

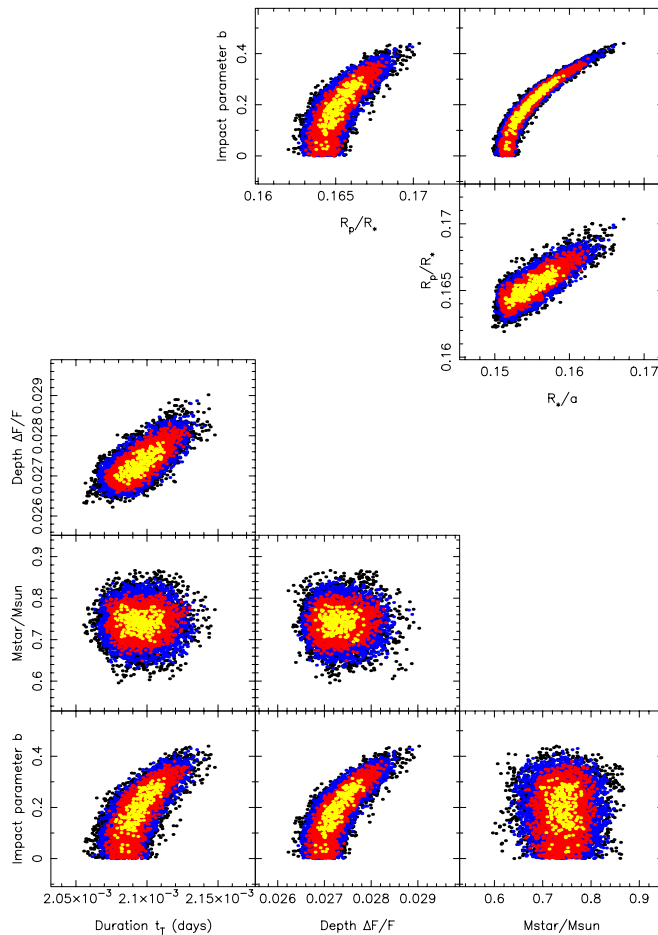
The Importance of Stellar Properties to Estimating Planet Characteristics

Andrew Collier Cameron
SUPA

School of Physics & Astronomy
University of St Andrews



Fundamental observables - transits

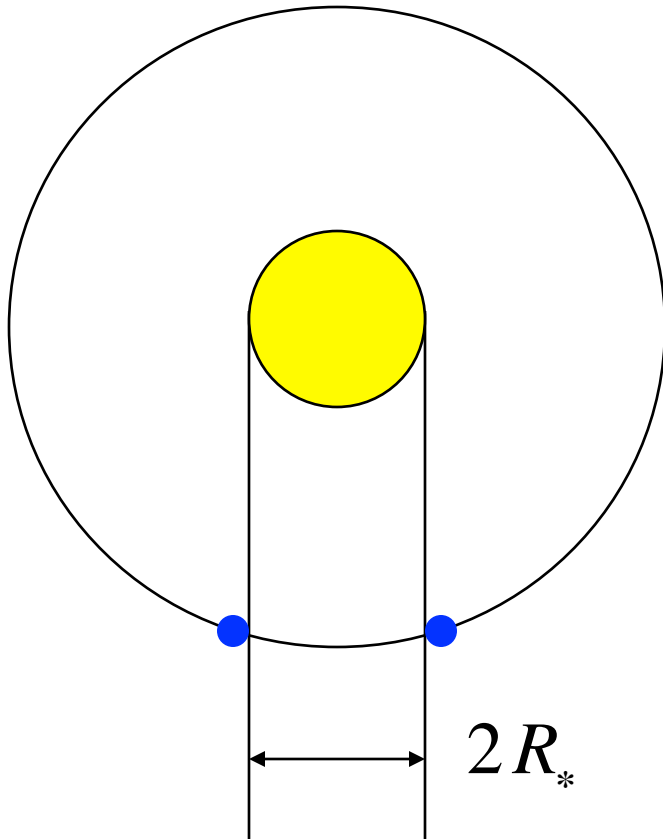


- Fundamental observables:
 - transit depth
 - transit duration
 - impact parameter
- Derived quantities:
 - R_p/R_*
 - R_*/a
- Need to know:
 - M_*
 - Limb darkening
 - cf. Jason Eastman's & Eric Agol's talks yesterday

Transit Duration ($i = 90^\circ$)

Consider circular edge-on orbit:

circumference = $2\pi a$



$$\frac{\Delta t}{P} \approx \frac{2(R_* + r_p)}{2\pi a} \approx \frac{R_*}{\pi a}$$

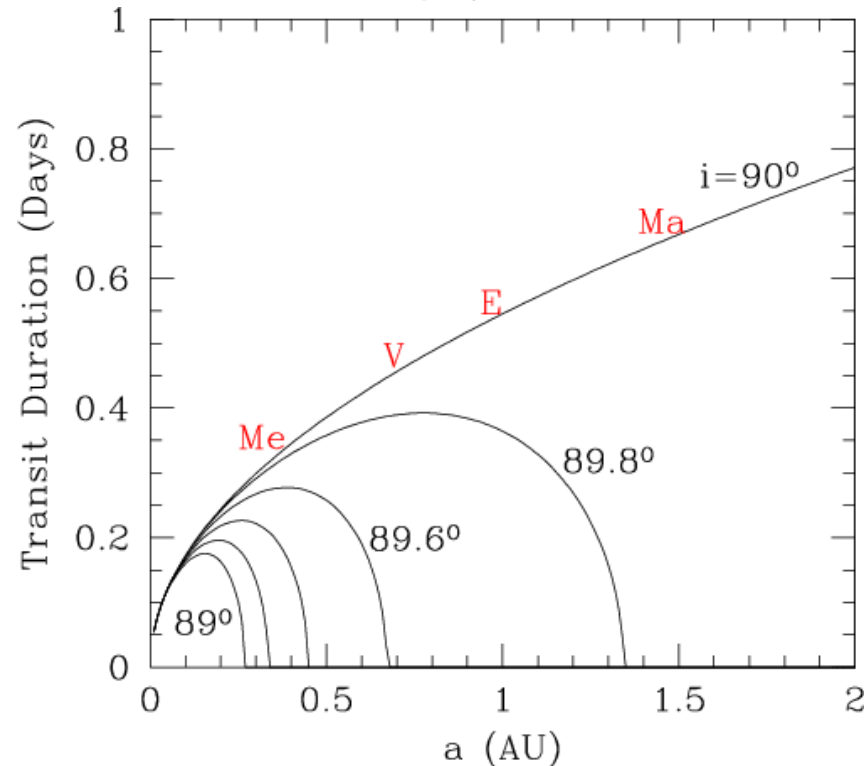
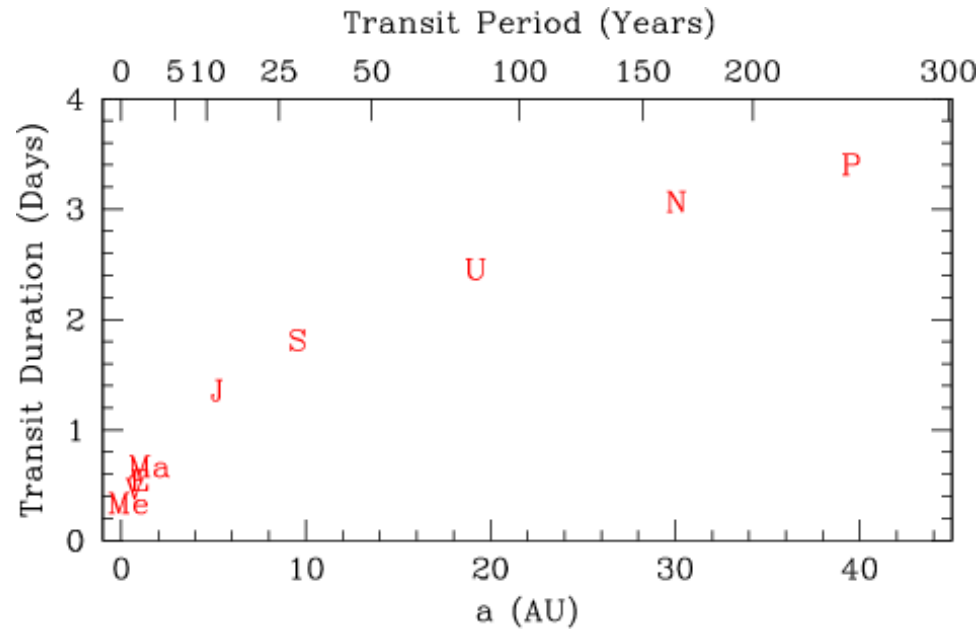
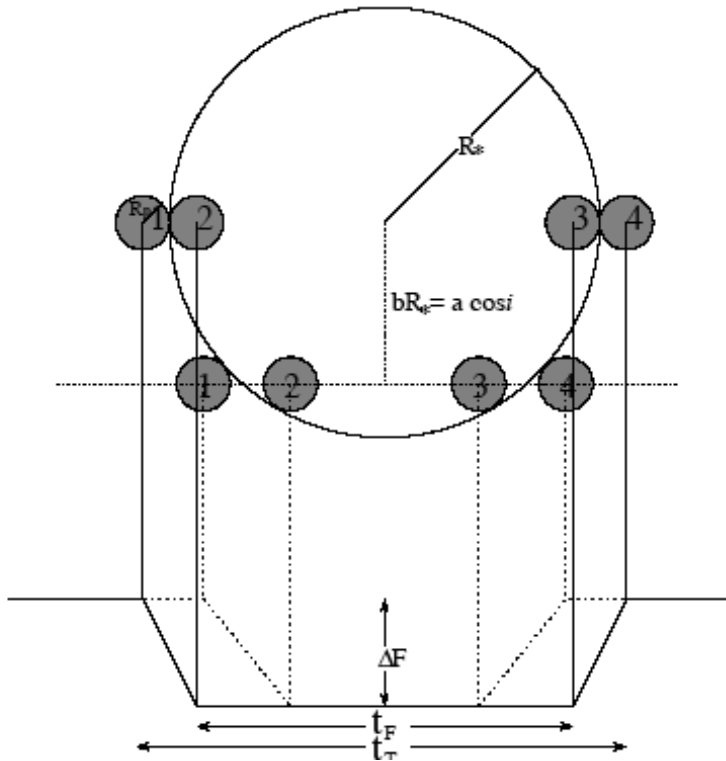
$$\text{Kepler's law : } a^3 = GM_* \left(\frac{P}{2\pi} \right)^2$$

$$\begin{aligned} \Delta t &\approx \frac{PR_*}{\pi a} = \frac{PR_*}{\pi} \left(\frac{4\pi^2}{GM P^2} \right)^{1/3} \\ &= 3h \left(\frac{P}{4d} \right)^{1/3} \left(\frac{R_*}{R_{Sun}} \right) \left(\frac{M_*}{M_{Sun}} \right)^{-1/3} \end{aligned}$$

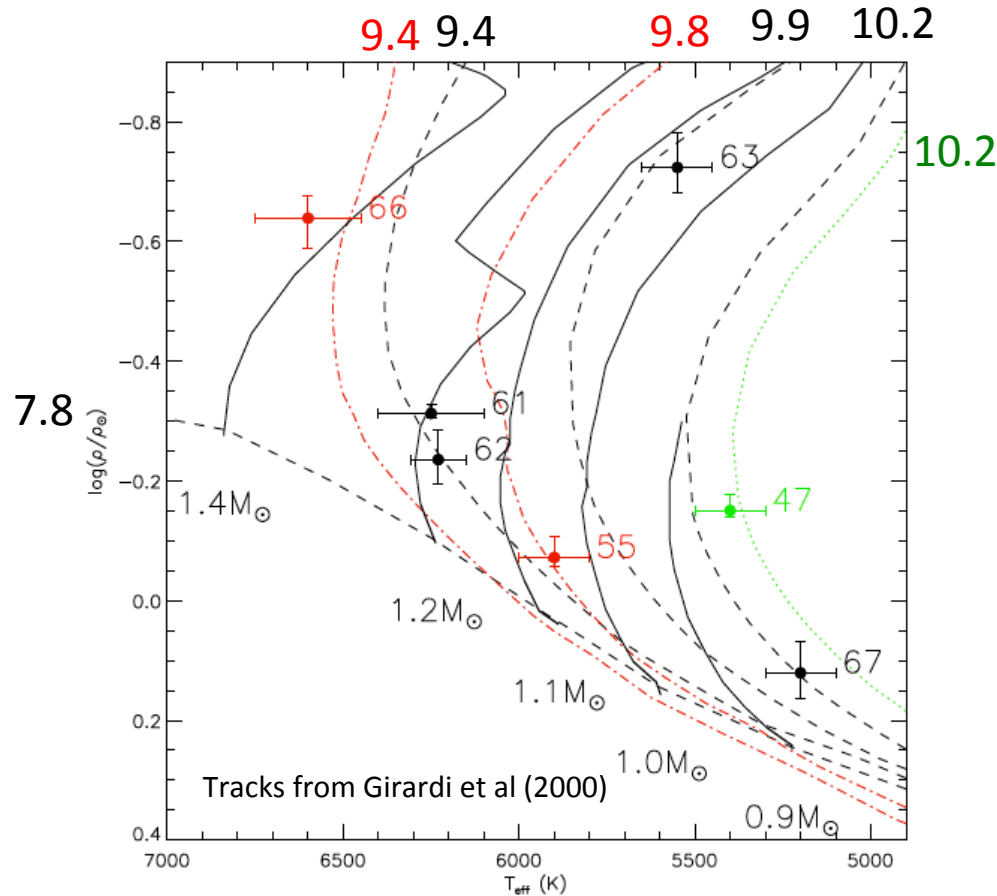
Transit Duration

$$t_T = \frac{PR_*}{\pi a} \sqrt{\left(1 + \frac{R_p}{R_*}\right)^2 - \left(\frac{a}{R_*} \cos i\right)^2}$$

Shape of lightcurve determines impact parameter, $b = a \cos i / R_*$ hence inclination.



The T_{eff} vs $\rho^{-1/3}$ HR diagram



[Fe/H]=+0.18, 0.0, -0.2

Hellier et al 2012, arXiv/1204.5095

- R_*/a is a direct measure of stellar density:

$$\left(\frac{R_*}{a}\right)^3 = \frac{3\pi}{GP^2} \frac{4\pi R_*^3}{3M_*}$$

$$\Rightarrow \frac{R_*}{a} = \left(\frac{3\pi}{G}\right)^{1/3} P^{-2/3} \rho_*^{-1/3}$$

- Stellar mass estimates are as good as the models that produce the tracks and isochrones!

