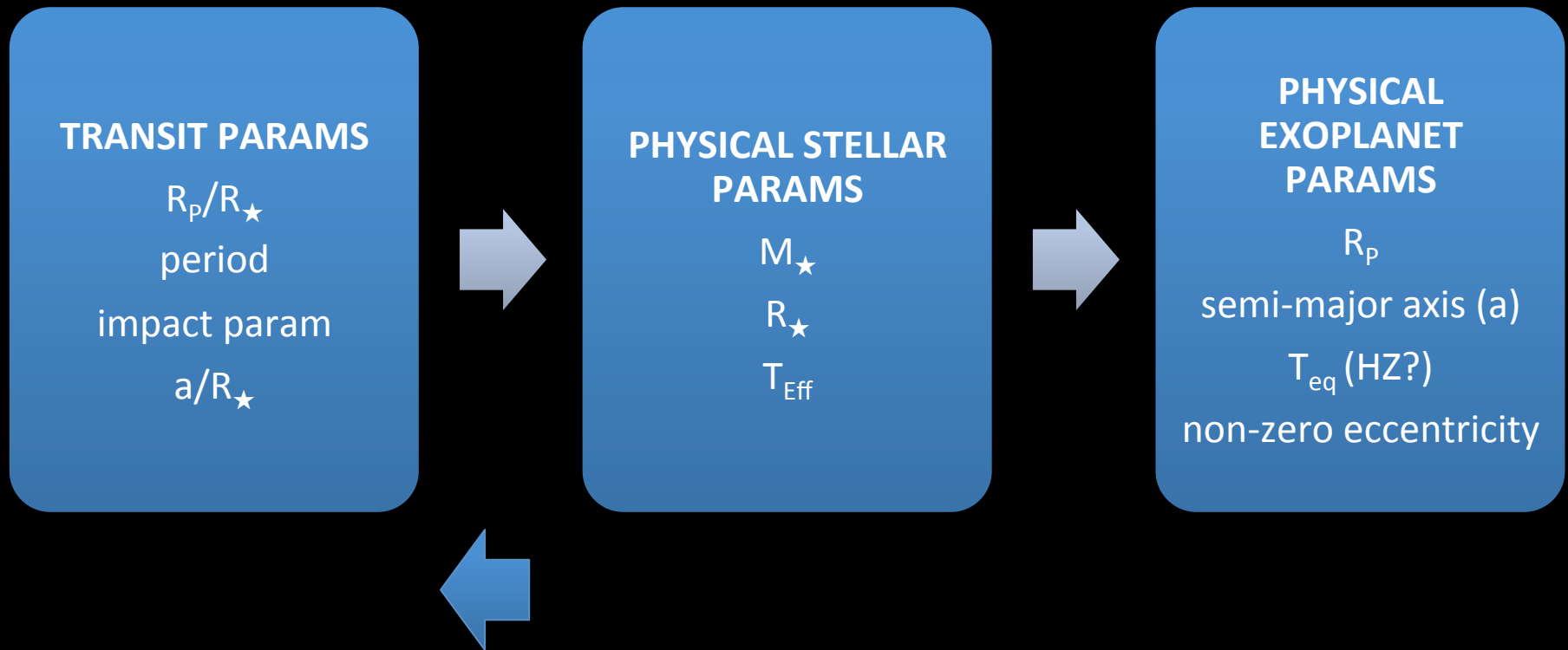
M4V  
[Kepler 42/KOI 961]



M8V  
[VB 10]

Phil Muirhead  
Caltech Postdoc

# Determining Physical Parameters of M Dwarf Planet-Hosts



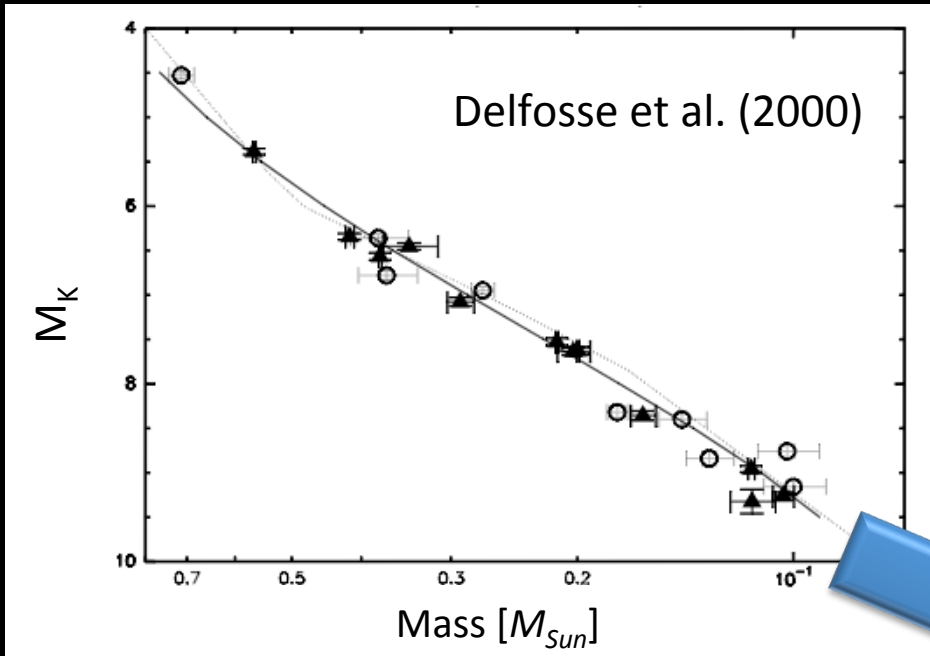
Can also use stellar params to constrain transit fit! Useful for multiple/low SNR transit light curves (J. Carter w/ KOI 961)

# Determining Physical Parameters of M Dwarf Planet-Hosts

Messy combination of:

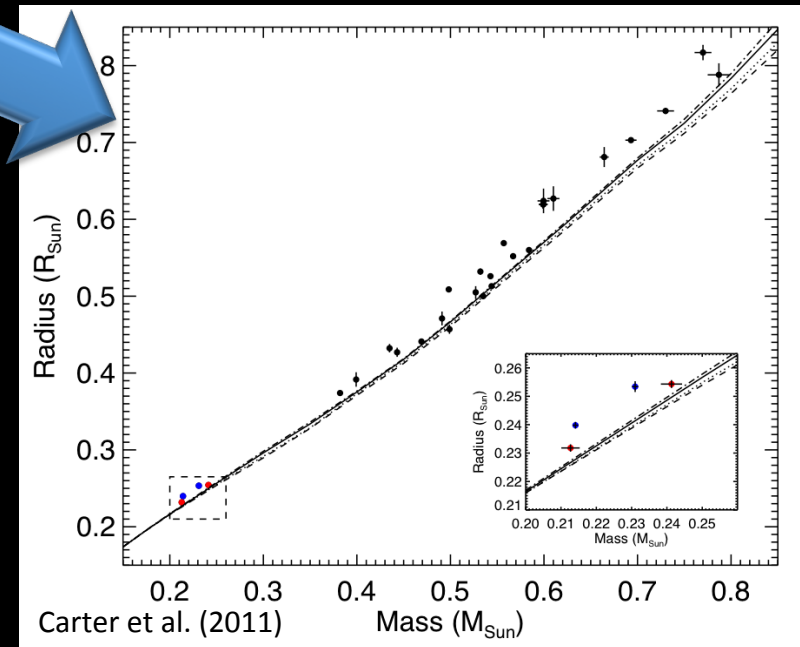
- **Empirical Measurements**
  - Luminosities from Parallaxes and Photometry
  - Masses from SB2 Binaries
  - Masses and Radii from Eclipsing SB2 Binaries
  - Metallicities from FGK + M Wide Binaries
  - Radii from Interferometry
  - Stellar densities from planet transits?
- **Evolutionary Models**
  - Predict M, R and L at a given age, metallicity
- **Atmospheric Models**
  - Predict spectra (and colors) at a given  $T_{\text{Eff}}$ , metallicity and  $\log g$

# The Canonical Method



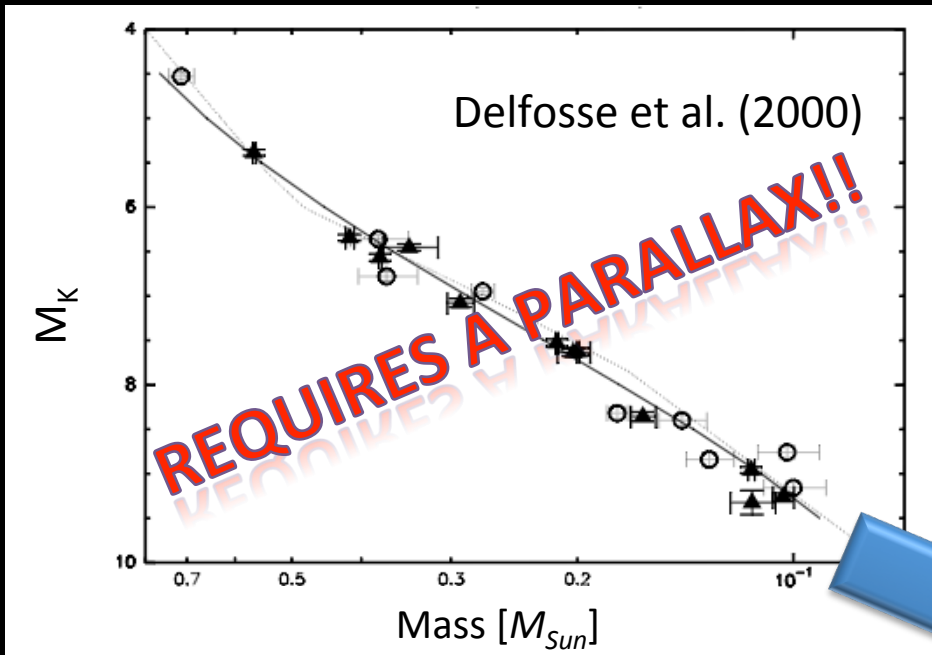
- **Mass-Luminosity Relation**
  - Calibrated on SB2s with parallaxes

- **Mass-Radius Relation**
  - Empirical from Eclipsing SB2s
    - e.g. Torres et al. (2010)
  - Or predictions from Evolutionary Models
    - e.g. Baraffe et al. (1998), Feiden et al. (2011)