Empirical mass-radius relation: 94 EBs

$$\log M = a_1 + a_2 X + a_3 X^2 + a_4 X^3 + a_5 (\log g)^2 + a_6 (\log g)^3 + a_7 [\text{Fe}/\text{H}]$$

$$\log R = b_1 + b_2 X + b_3 X^2 + b_4 X^3 + b_5 (\log g)^2 + b_6 (\log g)^3 + b_7 [\text{Fe}/\text{H}], \text{ where } X = \log T_{\text{eff}} - 4.1.$$

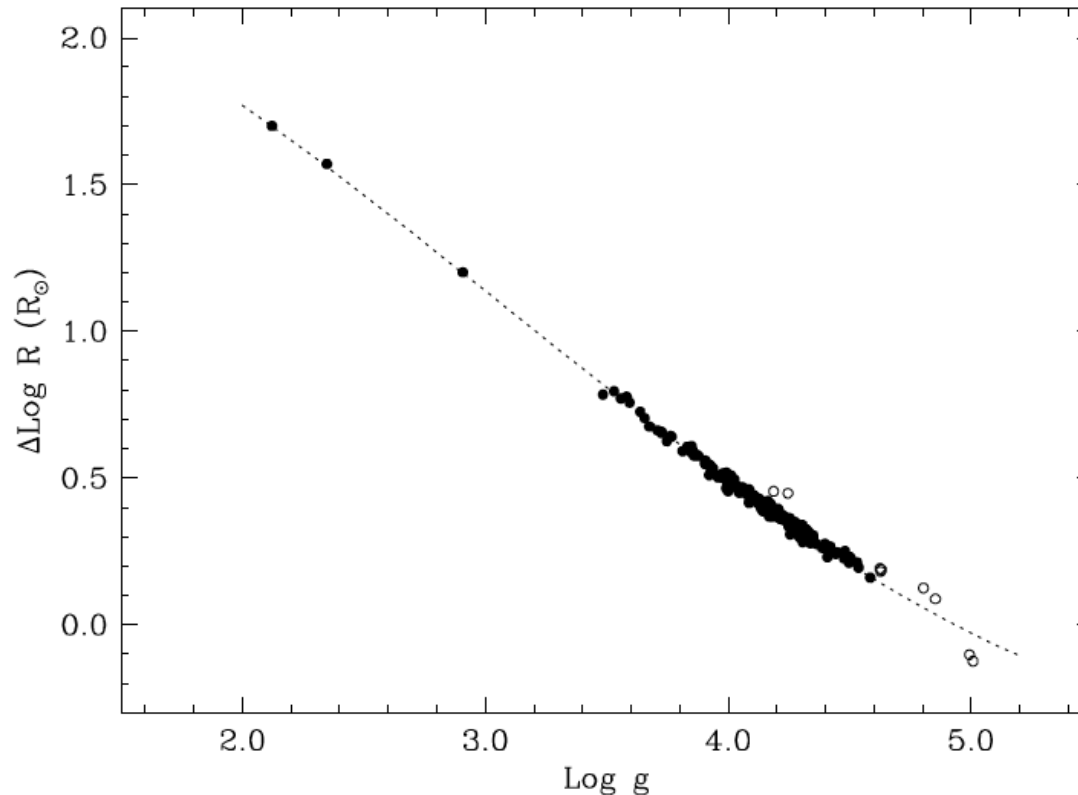
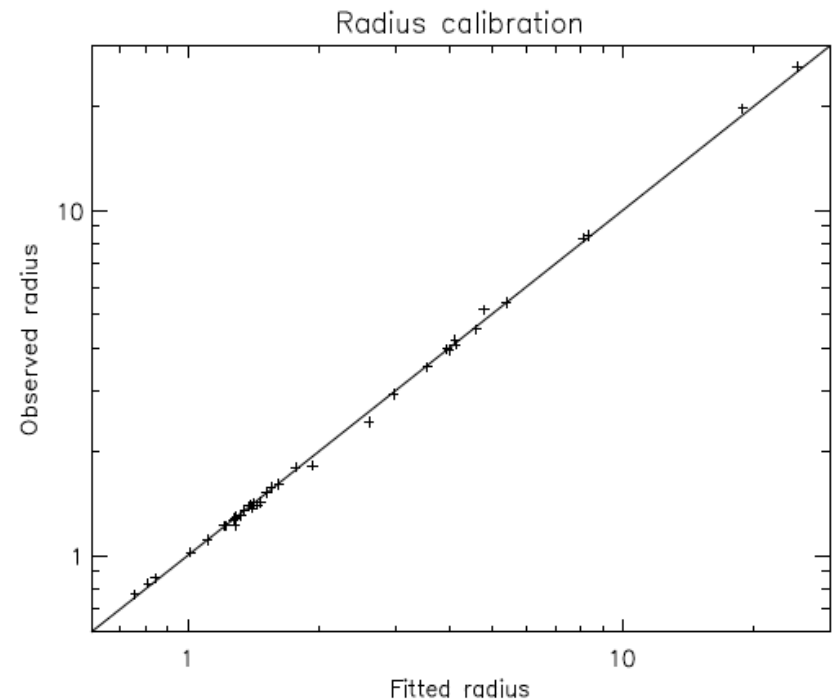
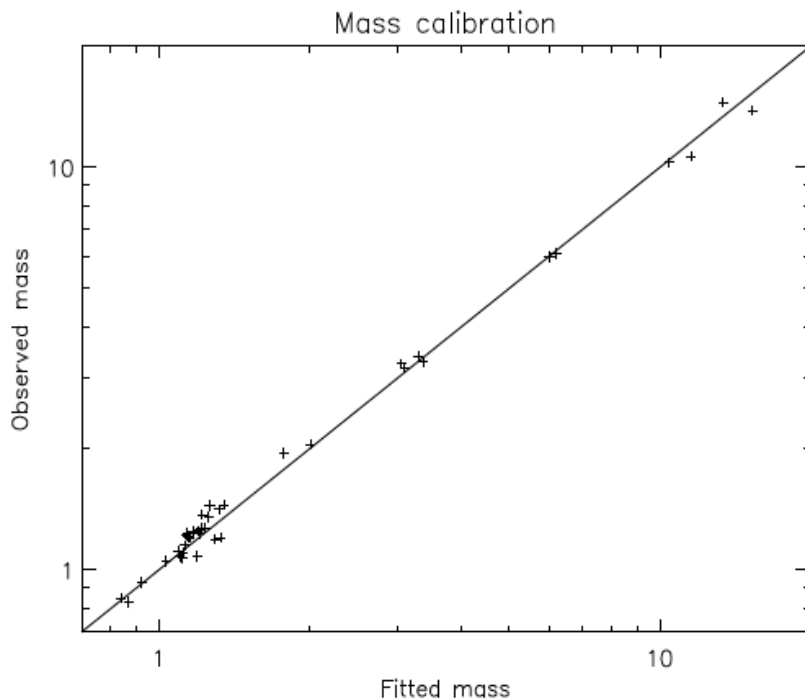


Fig. 14 Deviation of the observed radii from a polynomial ZAMS relation in T_{eff} and $[\text{Fe}/\text{H}]$, $\Delta \log R$ vs. $\log g$. Open symbols denote stars below $0.6 M_{\odot}$ and pre-main-sequence stars. The dotted line represents the remaining fitted dependence on $\log g$.

Empirical mass-radius-relation 2

$$\log M = a_1 + a_2 X + a_3 X^2 + a_4 \log \rho + a_5 \log \rho^2 + a_6 \log \rho^3 + a_7 [\text{Fe}/\text{H}]$$

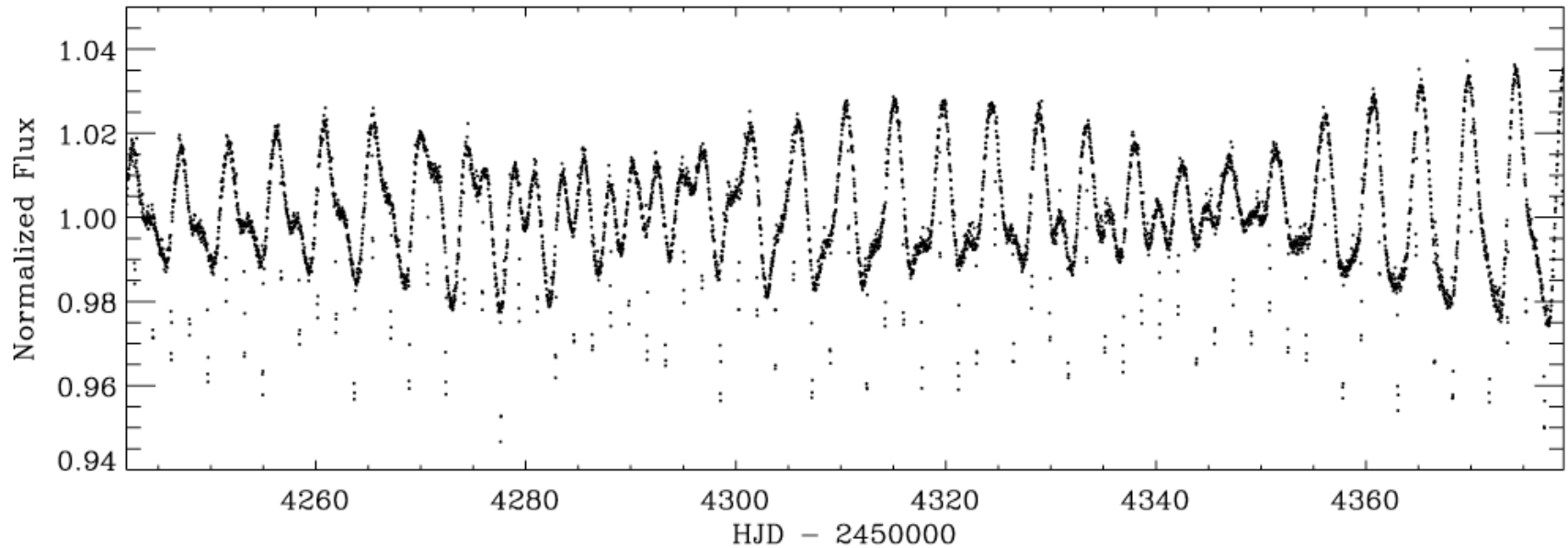
$$\log R = b_1 + b_2 X + b_3 \log \rho + b_4 [\text{Fe}/\text{H}].$$



38 binary components with well-determined [Fe/H] from Torres et al 2010.

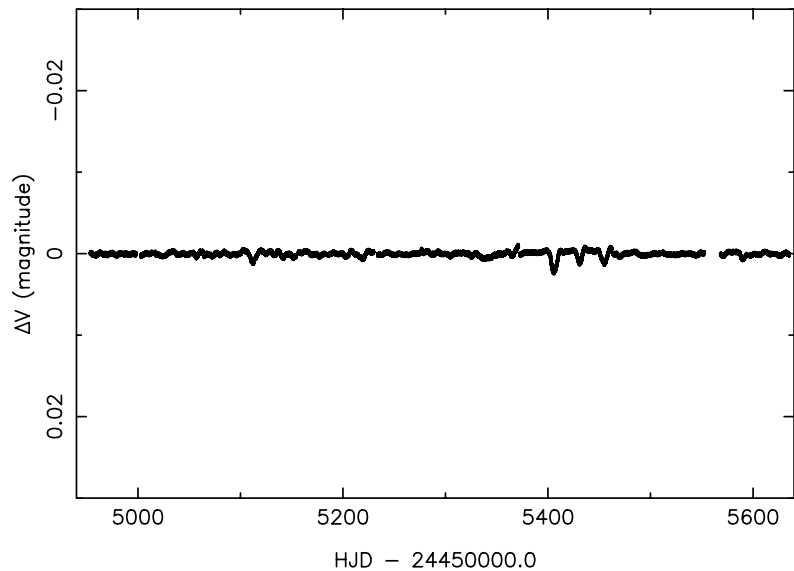
Benign uses for starspots

R. Alonso et al.: CoRoT-Exo-2b

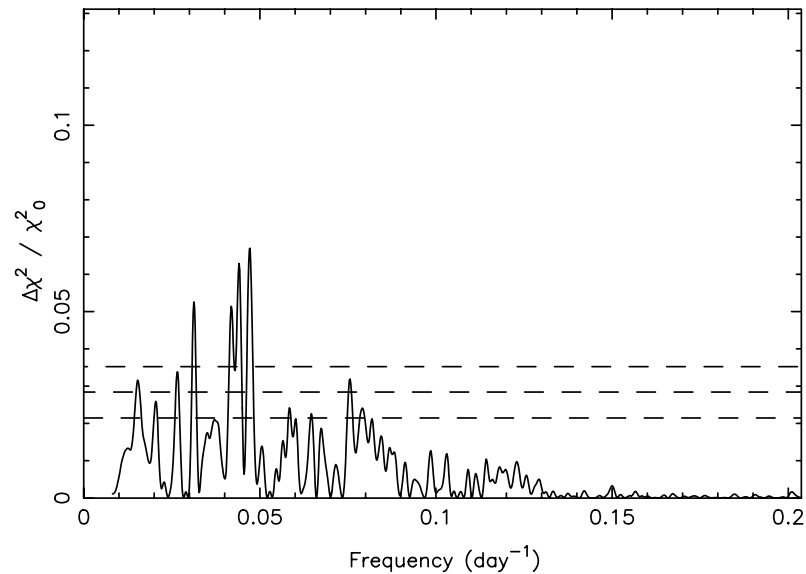


Alonso et al 2008, A&A 482, L21: CoRoT-2
Nutzman et al 2011, ApJ 740, 10

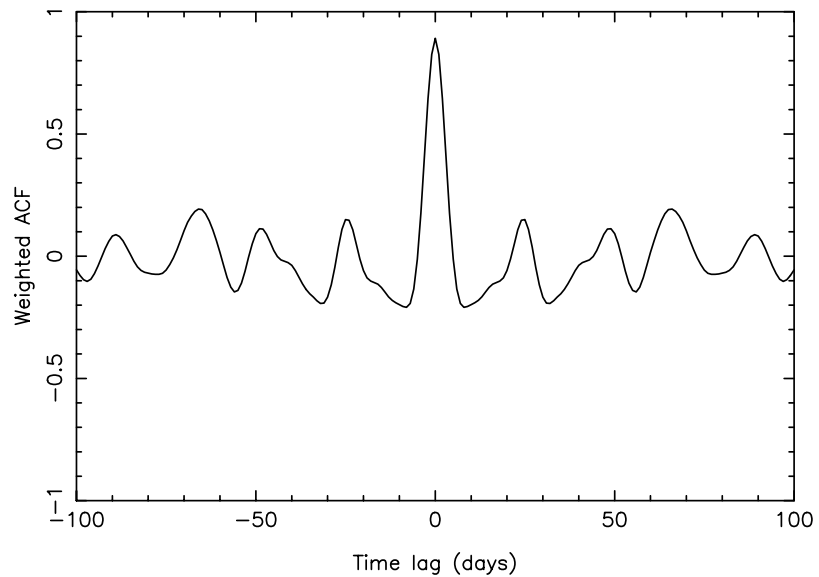
kepler-22.csv P= 21.144087 $\Delta V = 1.13714421E-04$



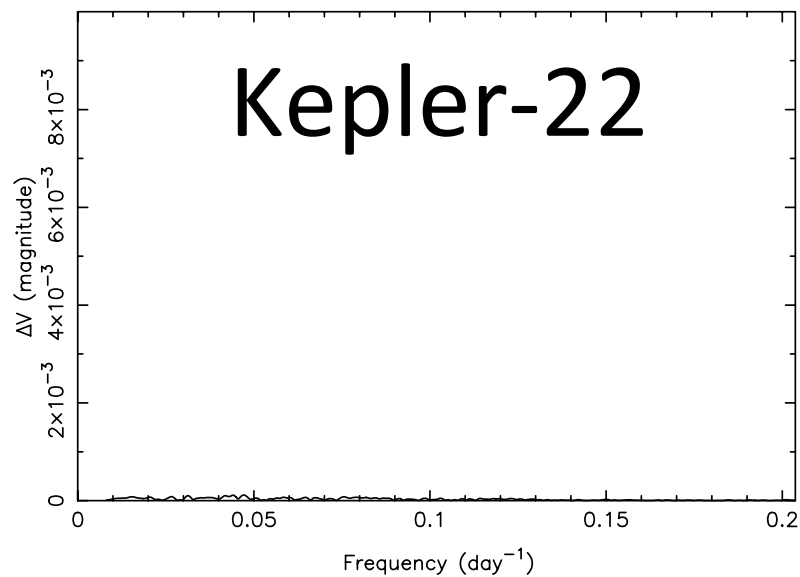
kepler-22.csv P= 21.144087 $\Delta \chi^2 = -72182.617$



kepler-22.csv P= 24.542400 ACF= 0.15422028



kepler-22.csv P= 21.144087 $\Delta V = 1.13714421E-04$

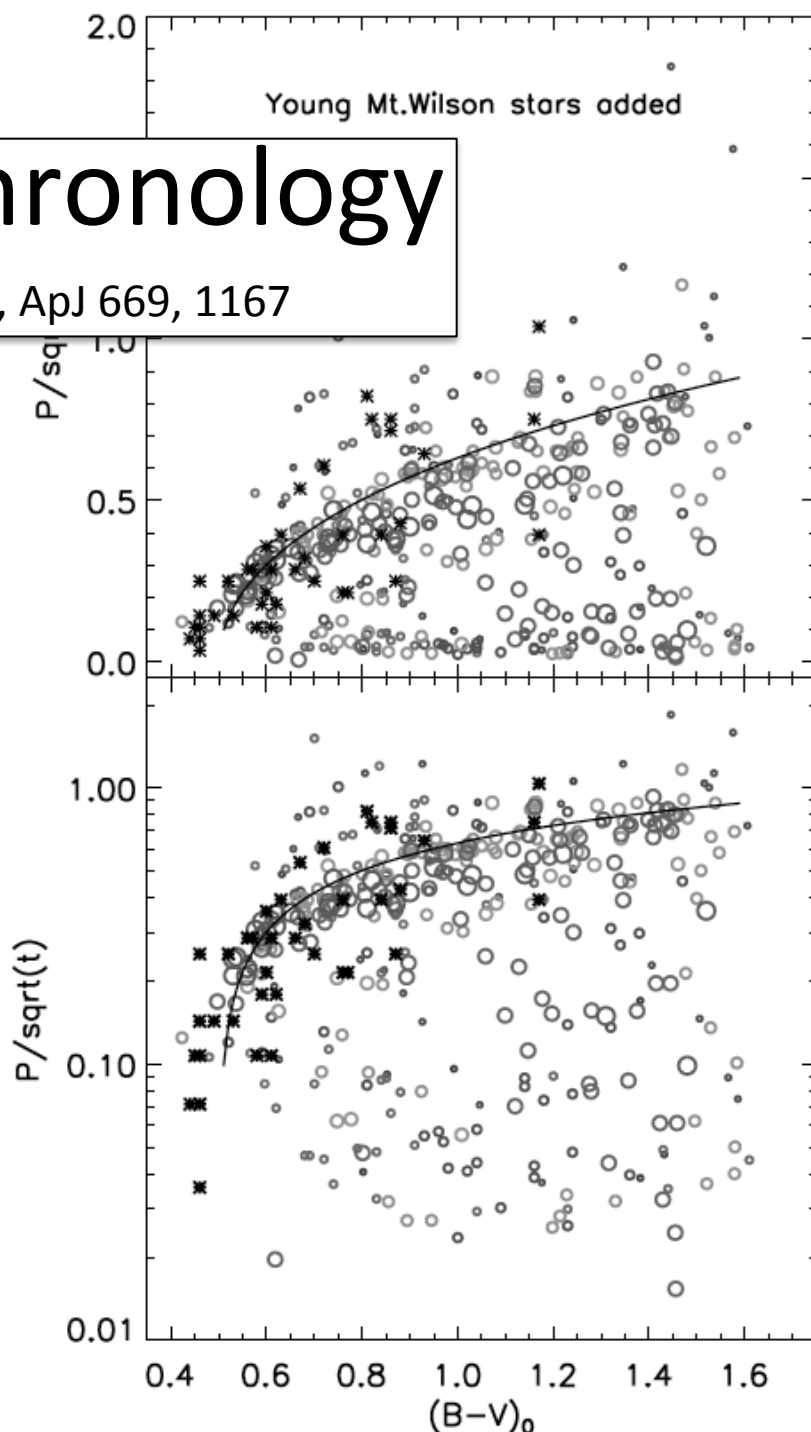
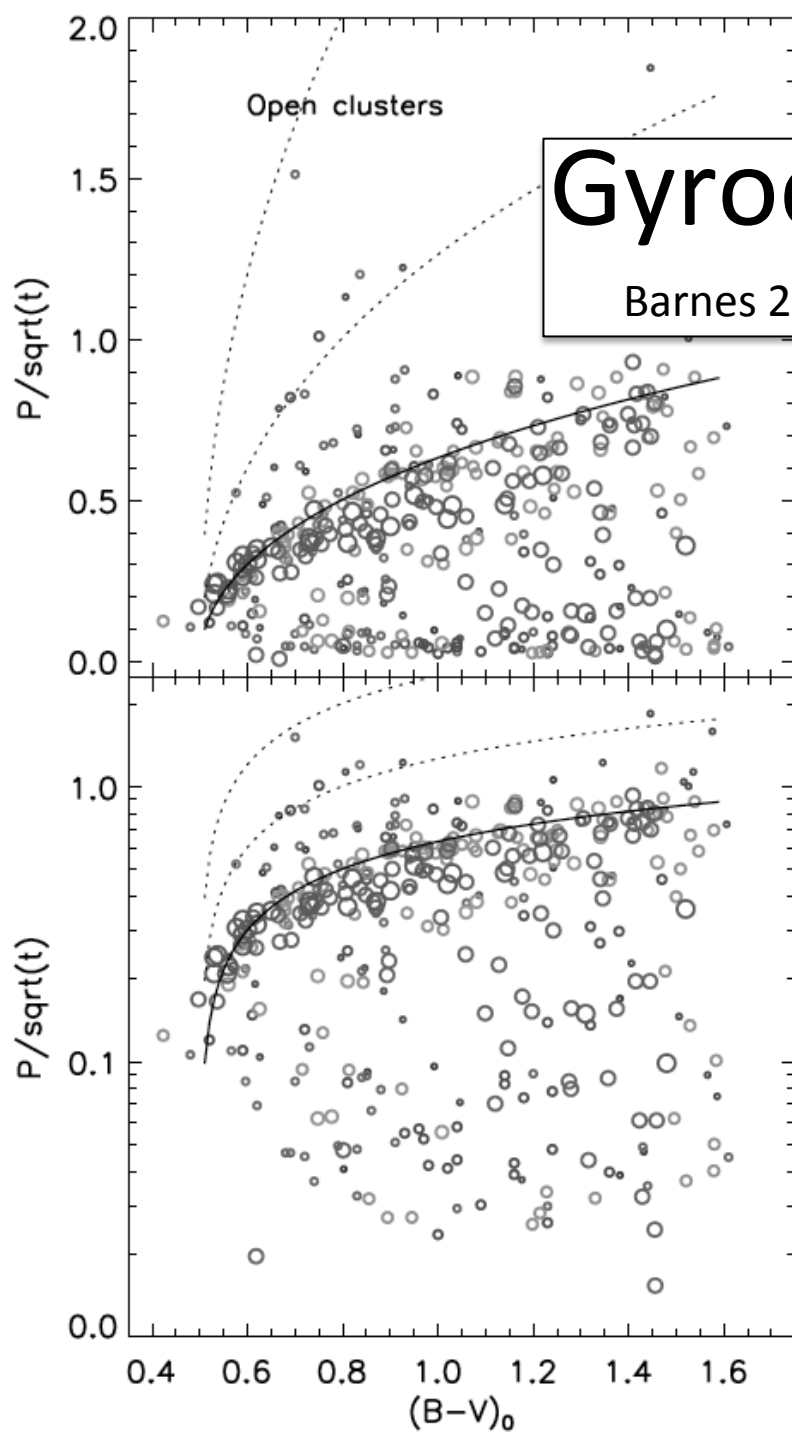


Gyrochronology

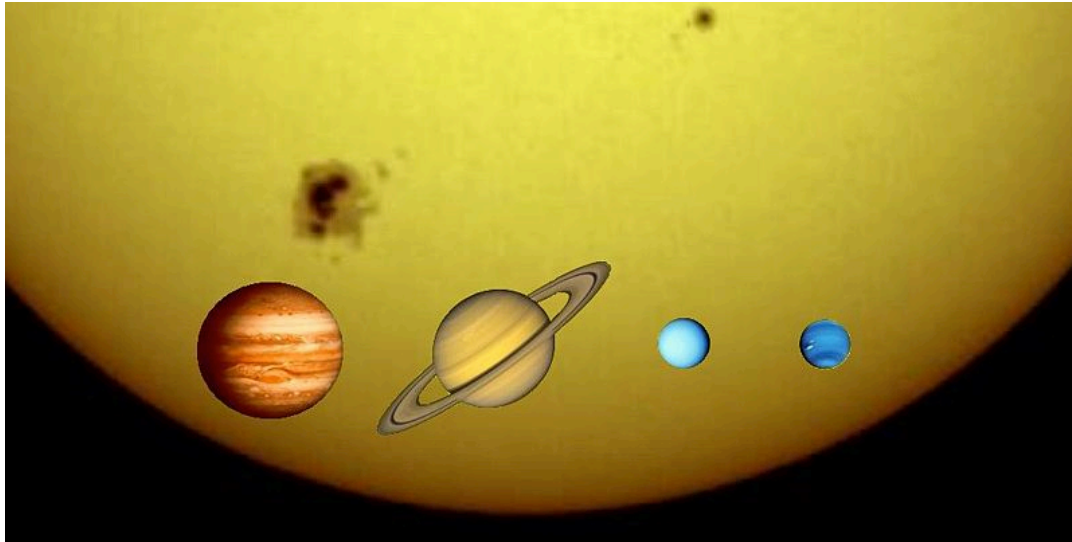
Barnes 2007, ApJ 669, 1167

Open clusters

Young Mt. Wilson stars added



Transit Depth



What fraction of the star's disk does the planet cover?

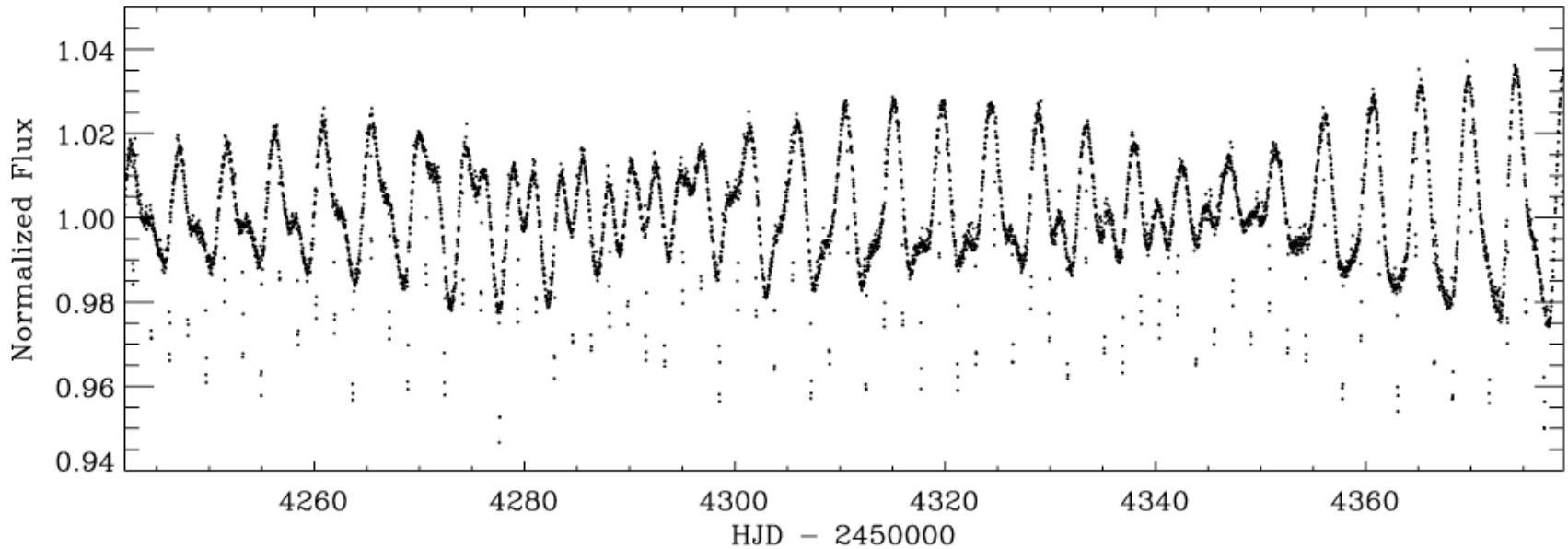
$$\frac{\Delta f}{f} \approx \left(\frac{r_p}{R_*} \right)^2 = 0.01 \left(\frac{r_p}{r_{Jup}} \right)^2 \left(\frac{R_*}{R_{sun}} \right)^{-2}$$

Find star radius from its spectral type.

Observed depth tells us planet's radius.