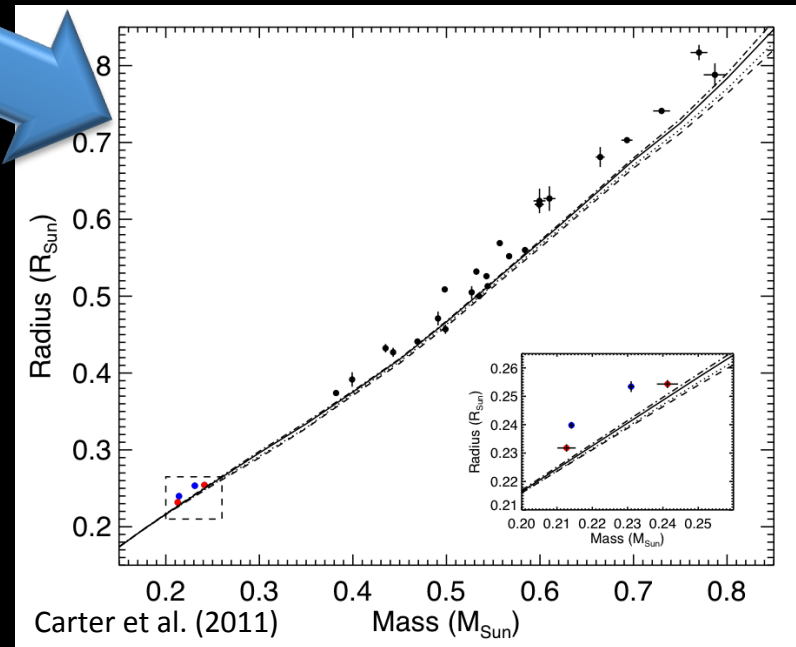


# The Canonical Method

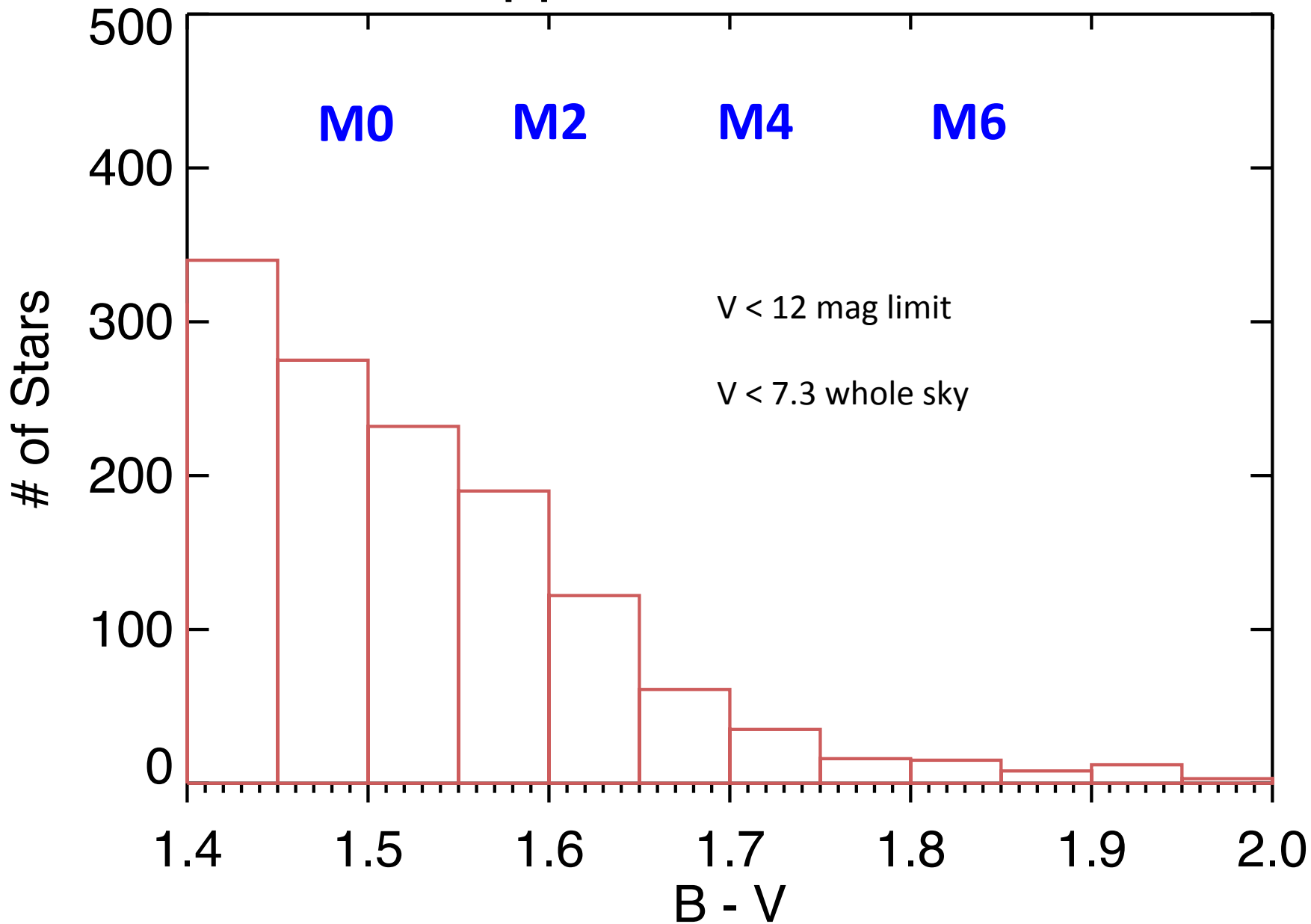


- Mass-Luminosity Relation
  - Calibrated on SB2s with parallaxes

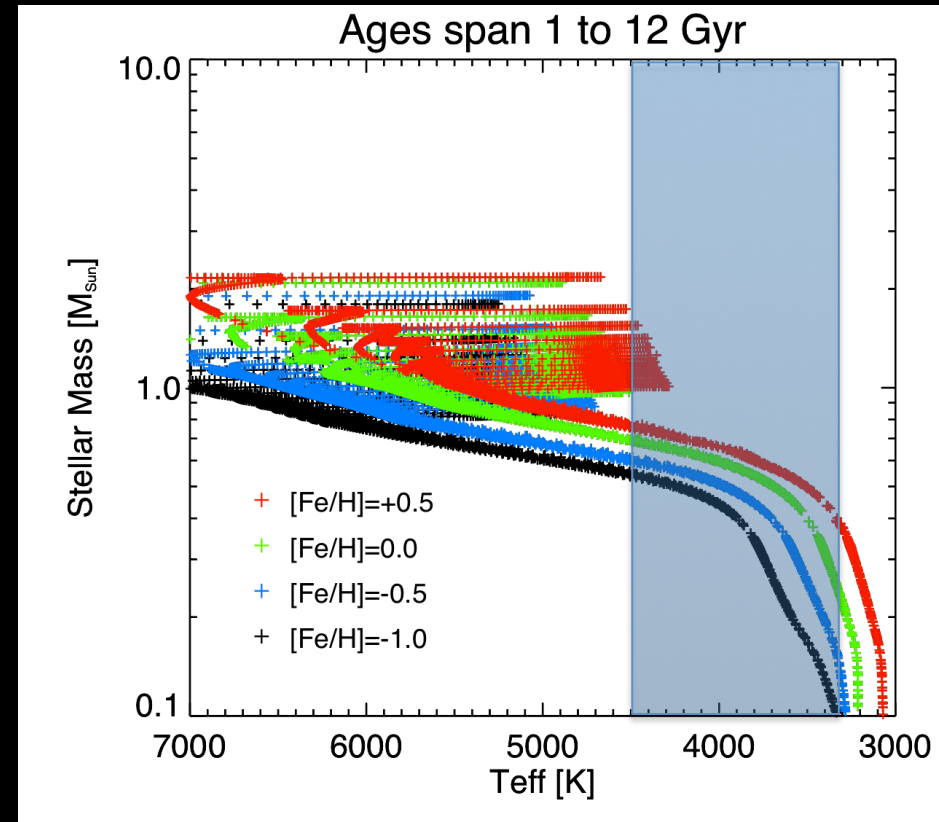
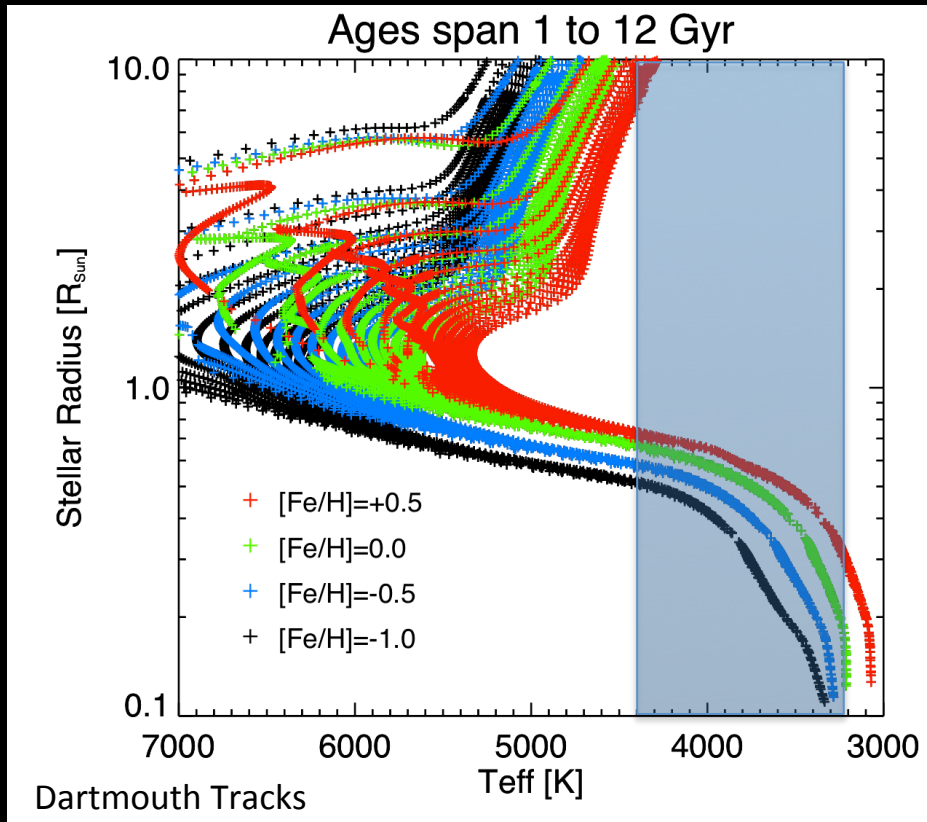
- Mass-Radius Relation
  - Empirical from Eclipsing SB2s
    - e.g. Torres et al. (2010)
  - Or predictions from Evolutionary Models
    - e.g. Baraffe et al. (1998), Feiden et al. (2011)