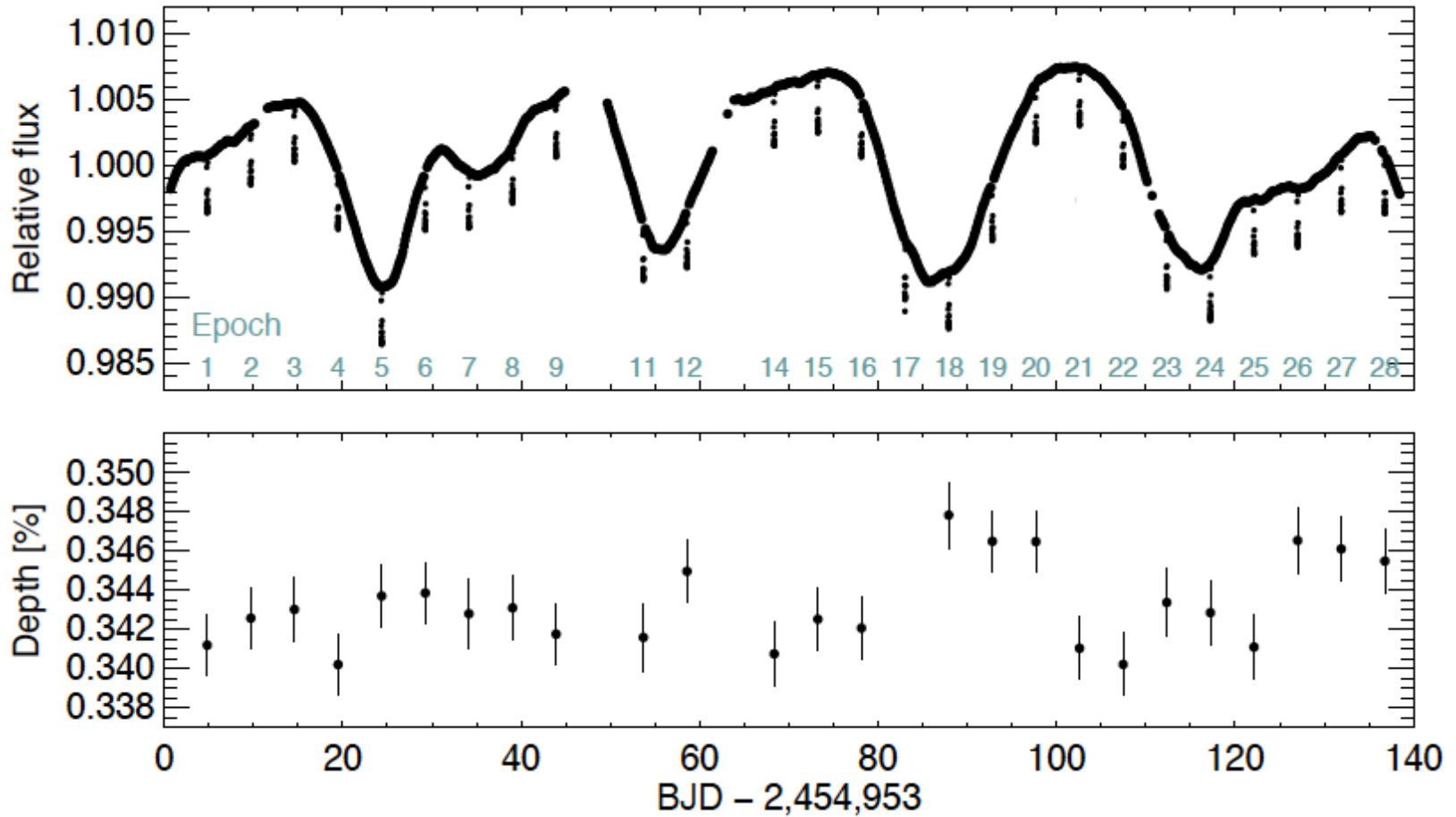
Starspots as vermin

R. Alonso et al.: CoRoT-Exo-2b



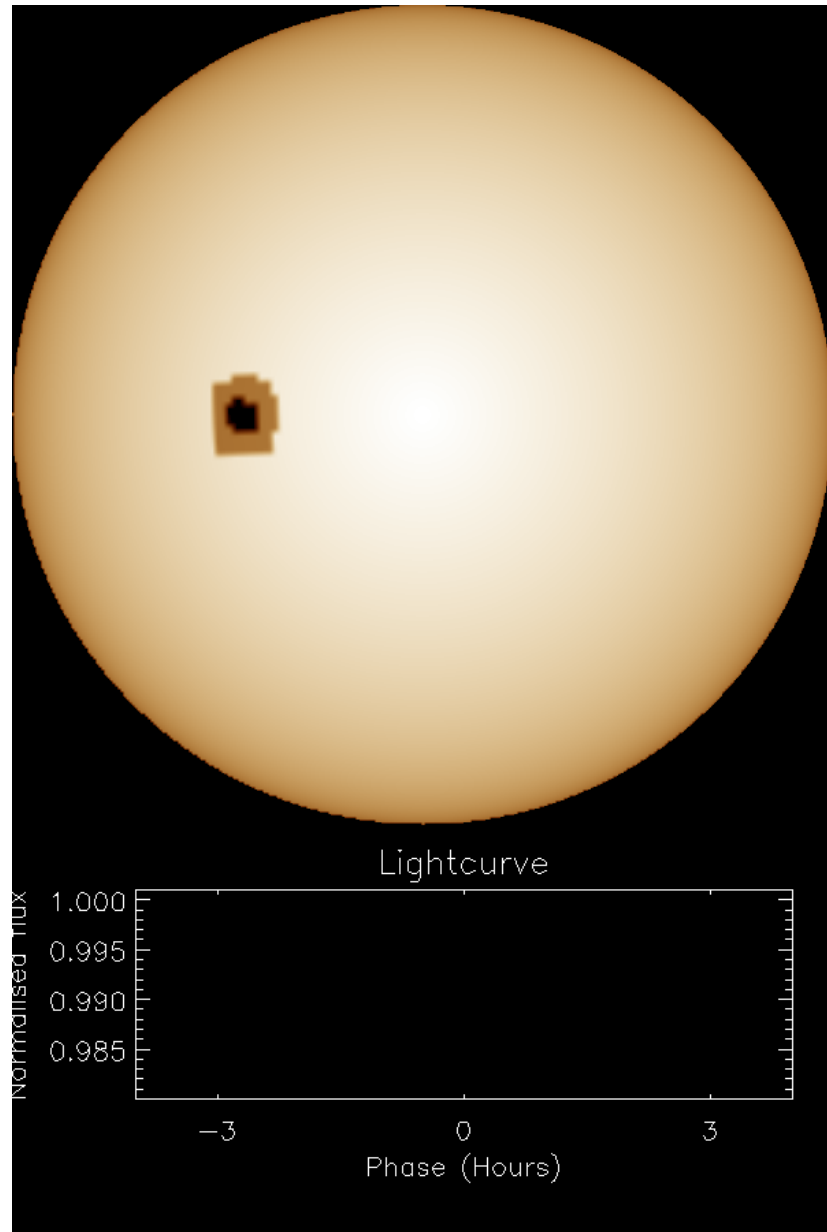
Alonso et al 2008, A&A 482, L21: CoRoT-2
Nutzman et al 2011, ApJ 740, 10

Constant flux deficit? HAT-P-11



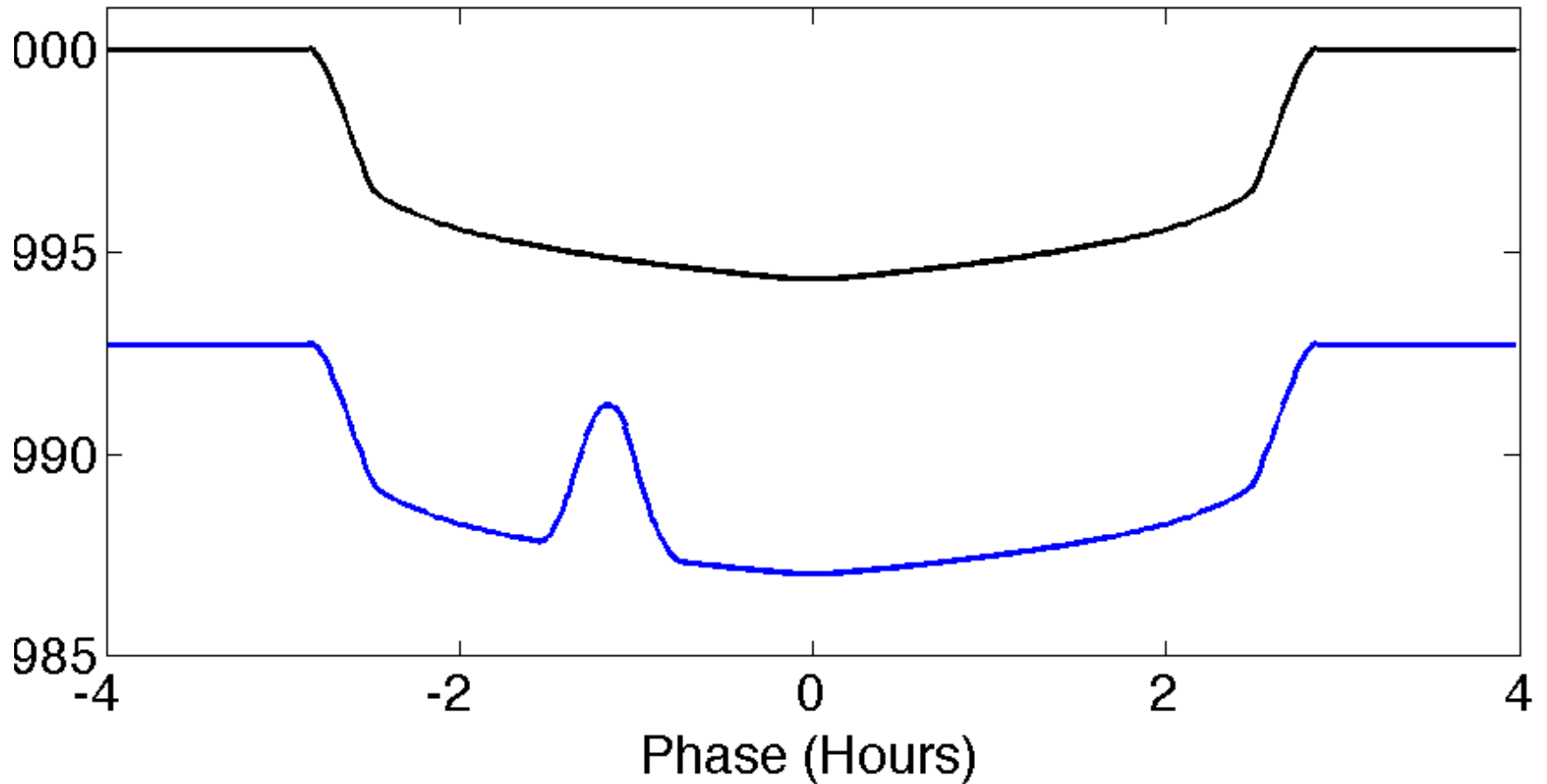
Transit depth amplification by unclipsed starspots

Constant flux deficit at all times except when planet occults a spot.



Animation courtesy of Joe Llama, St Andrews

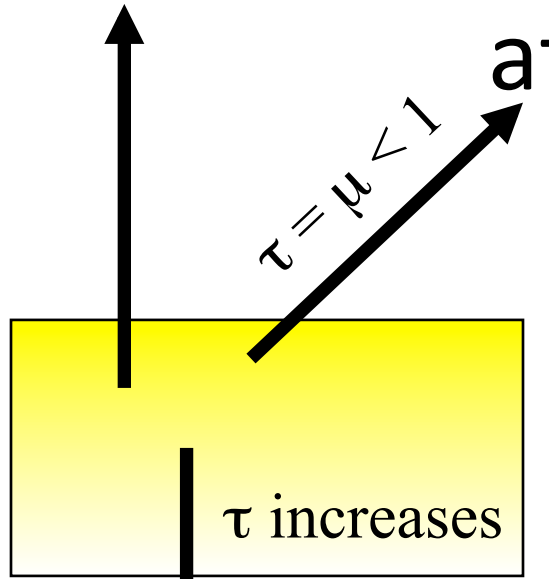
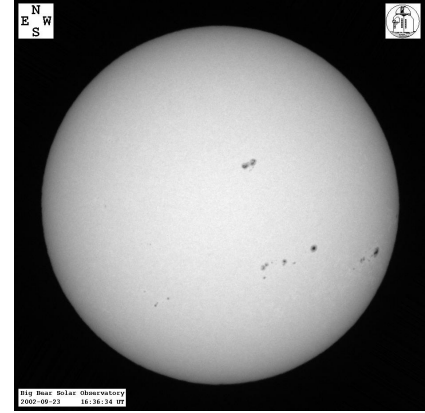
Transit depth amplification



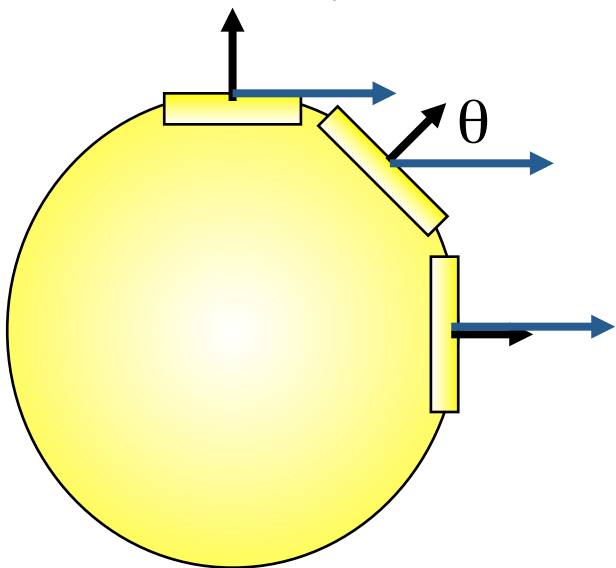
Plot courtesy of Joe Llama, St Andrews

$$\tau = \mu = 1$$

Limb darkening and atmospheric structure



$$\mu = \cos \theta$$

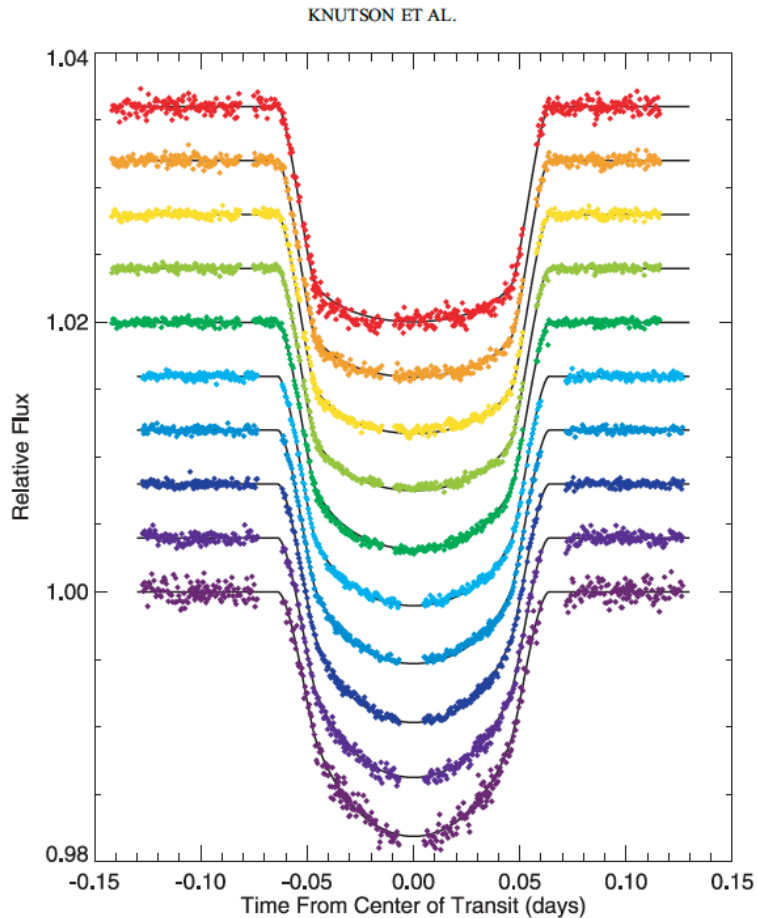


- Depth dependence of source function maps on to angular dependence of emergent specific intensity via Laplace transform:

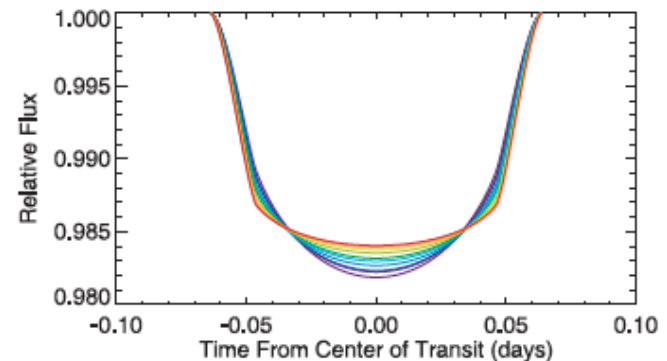
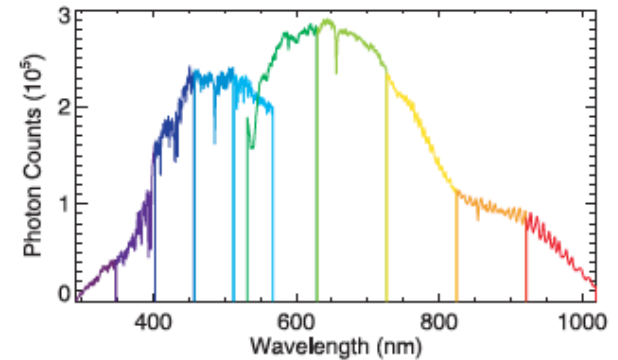
$$S_v(\tau_v) = \sum_{n=0}^{\infty} a_n \tau_v^n$$

$$I_v^+(0, \mu) = \mathcal{L}_{1/\mu} \{S_v(\tau_v)\} = \sum_{n=0}^{\infty} n! a_n \mu^n$$

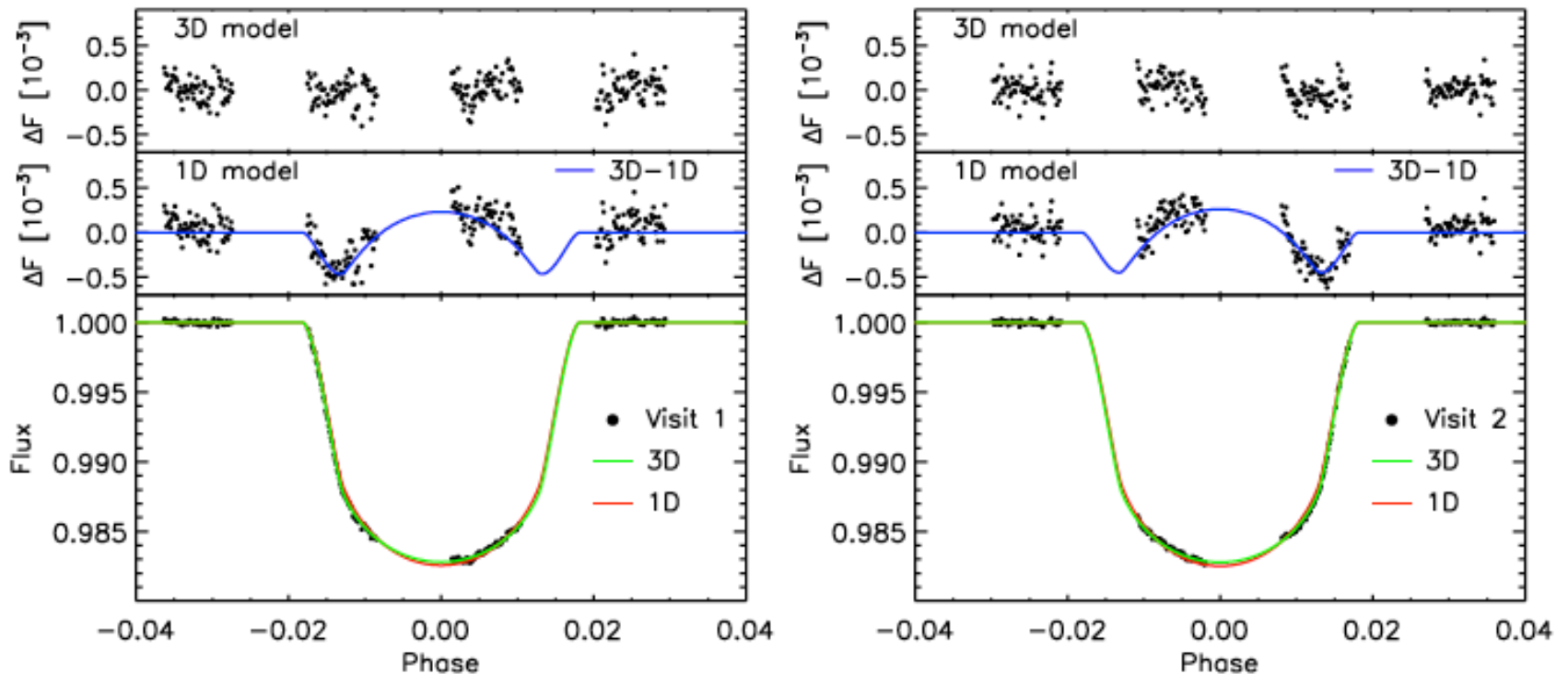
Wavelength dependence



- Knutson et al 2007
- STIS spectrophotometry of HD 209458b transit



1D versus 3D atmosphere models



Hayek et al 2012, A&A 539, A102: 3D hydrodynamical atmosphere models including granulation vs 1D MARCS model atmosphere.

Transit depth reduction by eclipsed spots

Which effect wins?

Depends on spot coverage and active-belt location.

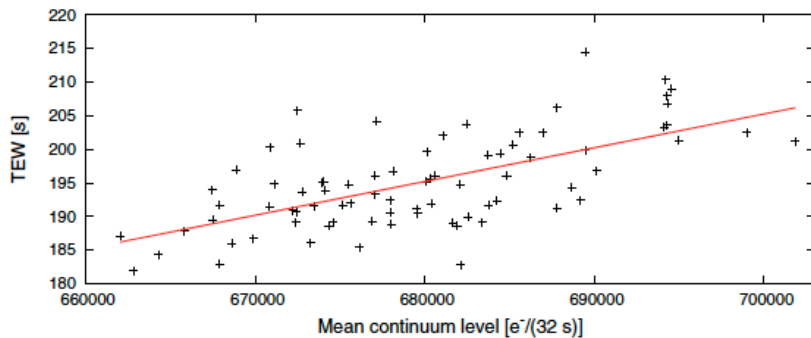


Fig. 1. Transit equivalent width (TEW) versus transit continuum level as well as the best-fit linear model.

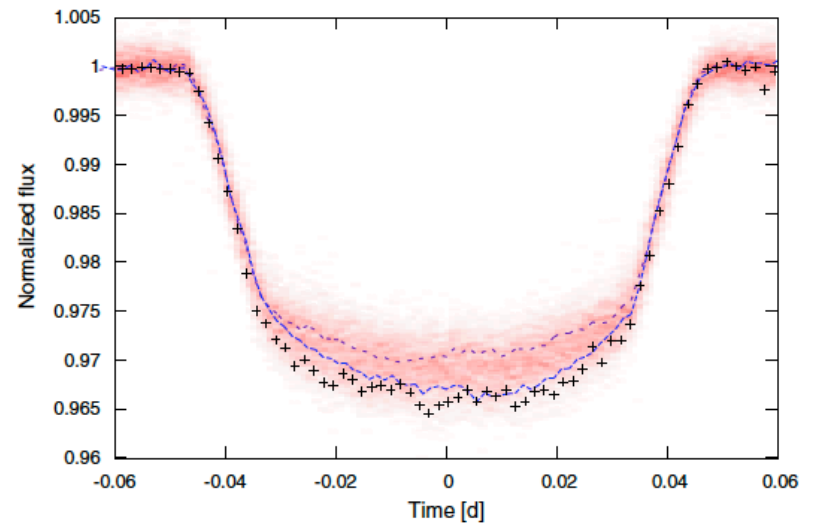
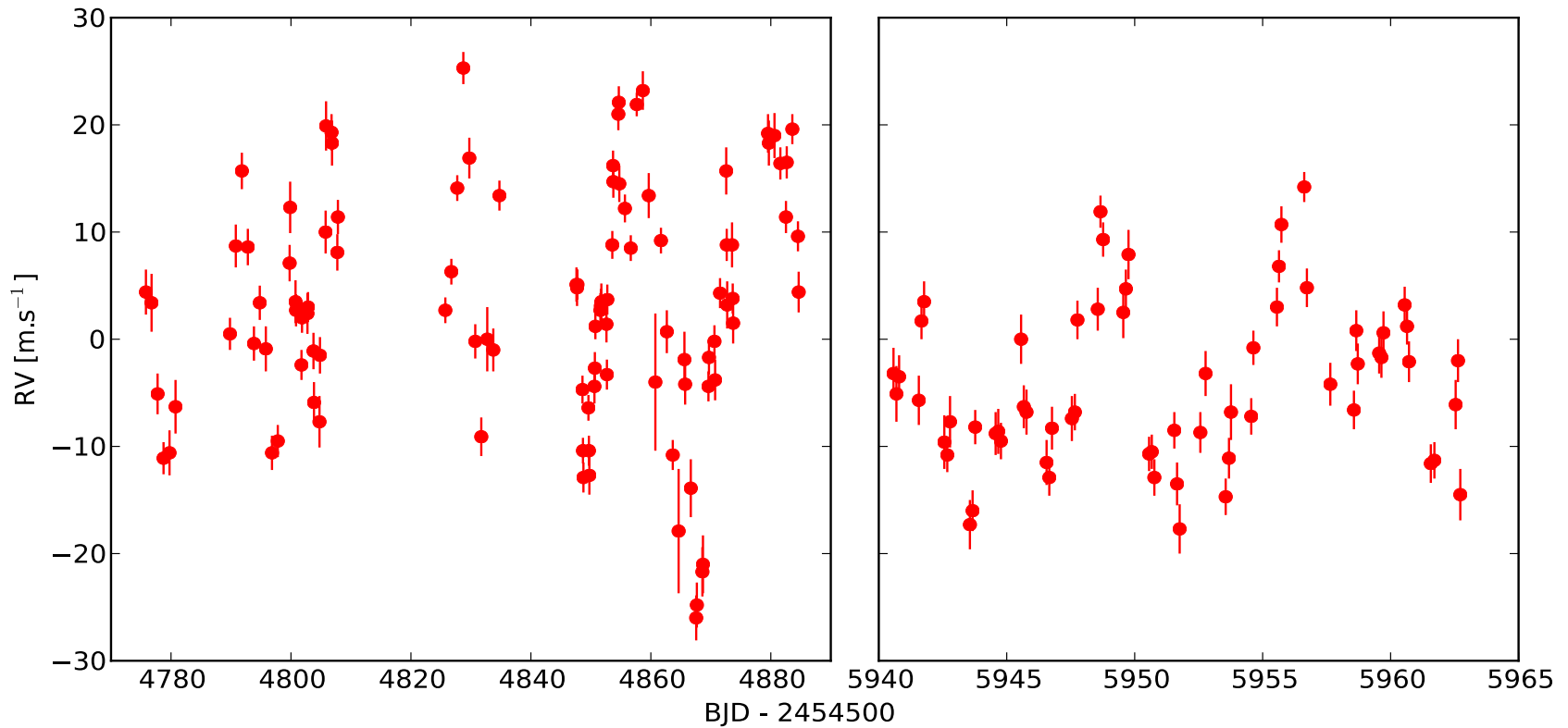


Fig. 2. Average transit light curves obtained by combining the ten profiles exhibiting the highest (thick dashes) and lowest (thin dashes) continuum levels. The crosses indicate our lower envelope estimate and the color gradient (red) illustrates the distribution of data points for all available transits.