# Hipparcos M Dwarfs

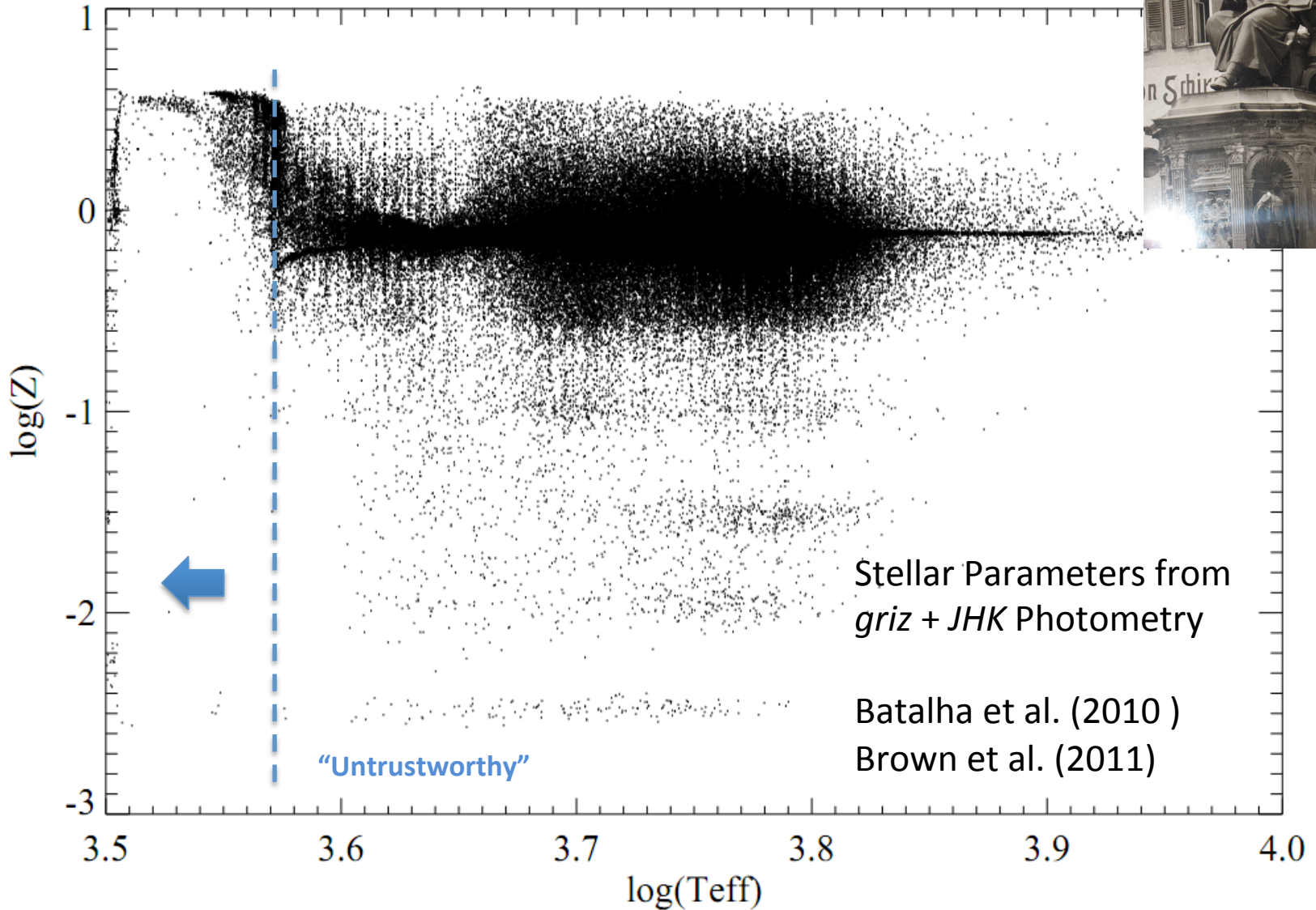


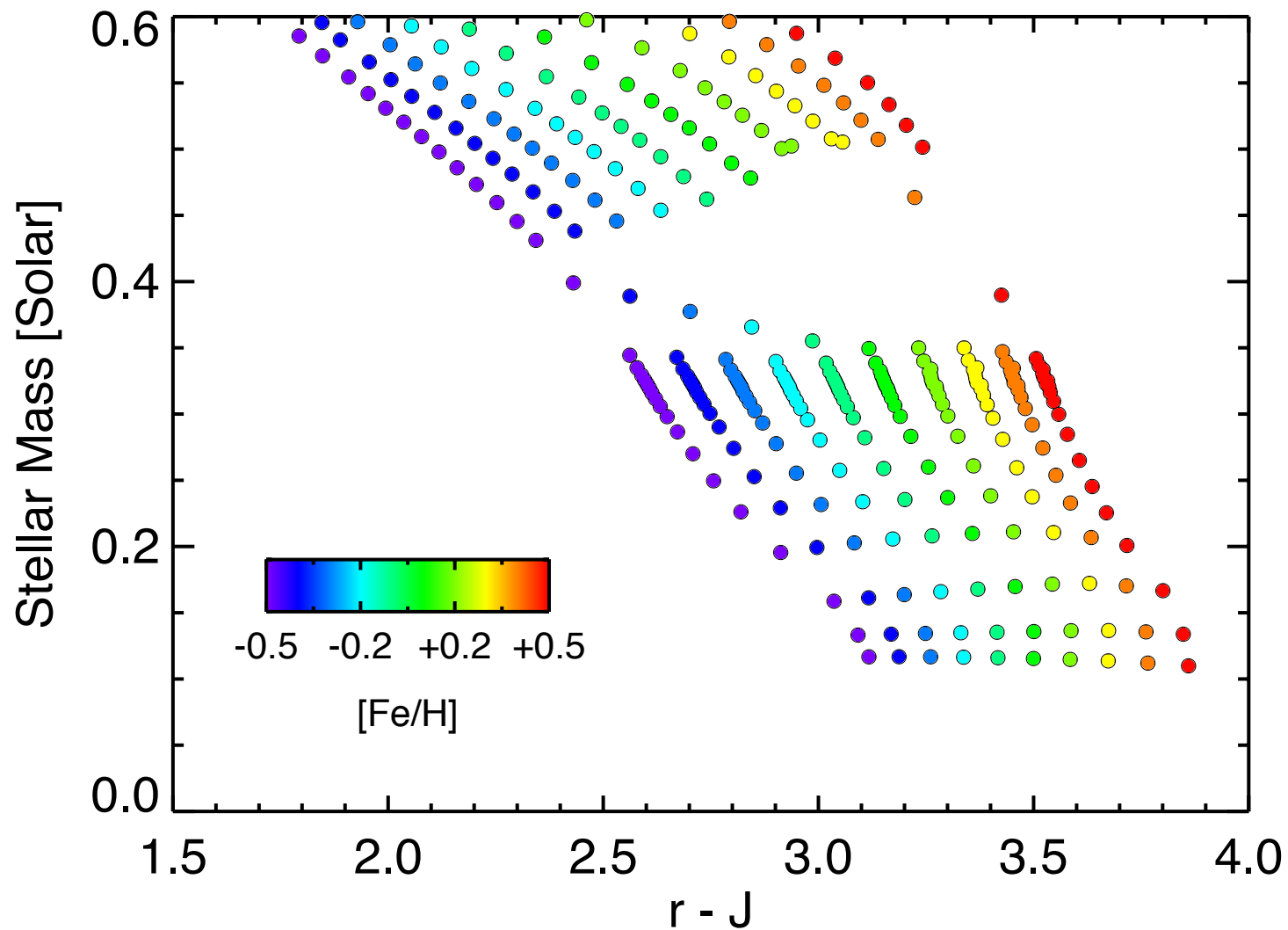
# M Dwarf Mass and Radius w/o Parallax

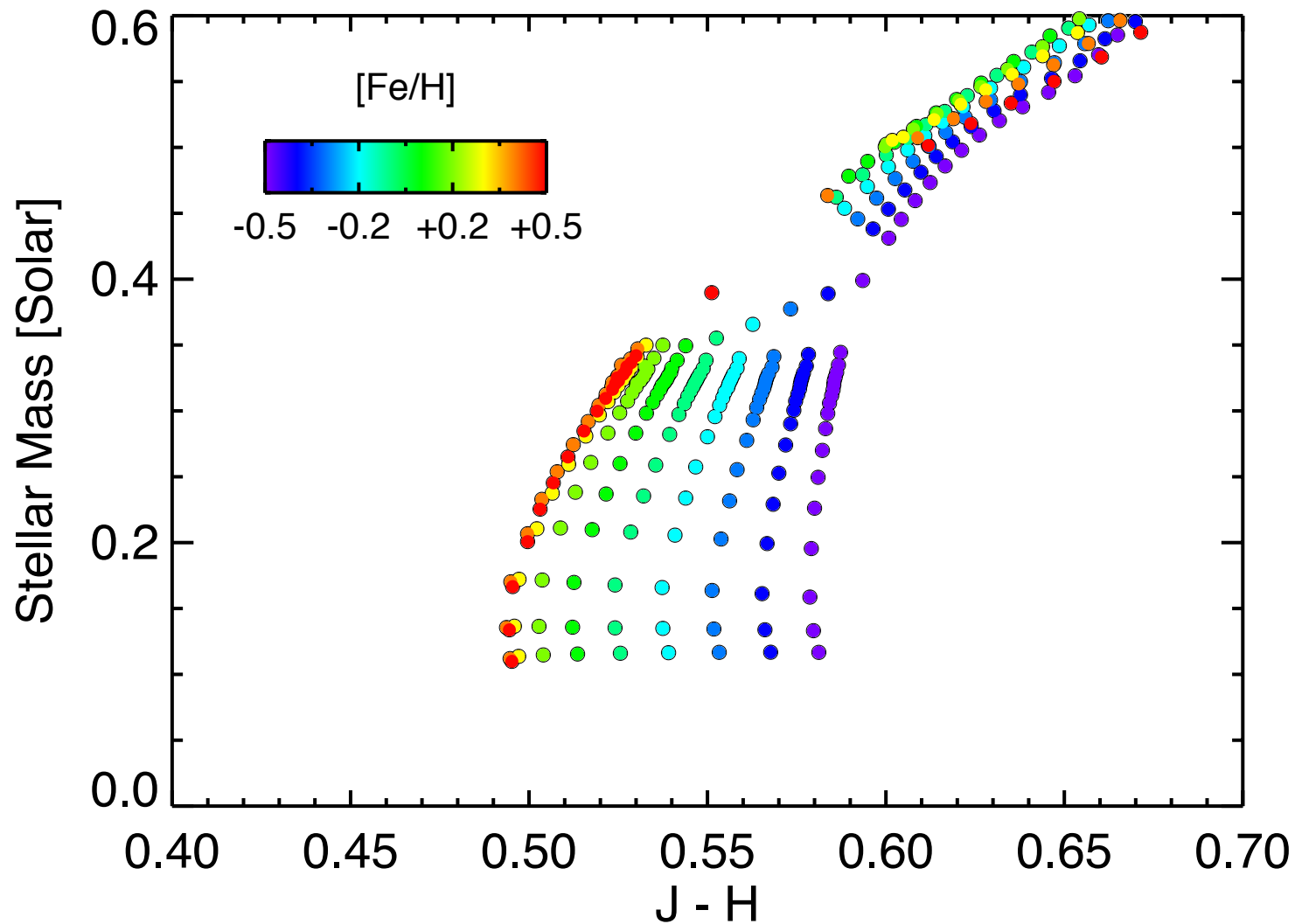


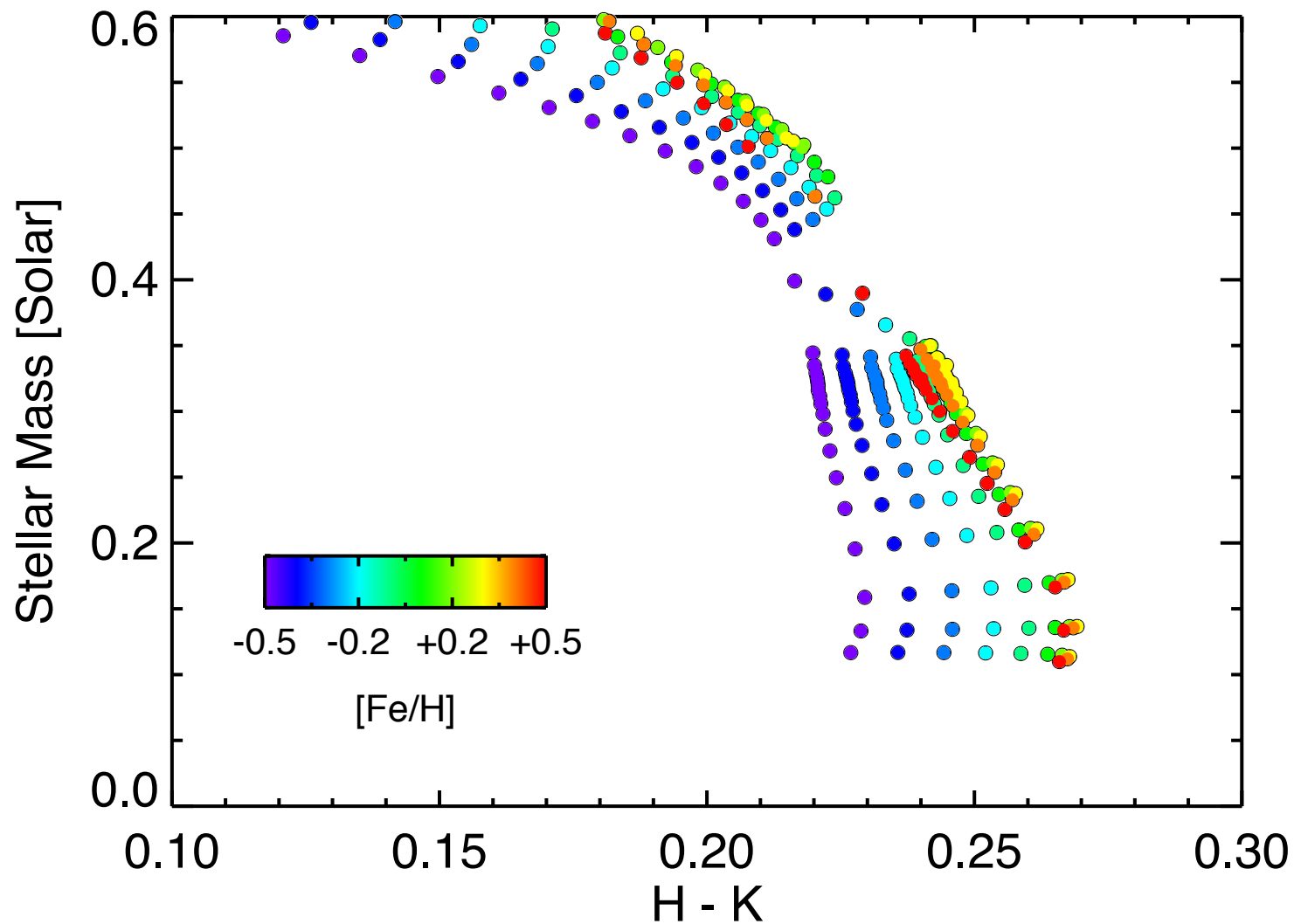
Burden falls on colors and spectra,  
which trace **effective temperature** and **metallicity**.