CoRoT-7: Spot-induced RV jitter

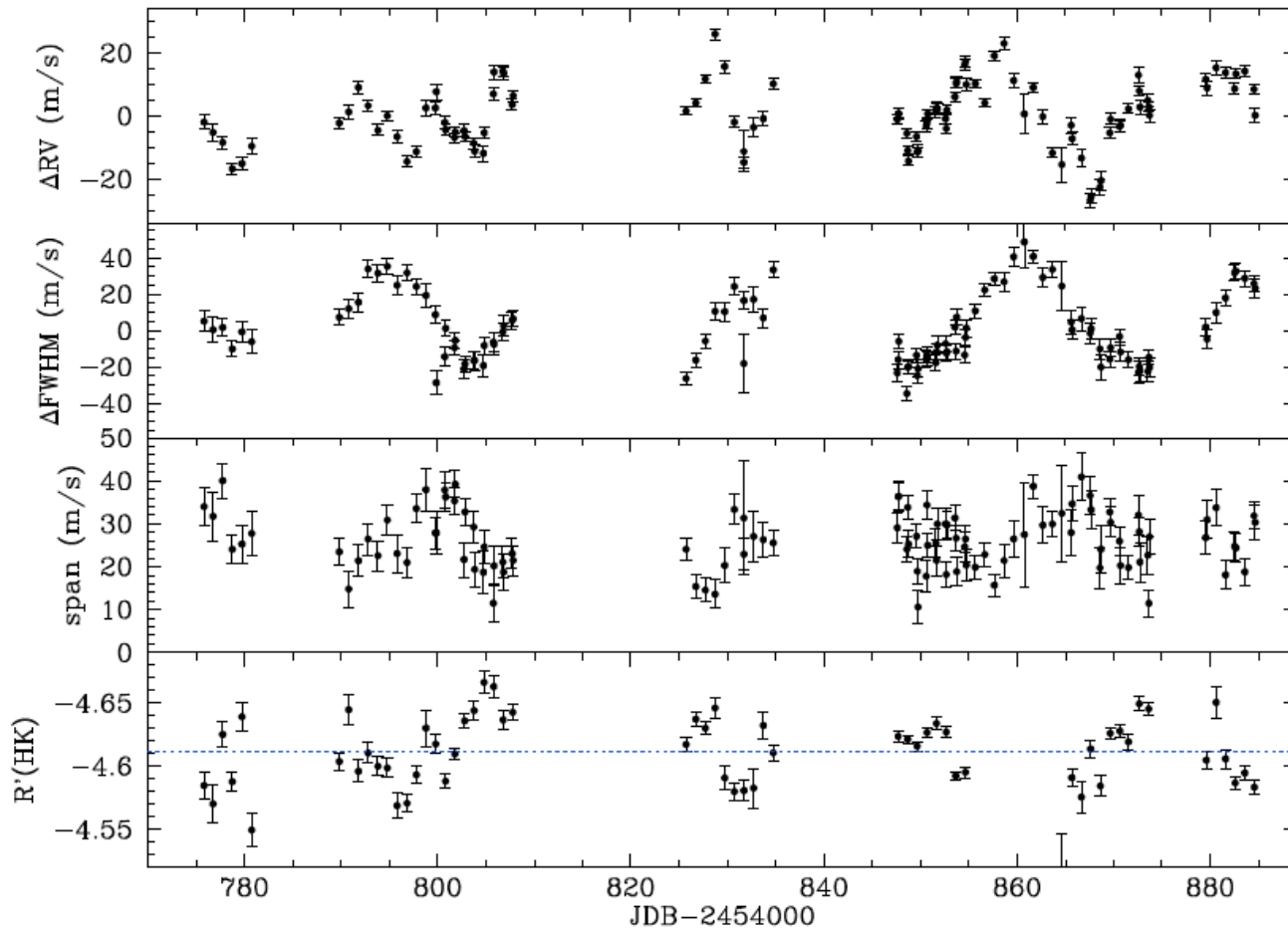
2009 HARPS campaign

2012 HARPS campaign



Decorrelation against activity proxies

CoRoT-7 2009 HARPS campaign

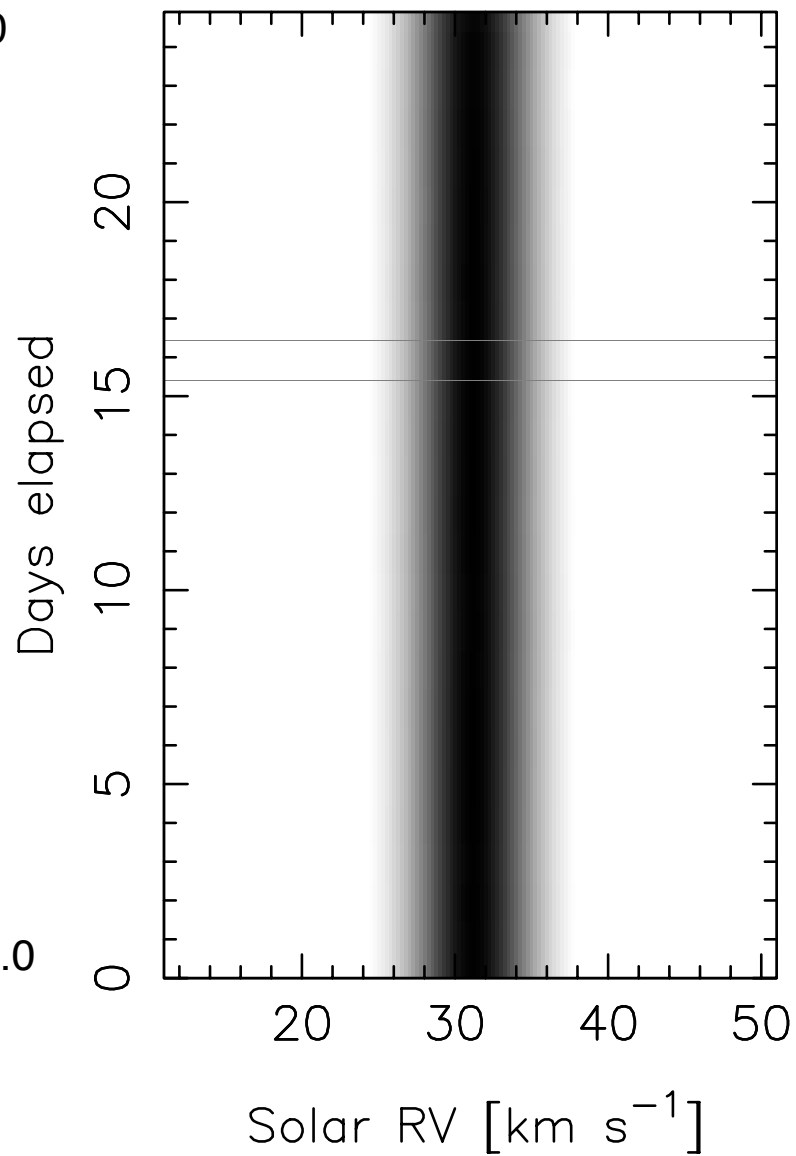


Queloz et al 2009, A&A 506, 303

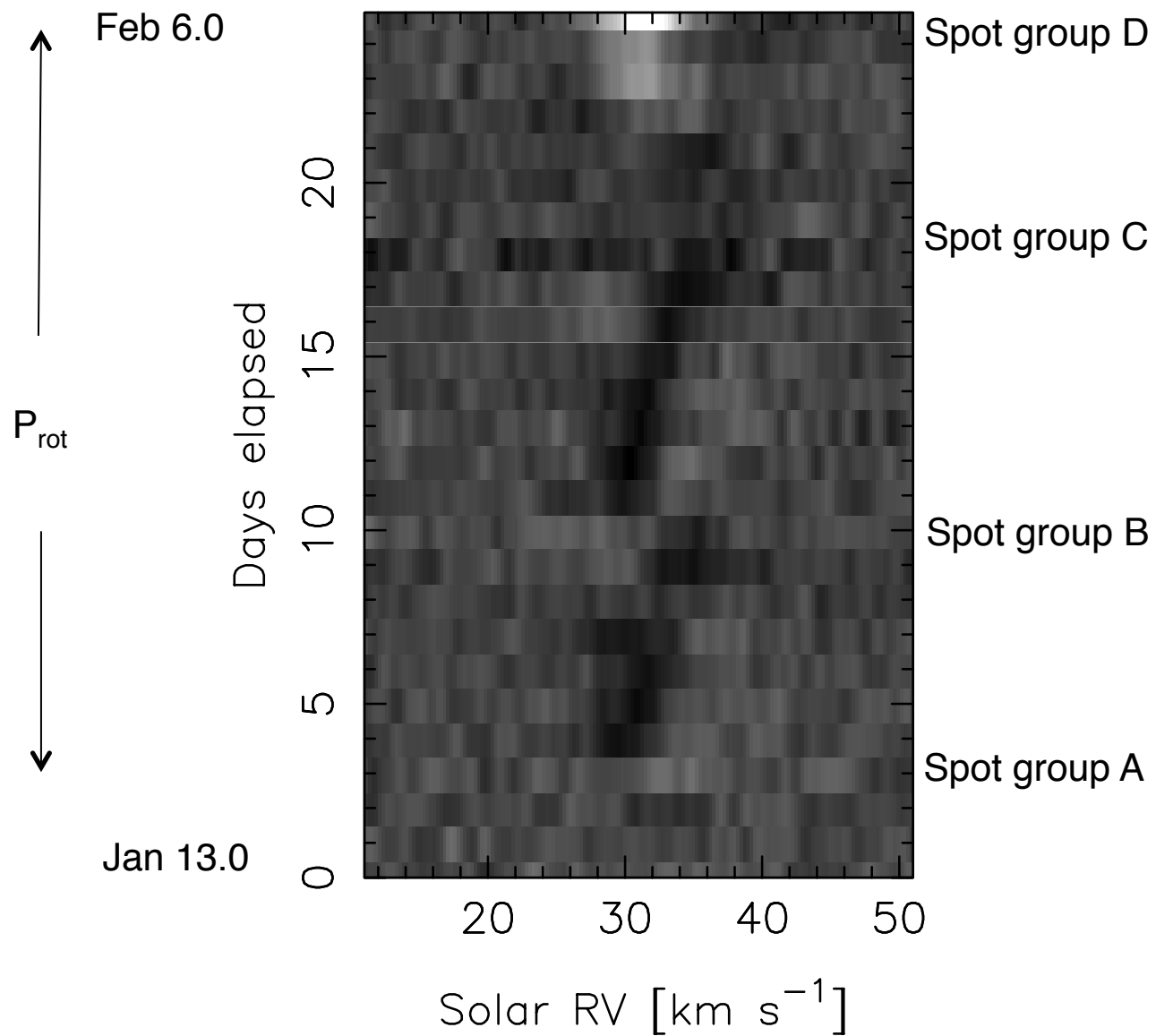
CoRoT-7: HARPS CCF

Feb 6.0

Jan 13.0

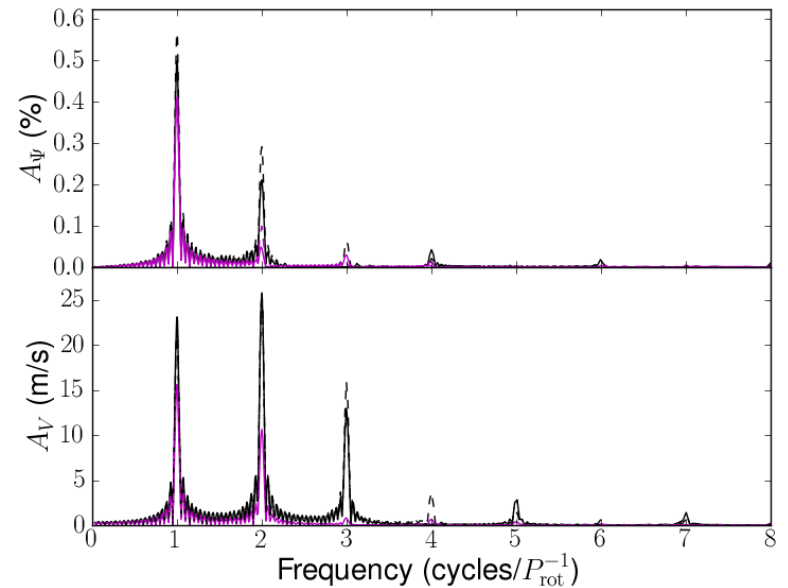
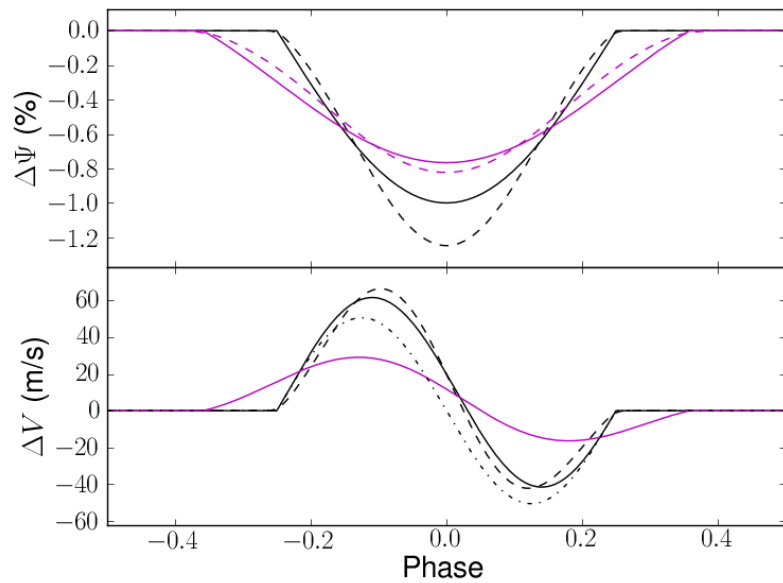


CoRoT-7: HARPS CCF



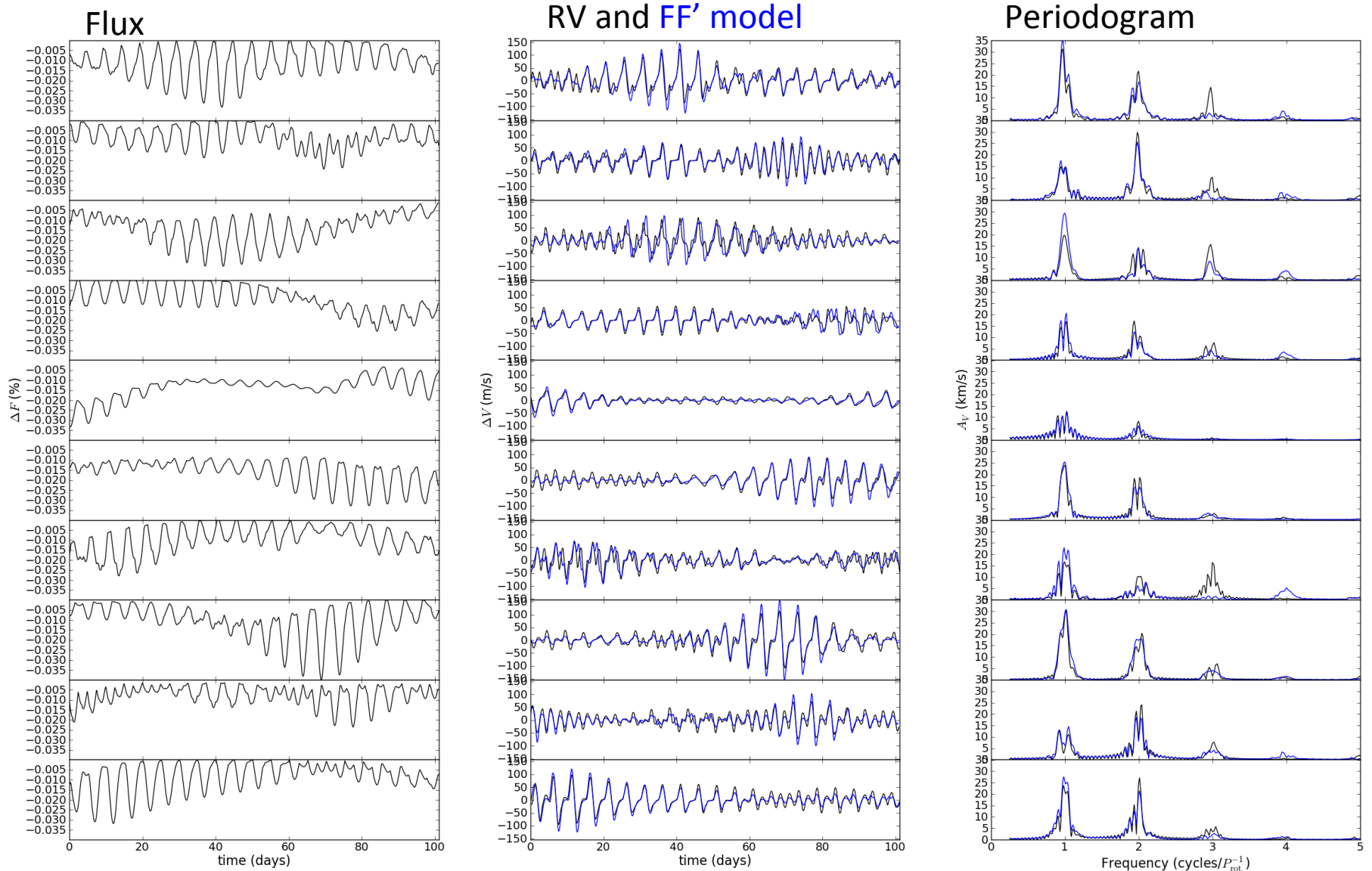
Flux and RV variations: isolated spot

RV variation is closely approximated by product of light curve and its first derivative