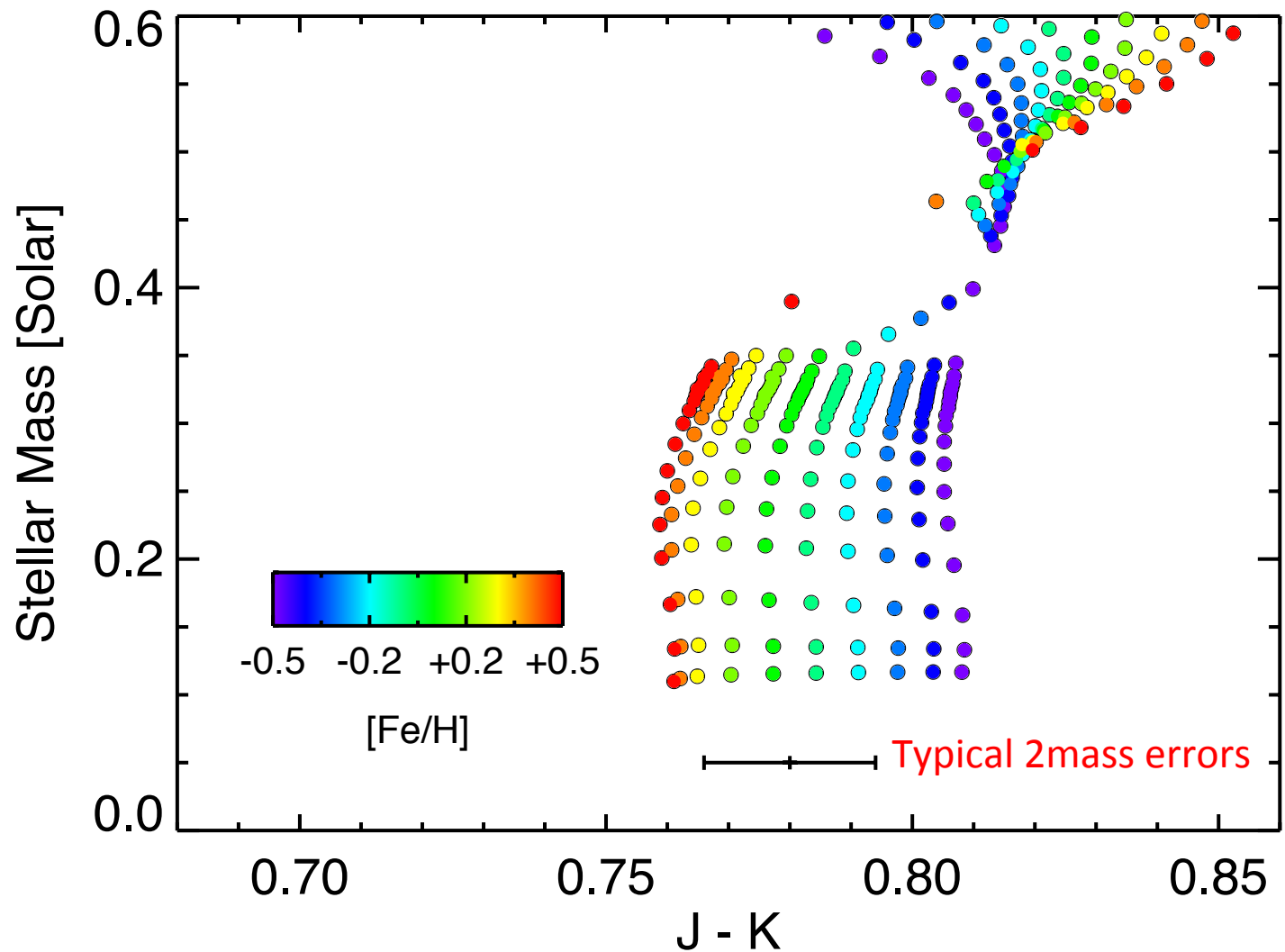
# Kepler Input Catalog



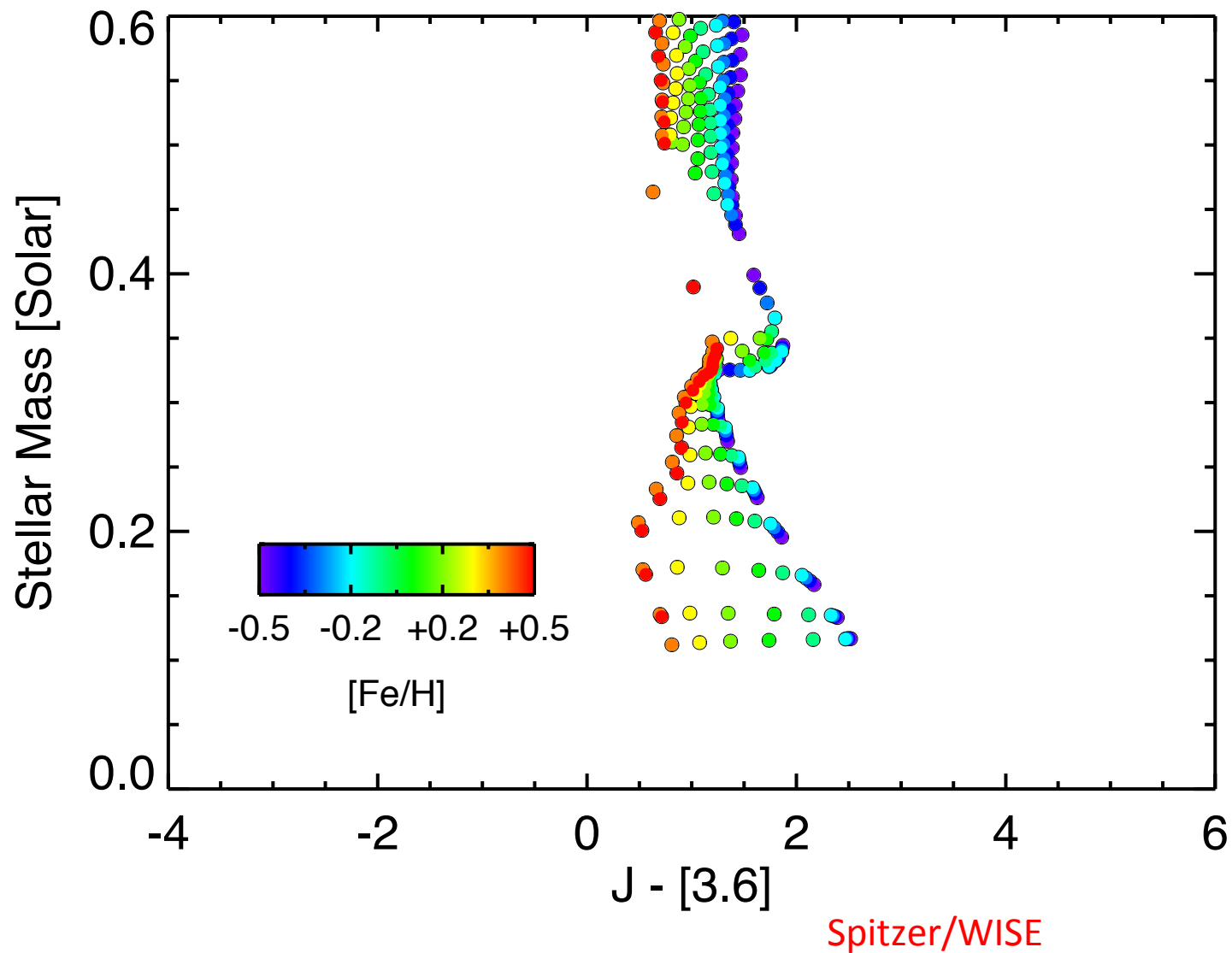


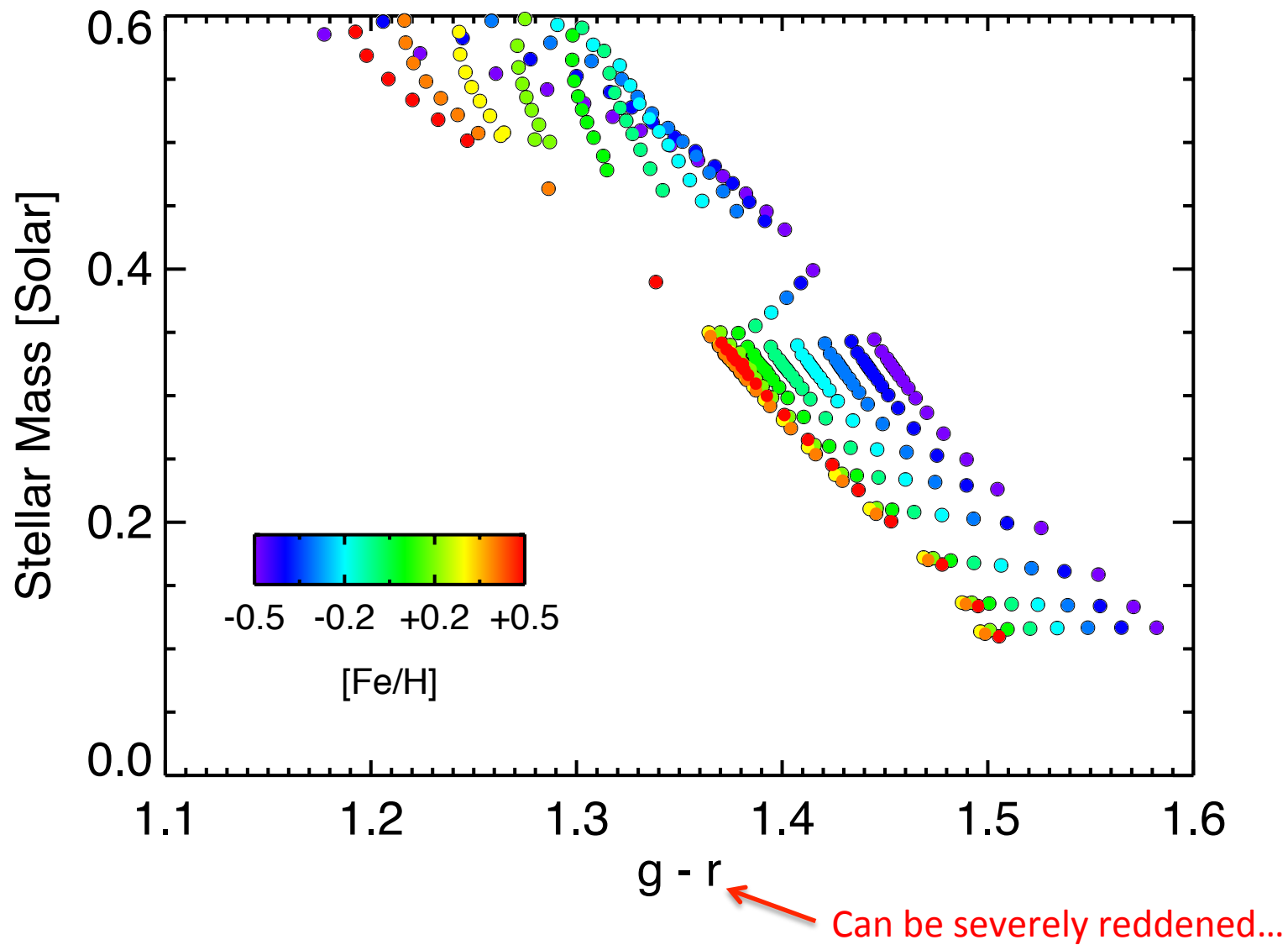








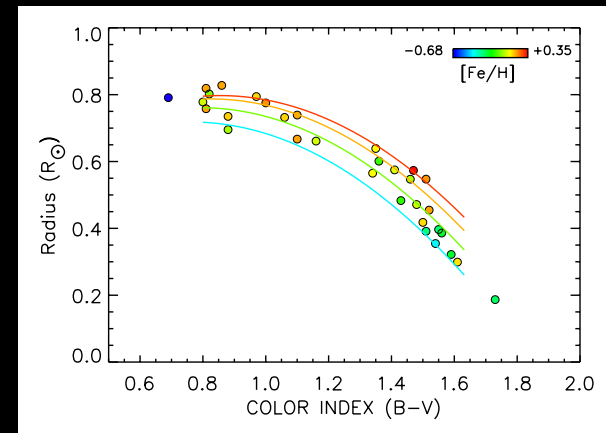




# M Dwarf Parameters from Photometric Colors Alone

- Extremely important for planet occurrence statistics
  - C. Dressing (CfA)
- Bayesian approach
  - Take everything you know, find the most likely values given the data
  - Johnson et al. 2011, 2012
- Need more empirical measurements!
  - More SB2s, EBs
  - Interferometric Radii
    - Boyajian et al. (2012)

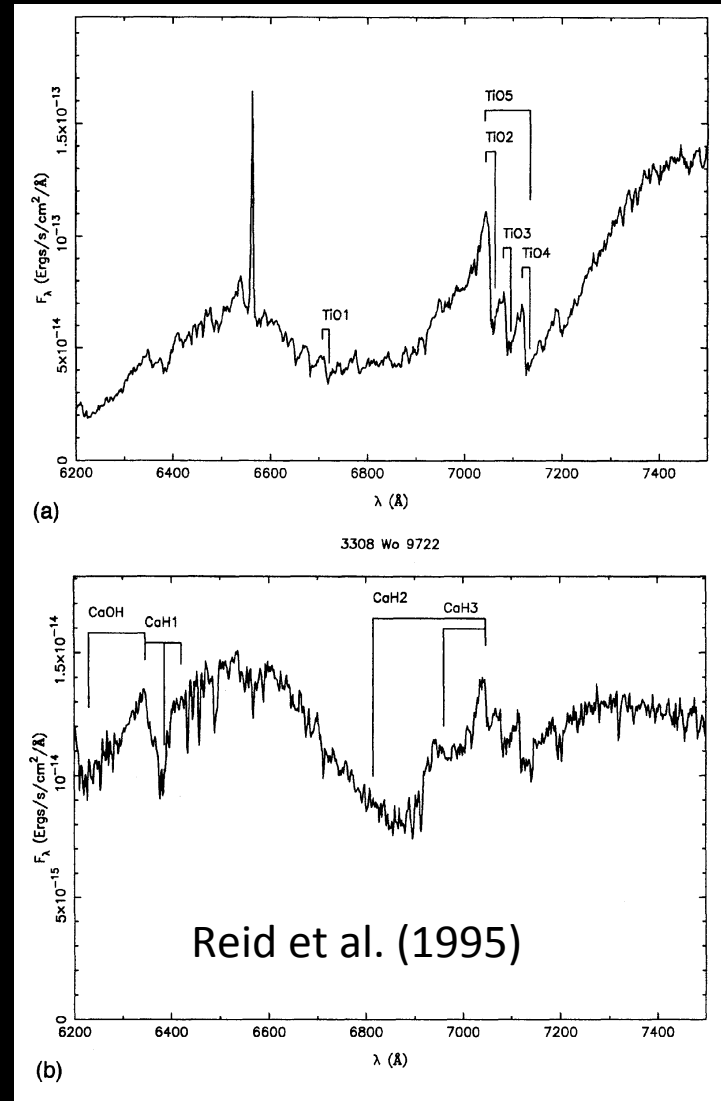
$$\chi_{\text{tot}}^2 = \sum_{i=1}^3 \left( \frac{m_{i,A} - m_i(M_A, d)}{\sigma_{m_{i,A}}} \right)^2 + \sum_{i=1}^3 \left( \frac{m_{i,B} - m_i(M_B, d)}{\sigma_{m_{i,B}}} \right)^2 + \left( \frac{V_{\text{tot}} - V_{\text{tot}}(M_A, M_B, d, F)}{\sigma_{V_{\text{tot}}}} \right)^2 + \left( \frac{a_R - a_R(M_A, M_C, P)}{\sigma_{a_R}} \right)^2.$$



# Spectroscopy

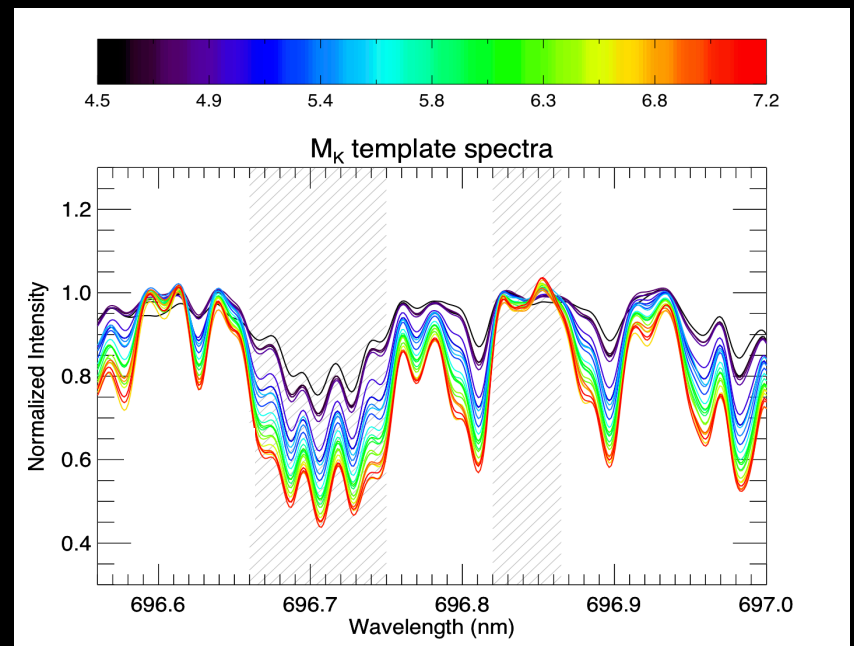
# Optical Spectroscopy

- **PMSU Survey**
  - Reid, Hawley and Gizis
- **Spectral Indices**
  - TiO, CaH, CaOH
  - Useful for spectral typing, determining luminosity class
  - Not well calibrated to physical  $T_{\text{Eff}}$  or  $[M/H]$ 
    - and therefore stellar mass and radius



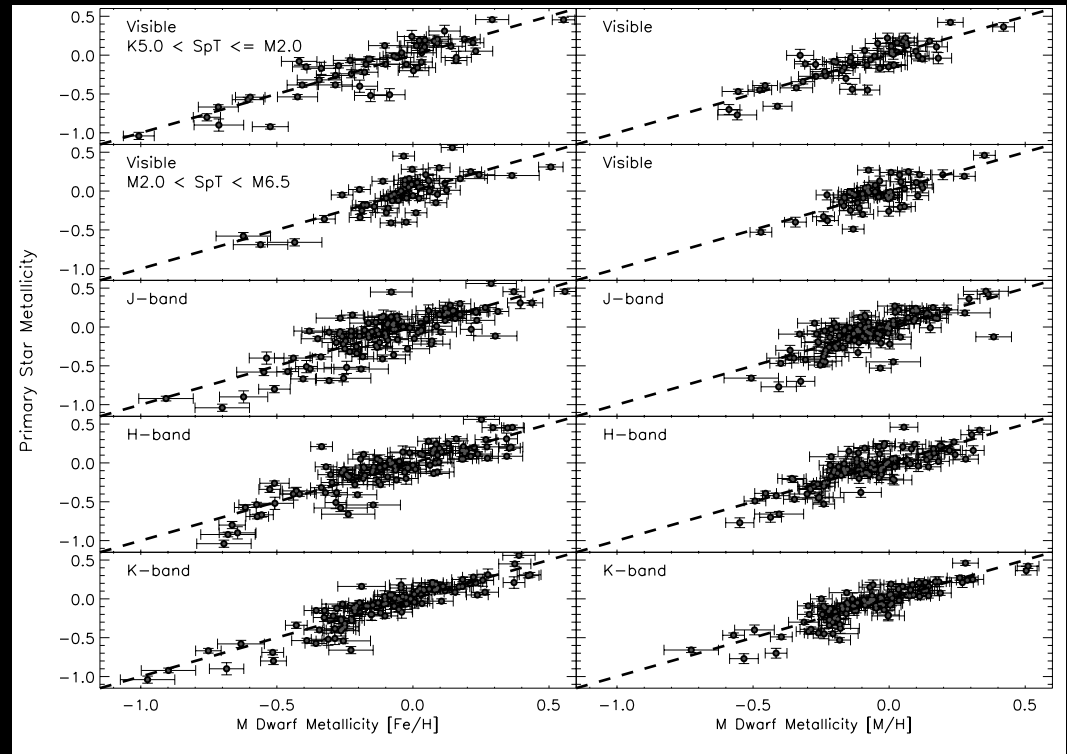
# Optical Spectroscopy

- New effort by **J. S. Pineda and M. Bottom (Caltech)**
- Archival HIRES M dwarf spectra from the California Planet Search
- Calibrate EWs to Delfosse et al. Stellar Mass

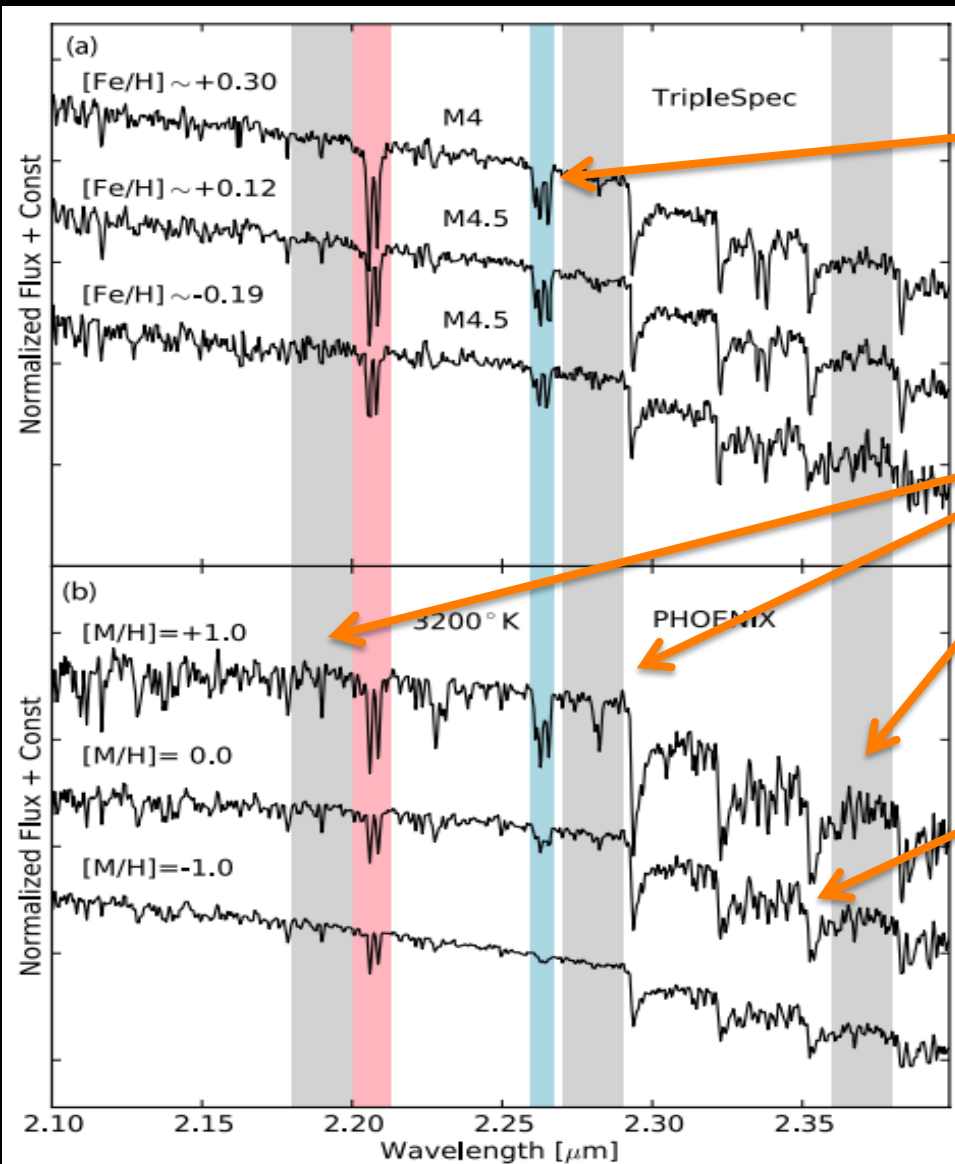


# Optical Spectroscopy

- New effort by **A. Mann (IfA)**
- Calibrate modern optical spectra to physical parameters



# K-Band Infrared Spectroscopy



Na and Ca EW trace  
 $[\text{Fe}/\text{H}]$ ,  $[\text{M}/\text{H}]$

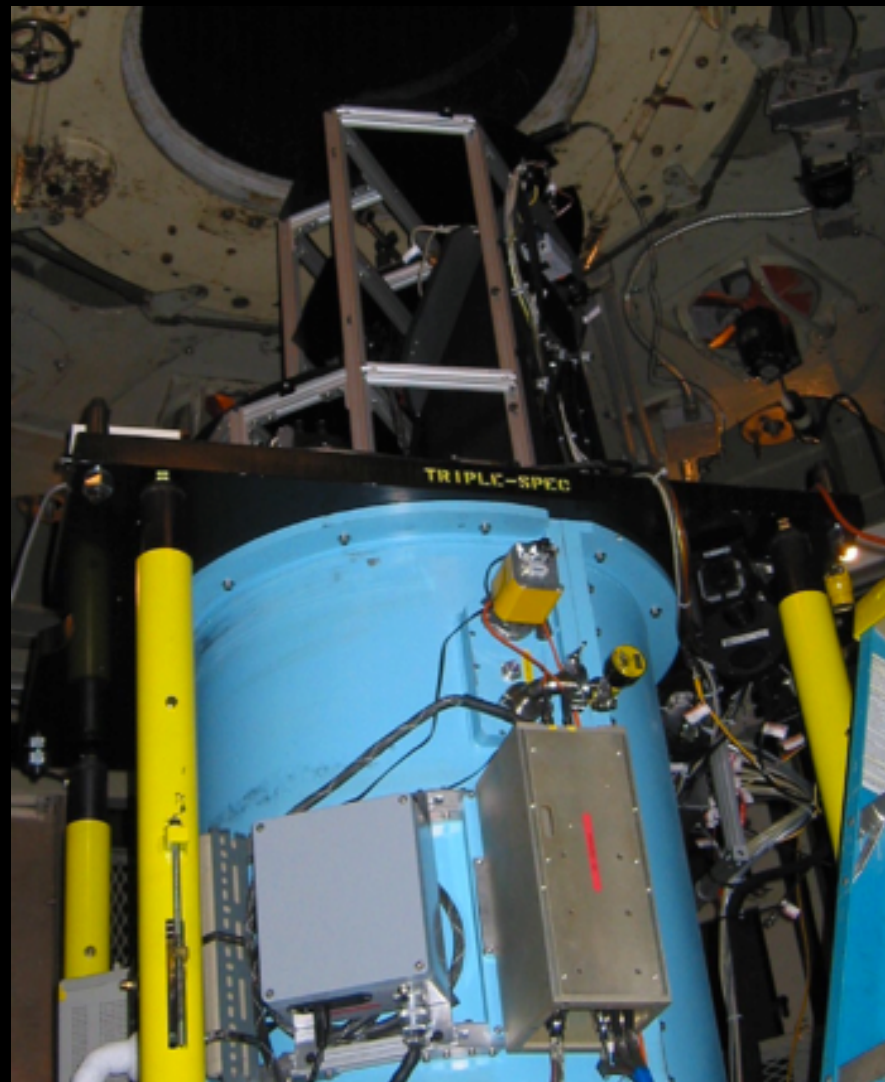
Deformation from  $\text{H}_2\text{O}$   
traces  $T_{\text{Eff}}$  ( $\text{H}_2\text{O-K}$  index)

CO EW determines  
luminosity class (V vs. III)