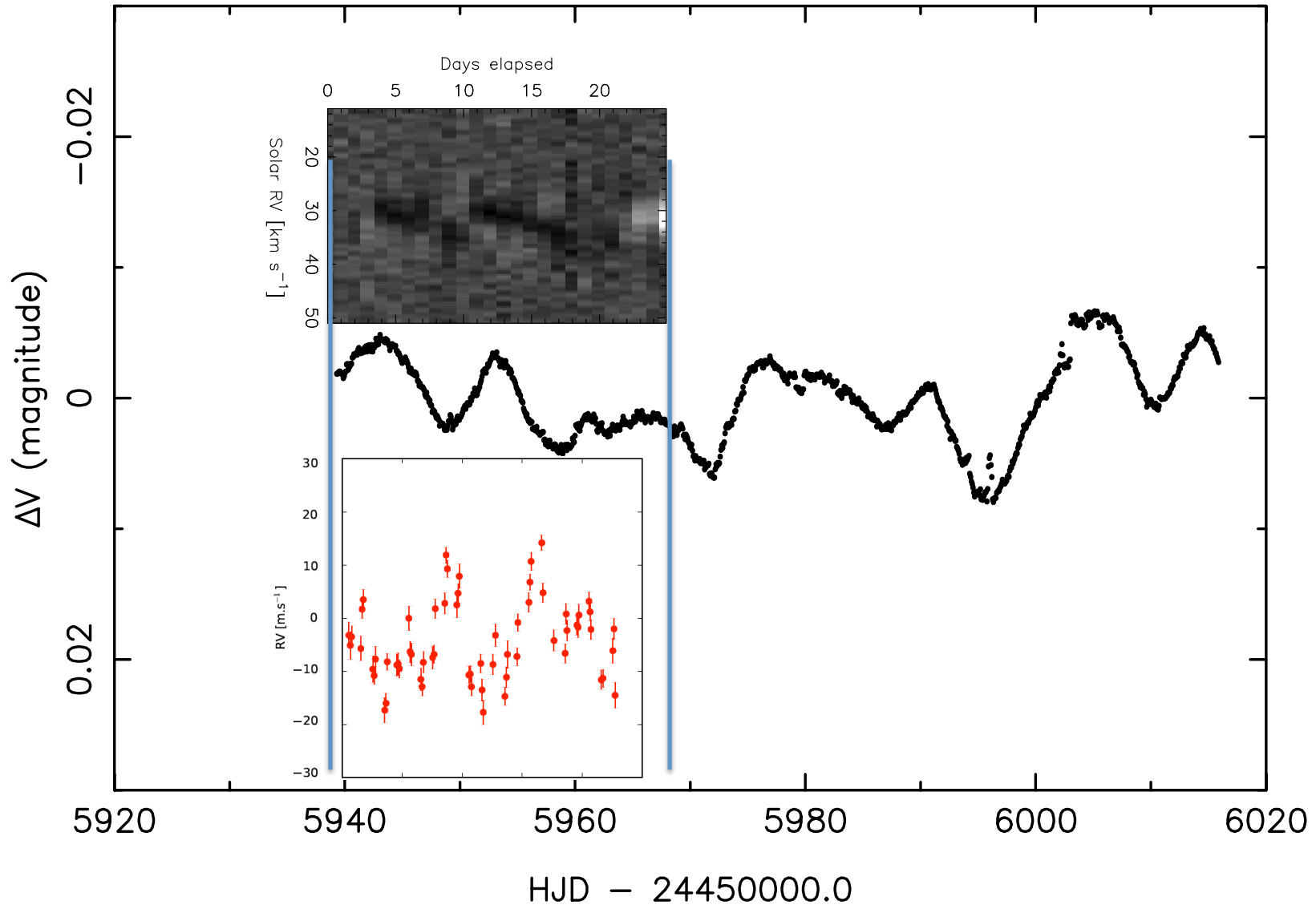


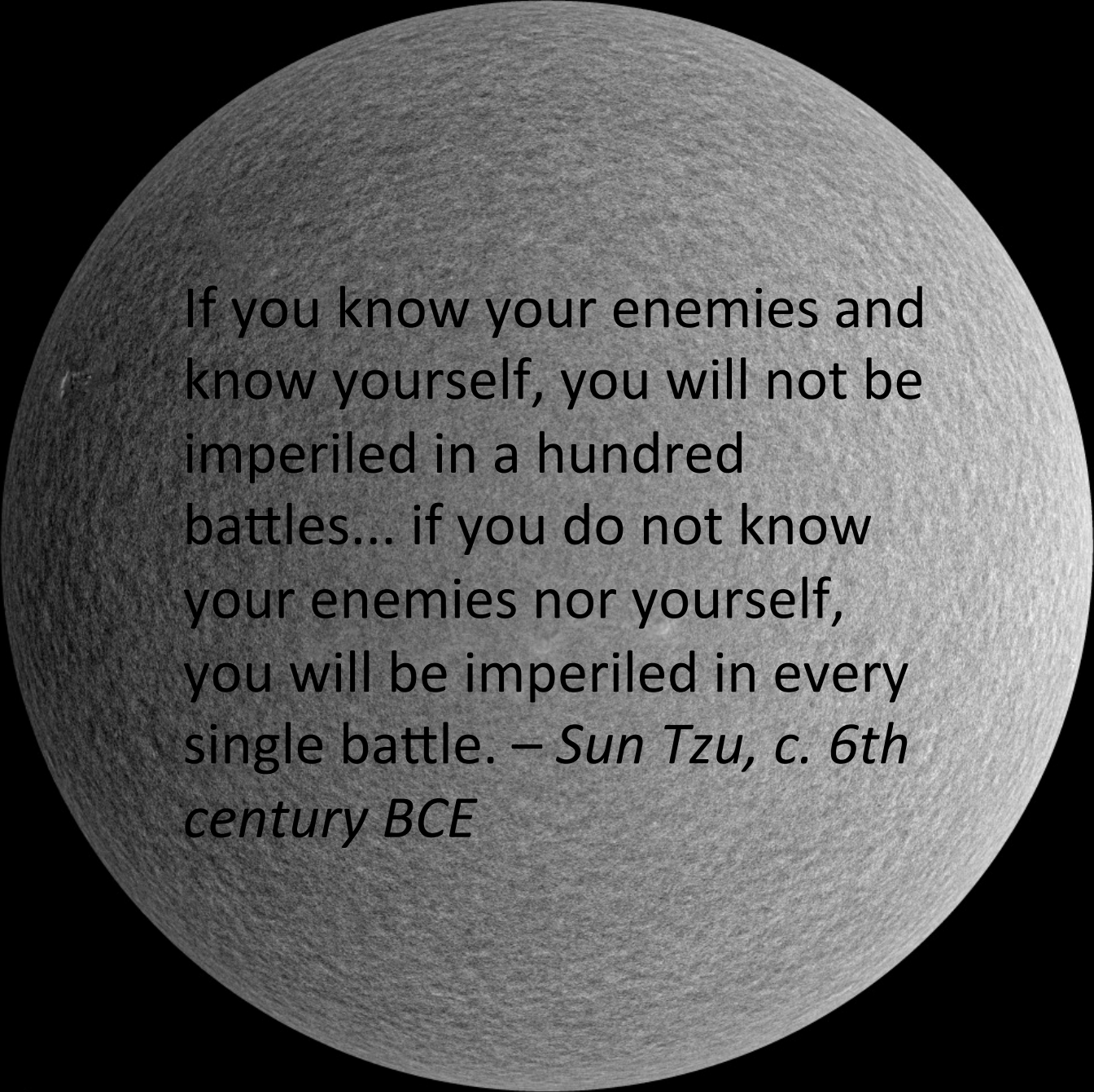
Aigrain, Pont & Zucker 2012, MNRAS 419, 3147

RV variations from photometry

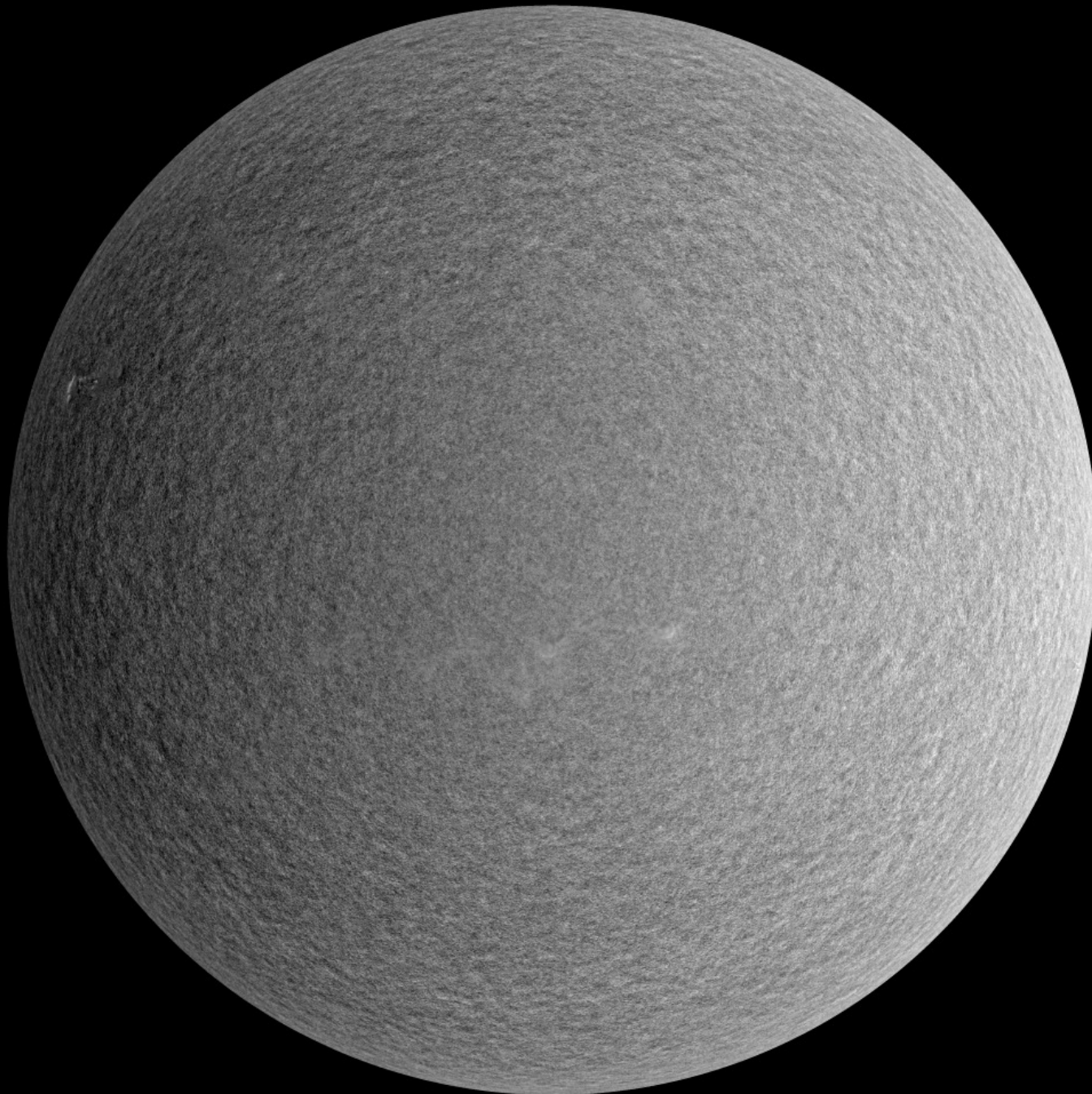


How are flux, CCF and RV jitter related?