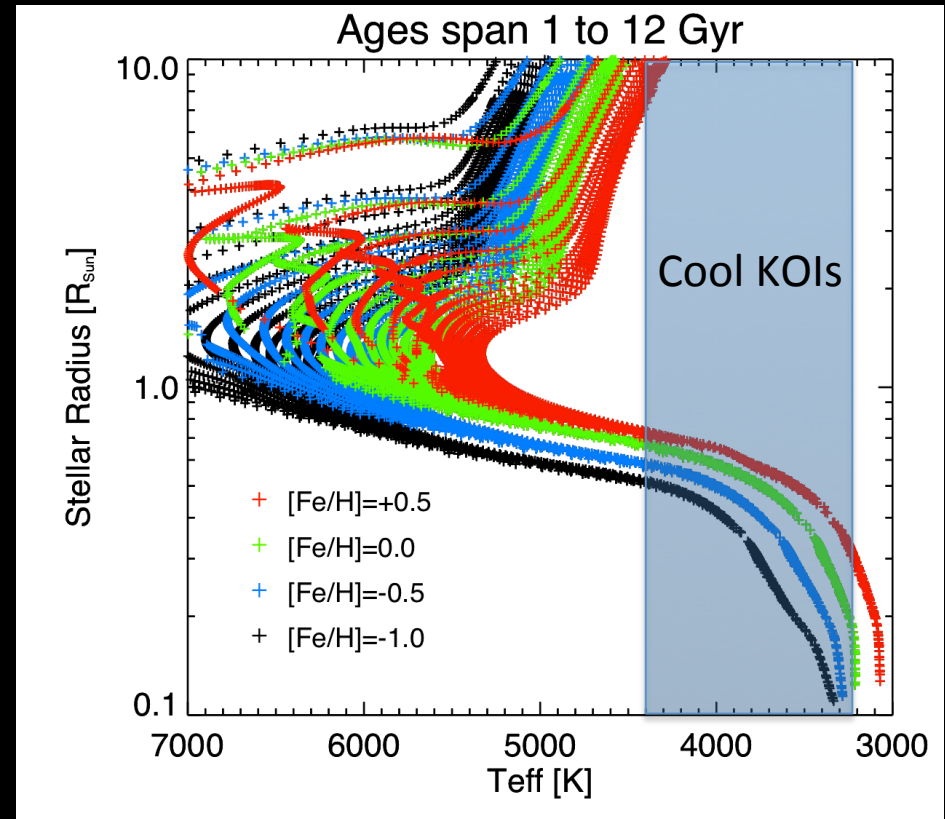
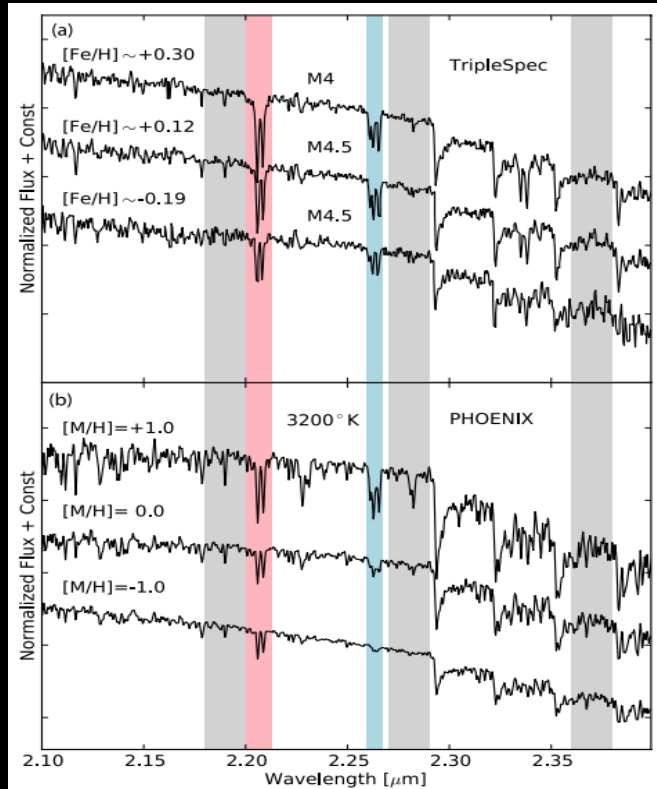
Rojas-Ayala et al.  
(2010, 2012)



# Palomar-TripleSpec



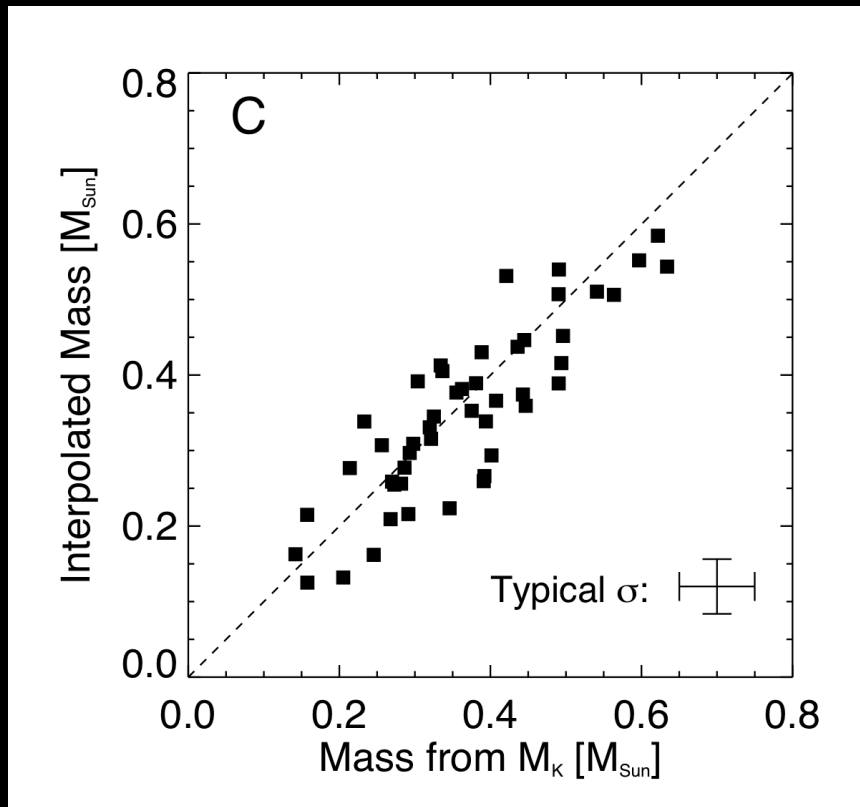
# Interpolate $T_{\text{eff}}$ and $[M/H]$ onto Dartmouth Isochrones for Mass and Radius



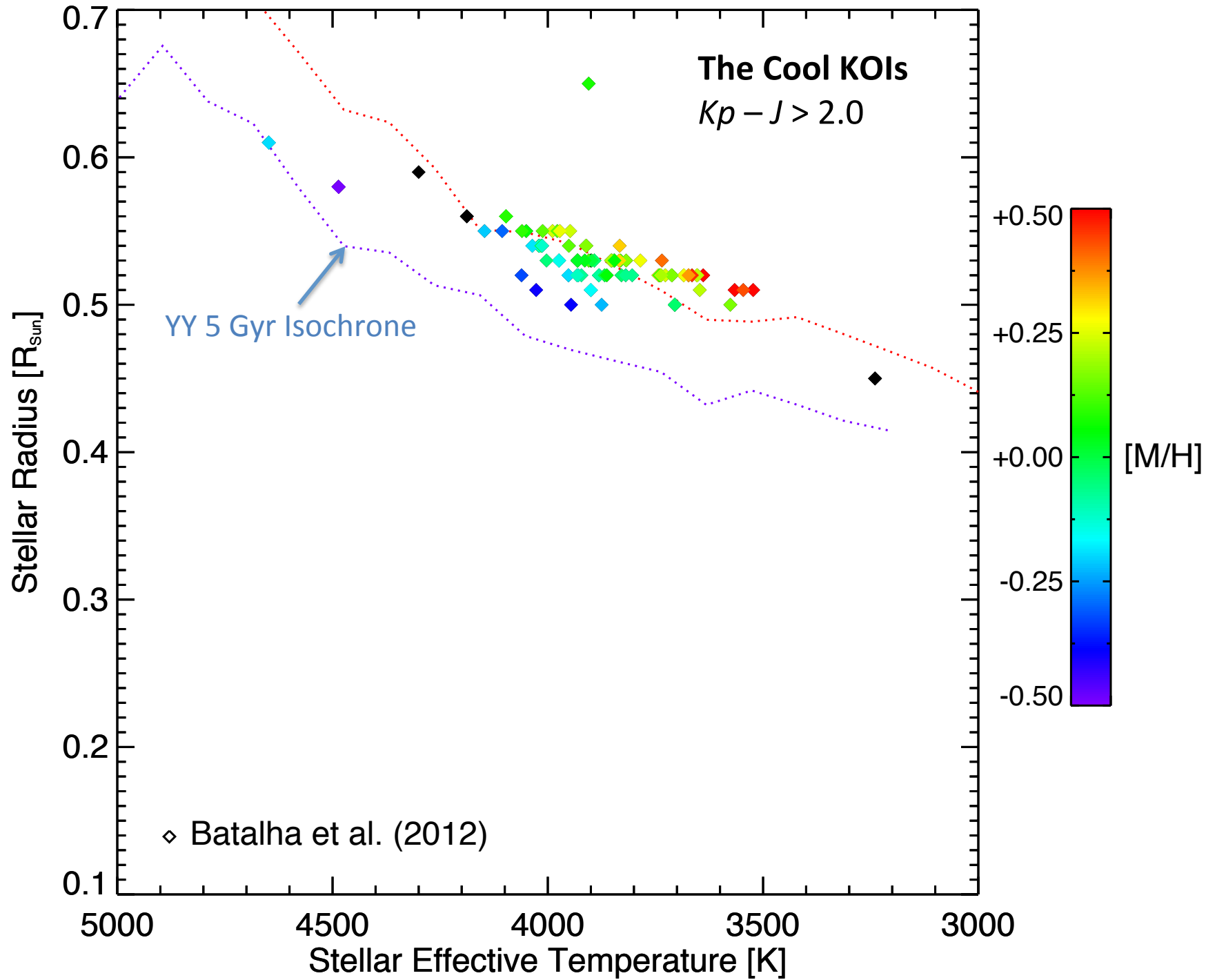
Rojas-Ayala et al. (2010, 2012)  
 $T_{\text{Eff}}$  and  $[M/H]$

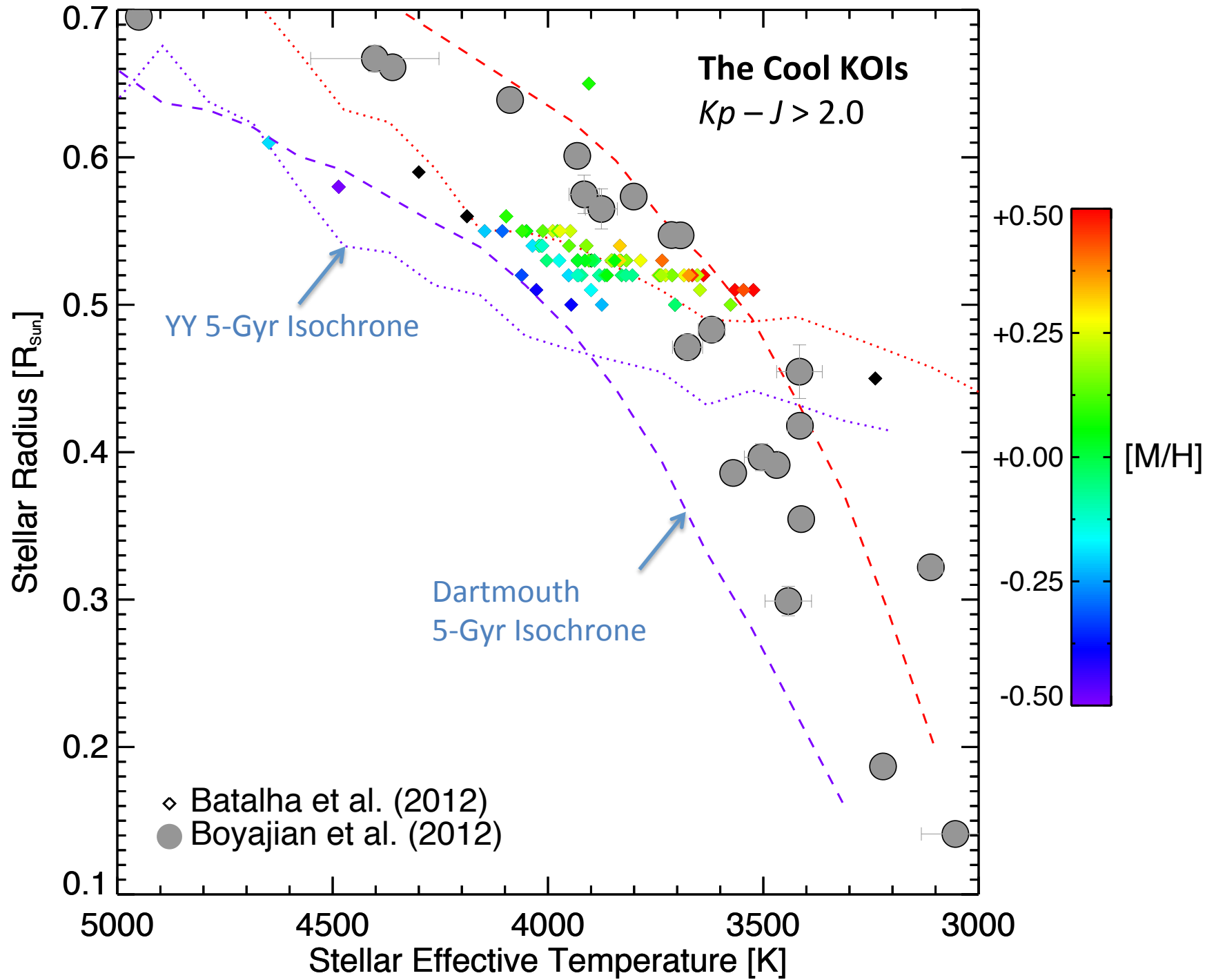
Dotter et al. (2008)  
 $M$ ,  $R$ ,  $L$ ,  $M_K$ , distance

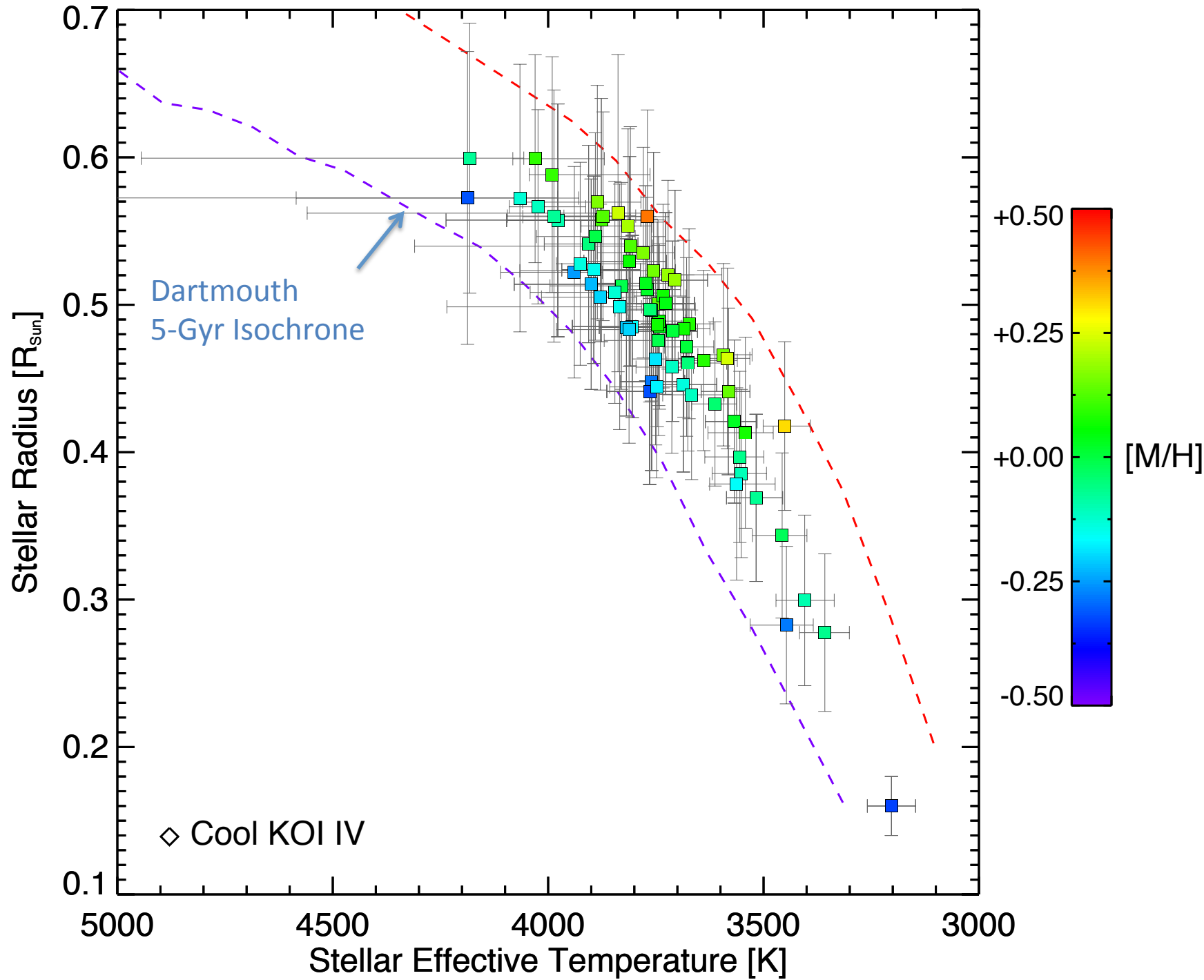
# Compare to Delfosse Masses

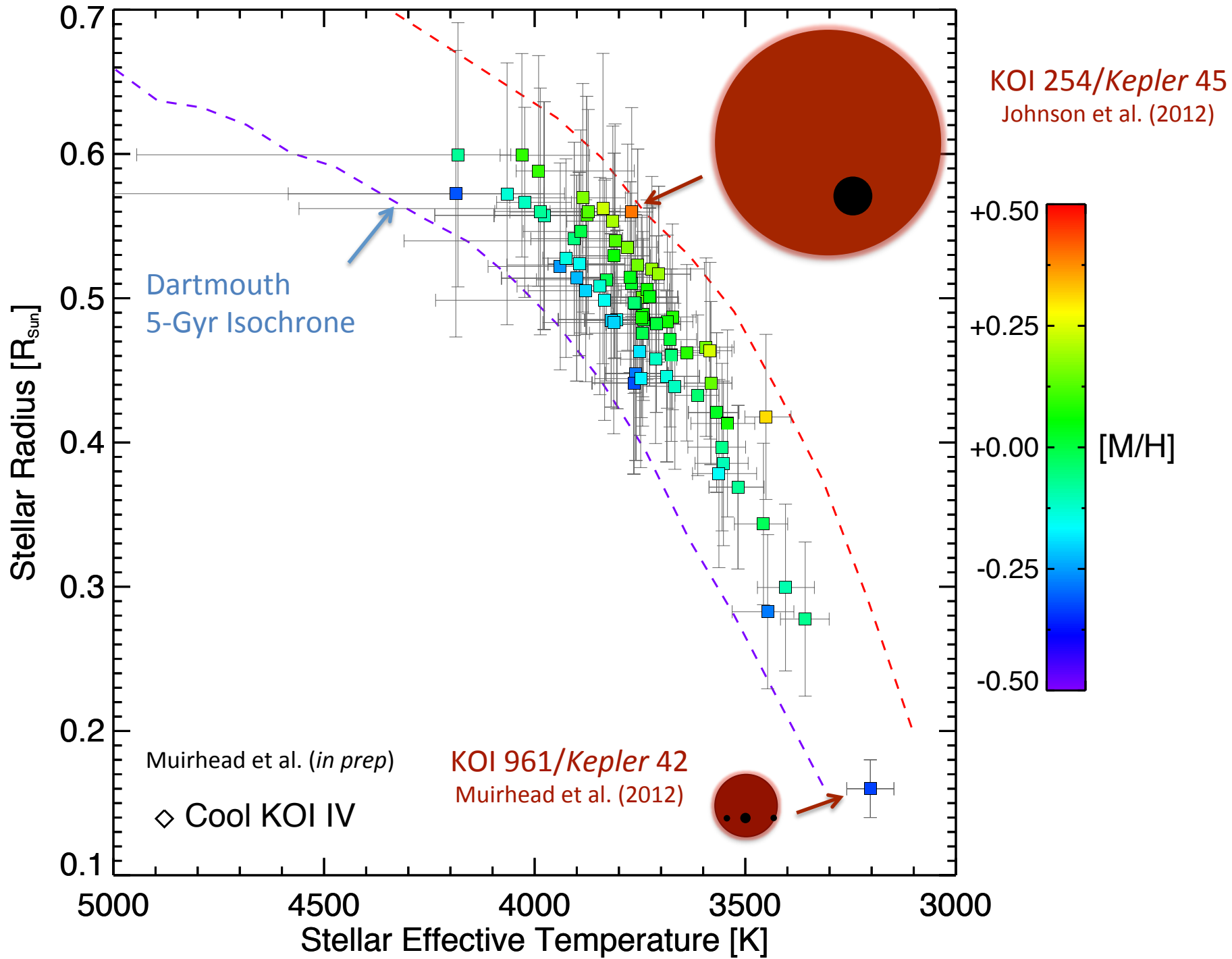


- Rojas-Ayala (2012) contains *K*-band spectra of 122 nearby M dwarfs.
- Compare interpolated mass to Delfosse et al. (2000) masses for stars with *Hipparcos* parallaxes.
- No systematic difference in mass estimates!



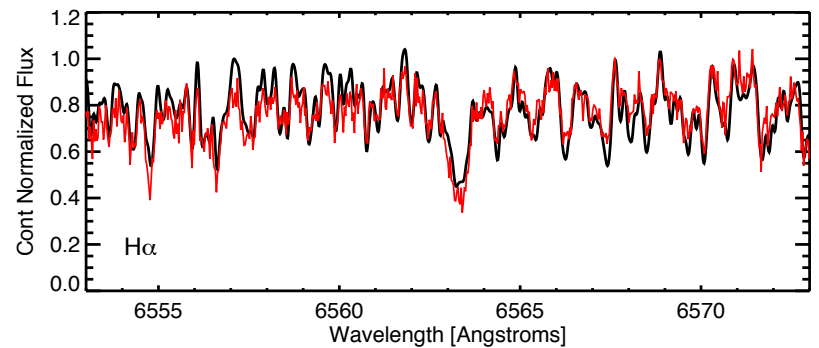
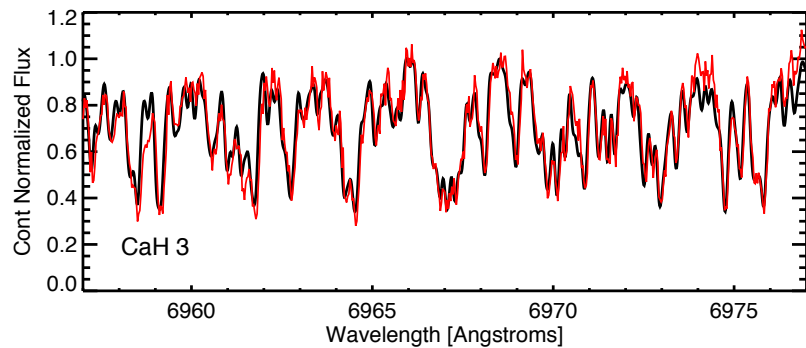
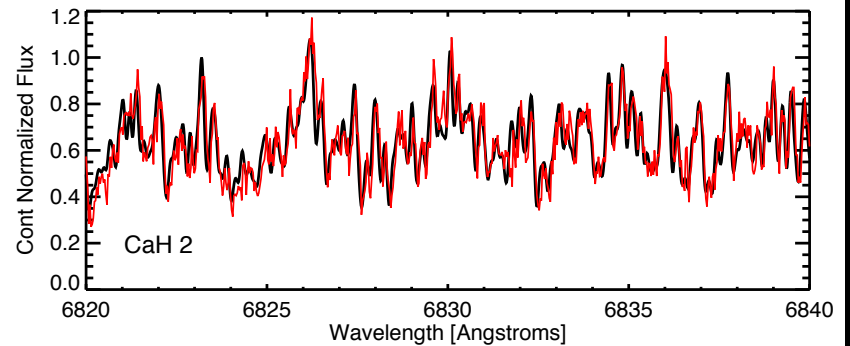
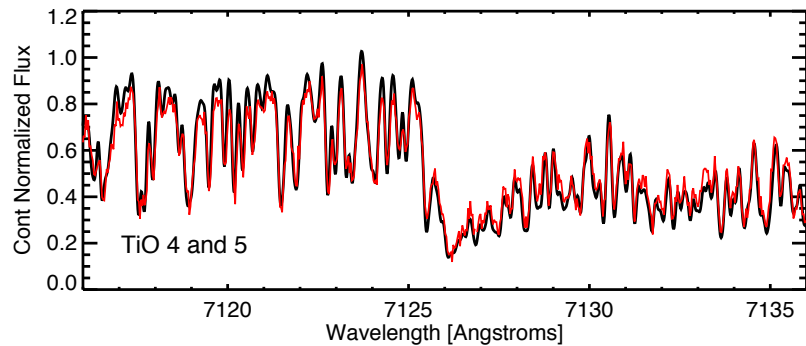
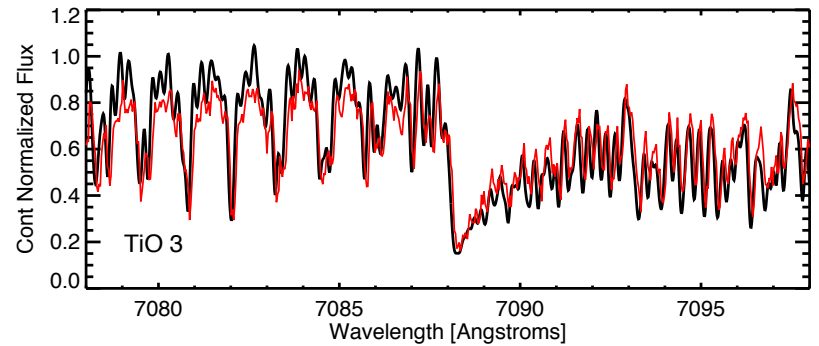
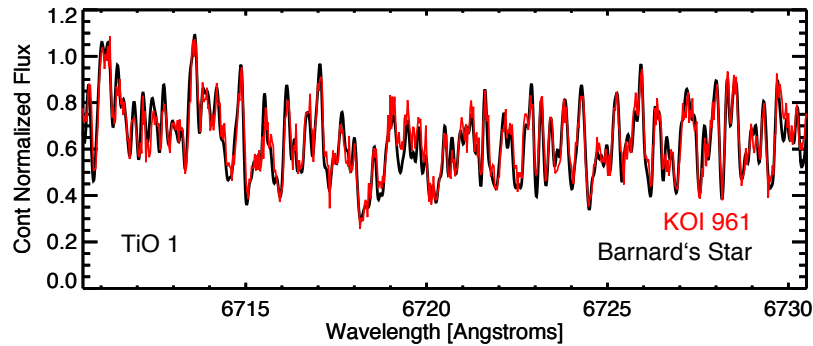








# KOI 961/Kepler 42 – Bootstrap off Barnard's Star



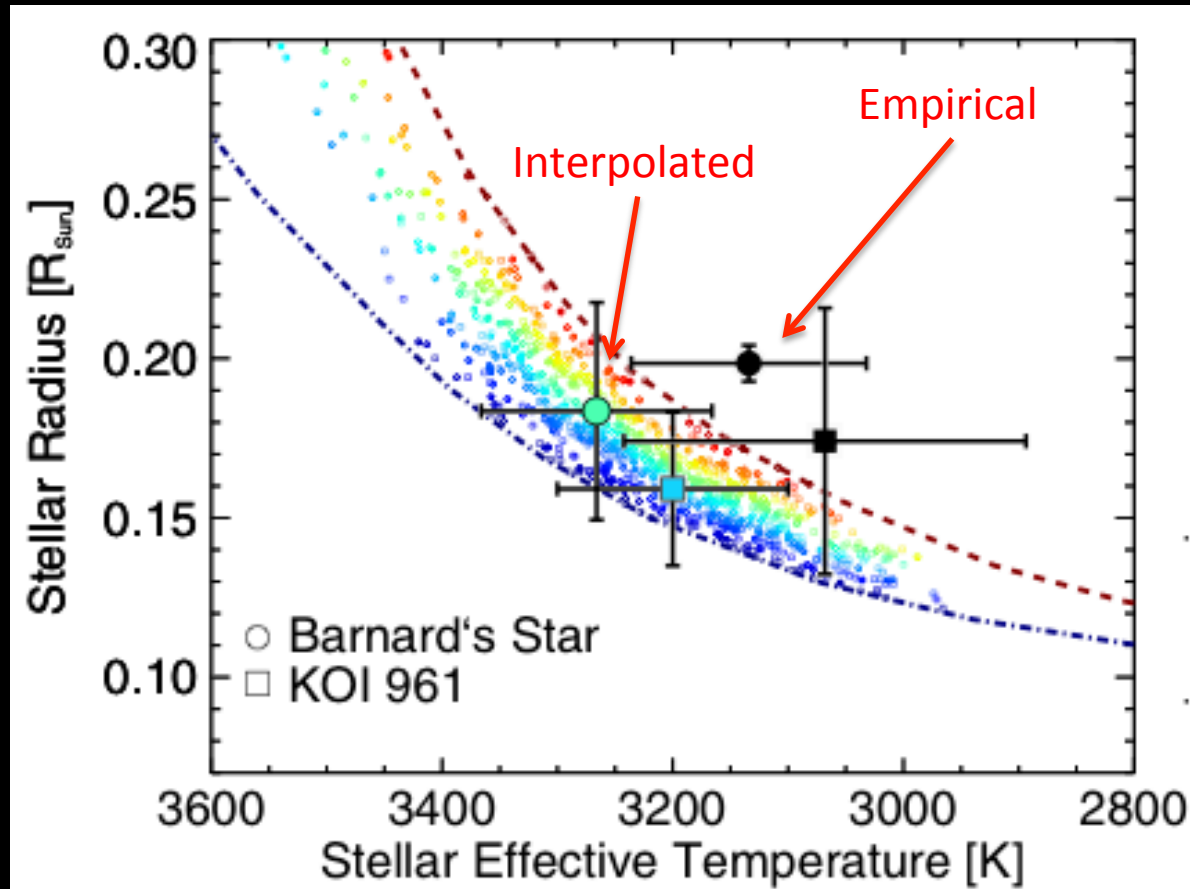


# Barnard's Star

## *A Small Star with Large Proper Motion* (Barnard 1916)

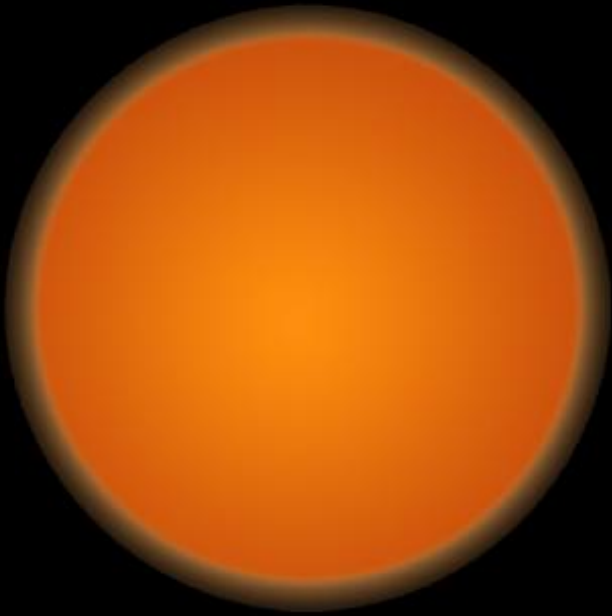
- Good *Hipparcos* parallax ( $d = 1.8$  pc)
  - Absolute magnitude  $\rightarrow$  Mass
- Old ( $> 7.5$  Gyr)
  - Slow rotator, no quiescent H-alpha emission, “Thick Disk” kinematics (Leggett 1992)
- Interferometric Radius! (Lane et al 2001, Boyajian et al. 2012)
- Carefully stitched spectra for bolometric luminosity (Dawson & de Robertis 2004)
  - With radius gives *empirical*  $T_{\text{eff}}$

# KOI 961/Kepler 42 – Bootstrap off Barnard's Star



- Also used bootstrap method on GJ 1214 to double-check.
- Recovered parameters based on *transit*  $a/R_*$  not models!!!
  - Method A from Carter et al. 2011

## KOI-961 and Its 3 Known Planets



02

01

03

## Jupiter and Its 4 Largest Moons



Io



Europa

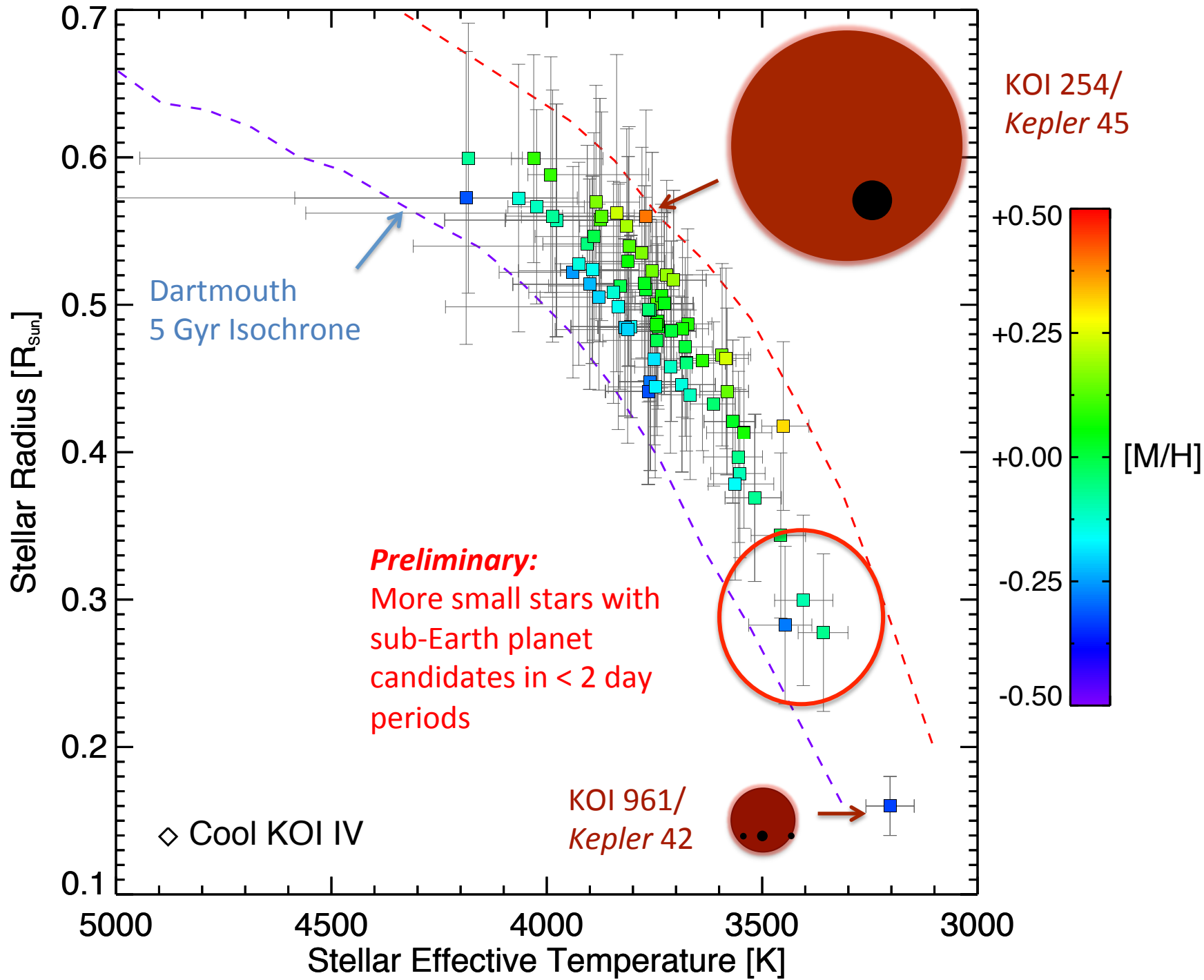


Ganymede

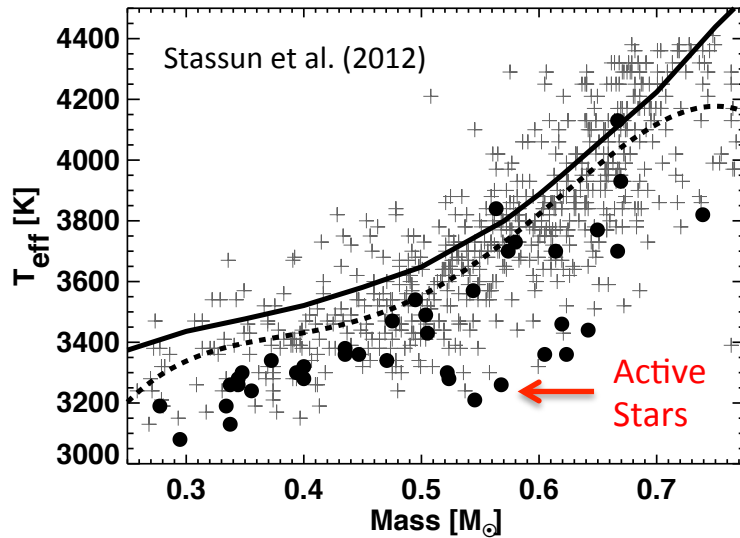


Callisto

**Orbital Scale = 5 x Size Scale**

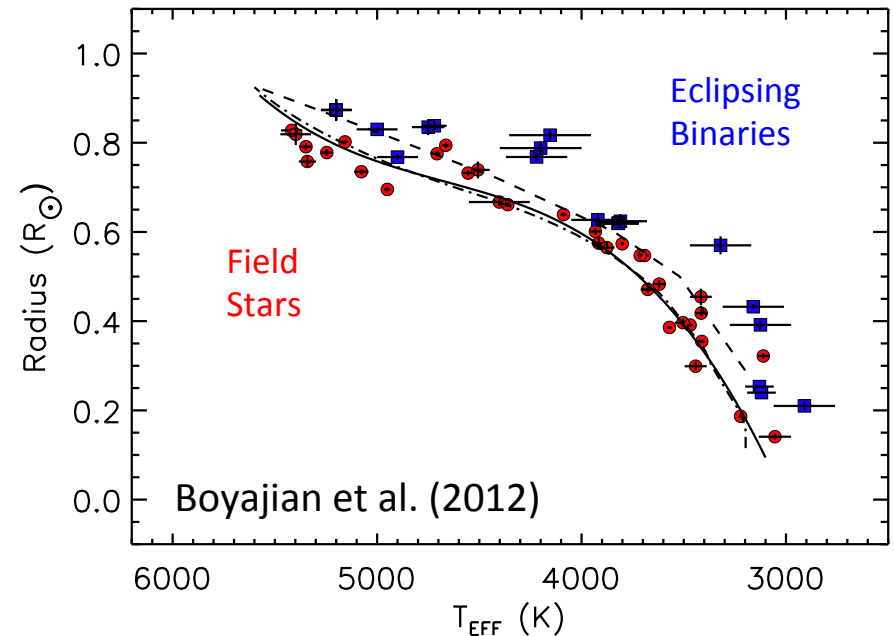


# Caveats/Research Problems



- How does activity change the connection between (Mass, Radius) and ( $T_{\text{eff}}$ , [M/H])?

- AKA: **What about magnetic fields!**



# More Research Problems

- Characterizing individual M dwarfs with exciting planets is fun...
- BUT we need physical parameters of ALL *Kepler* M dwarf targets for accurate statistics. Some possible approaches:
  - Spectra of all 3500 M dwarf targets?
    - Or a sub-sample, but how do you define it? Colors?
  - Better KIC color calibration to stellar mass and radius?
  - Parallaxes directly from *Kepler* data?
    - Few are willing to try. Crowd-source this for prize money?
  - Wait for *Gaia*... Launch next year!