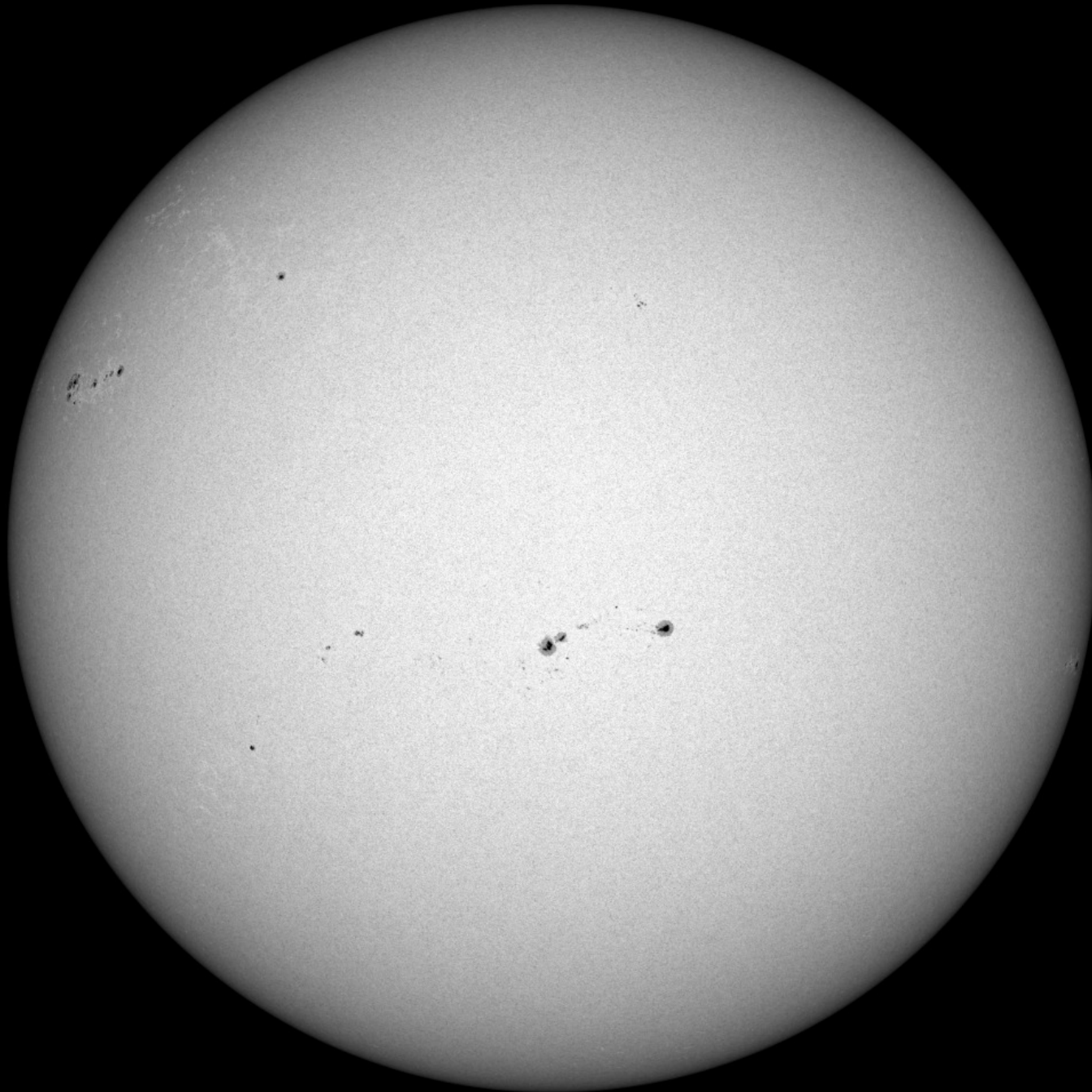


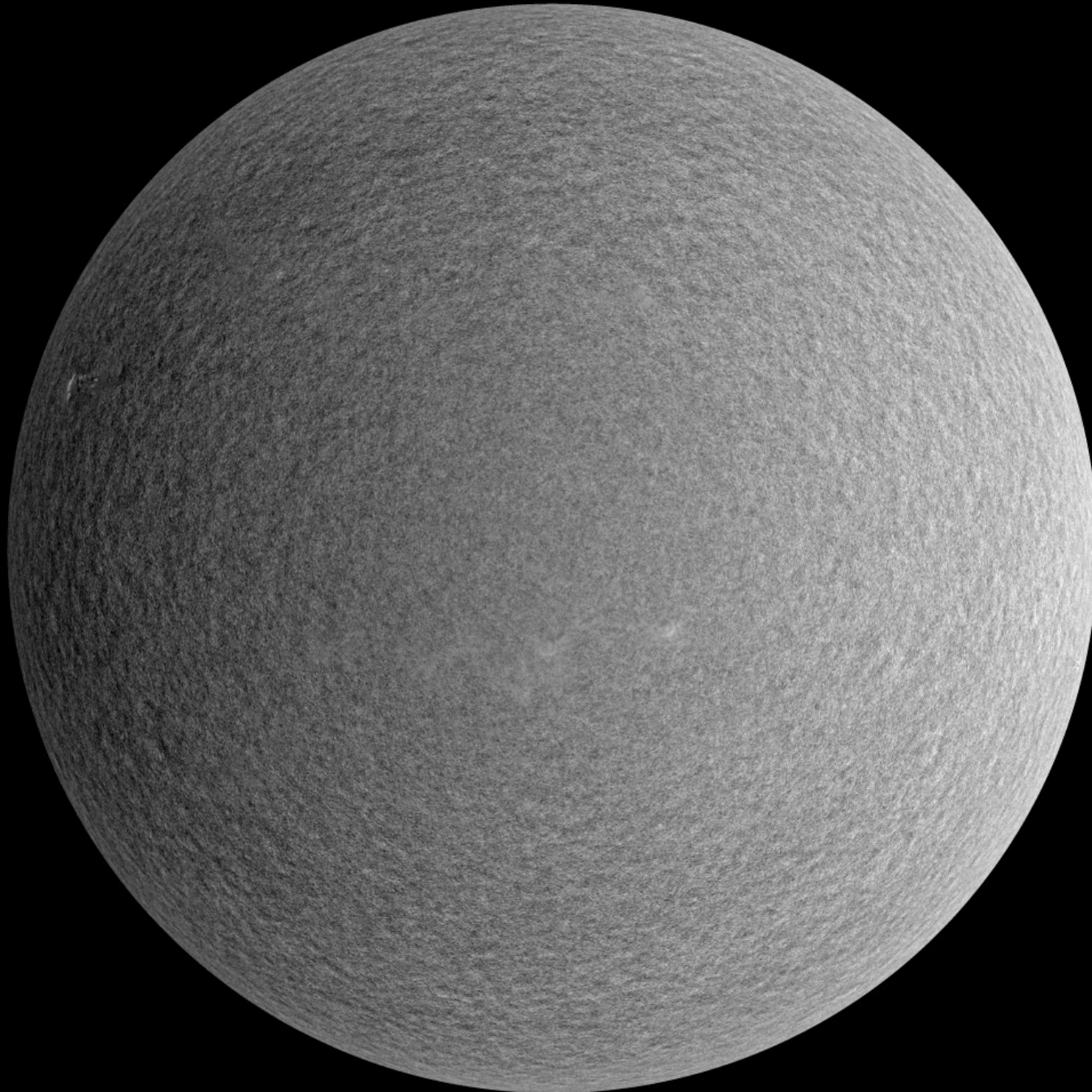


If you know your enemies and
know yourself, you will not be
imperiled in a hundred
battles... if you do not know
your enemies nor yourself,
you will be imperiled in every
single battle. – *Sun Tzu, c. 6th
century BCE*

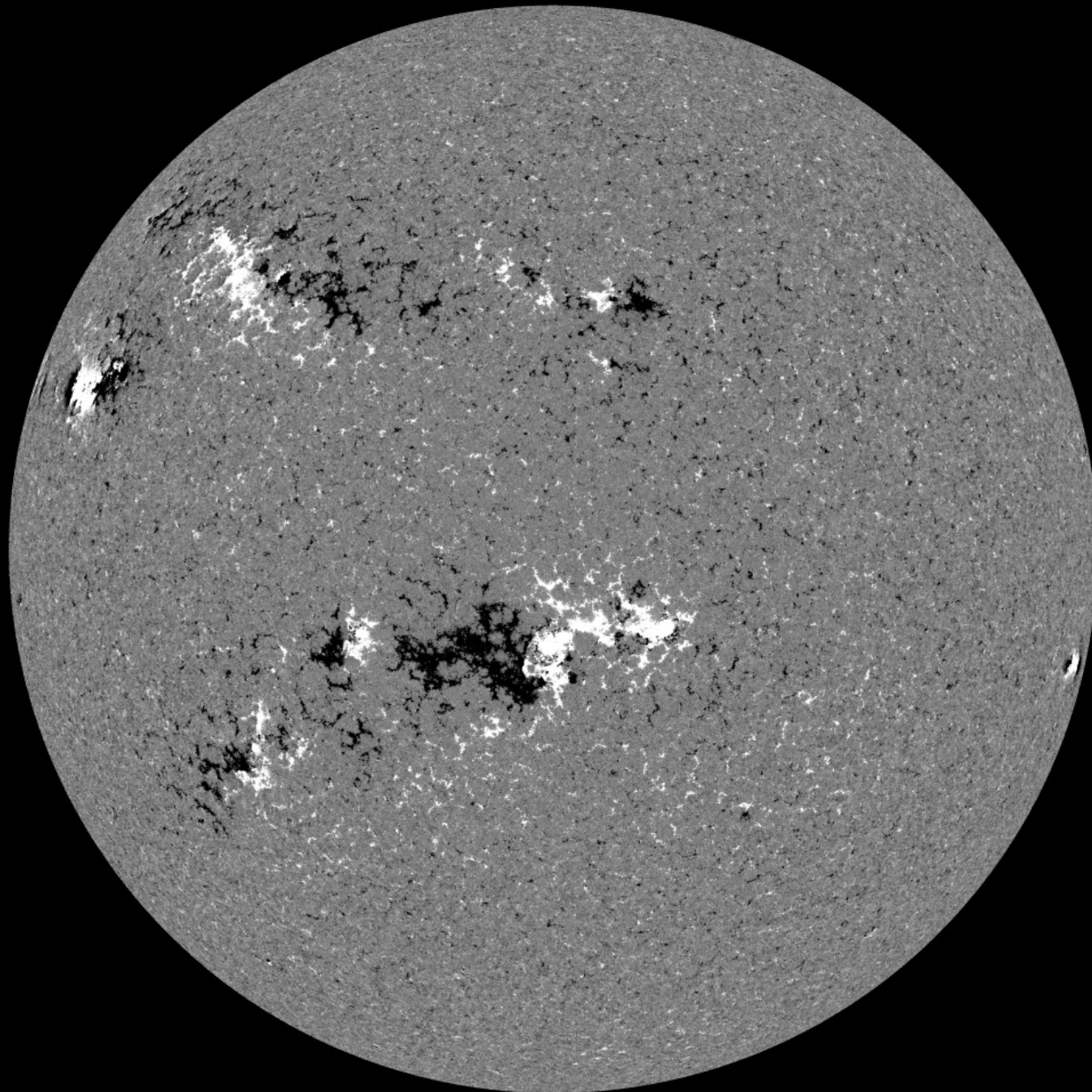


SDO/HMI Quick-Look Dopplergram: 2011.03.28_13:23:15_TAI

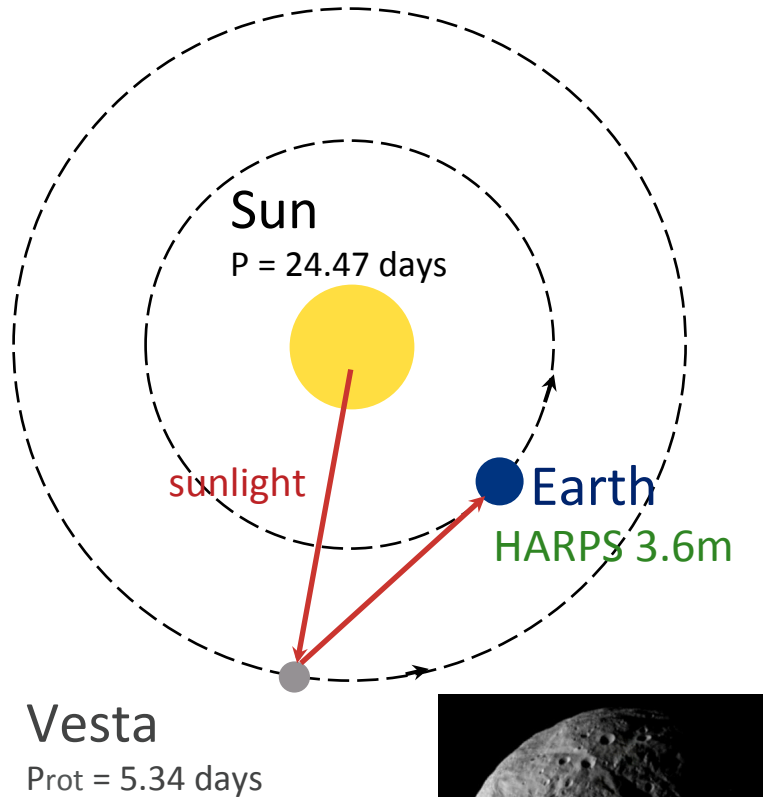




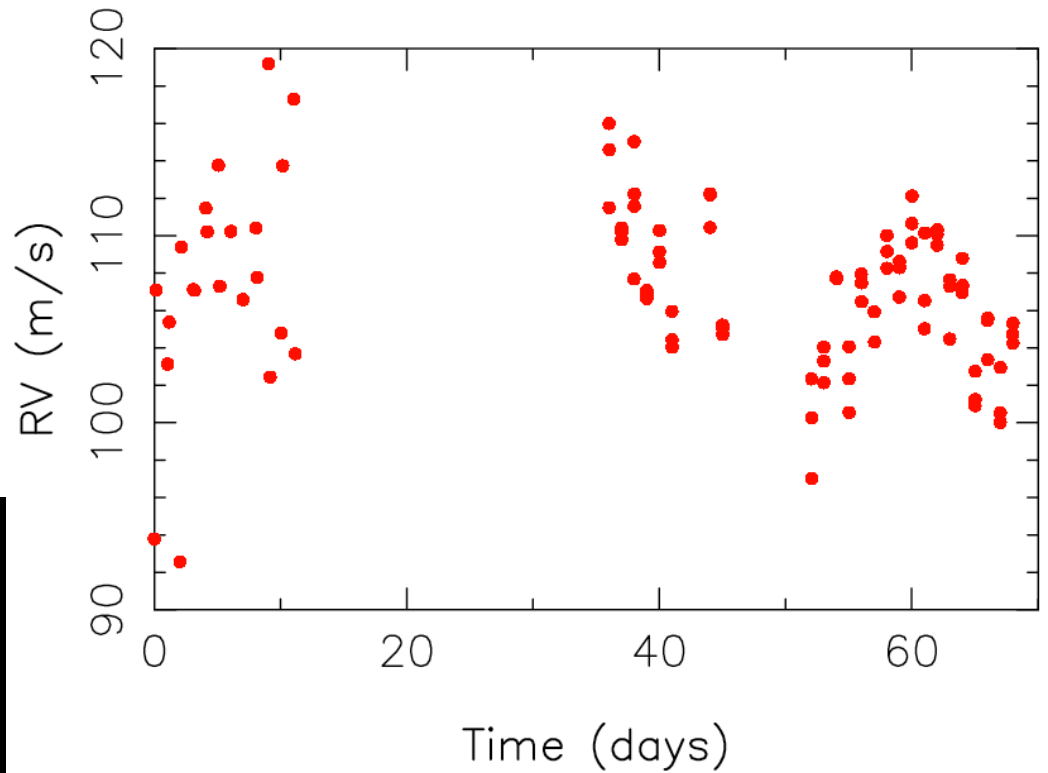
SDO/HMI Quick-Look Dopplergram: 2011.03.28_13:23:15_TAI



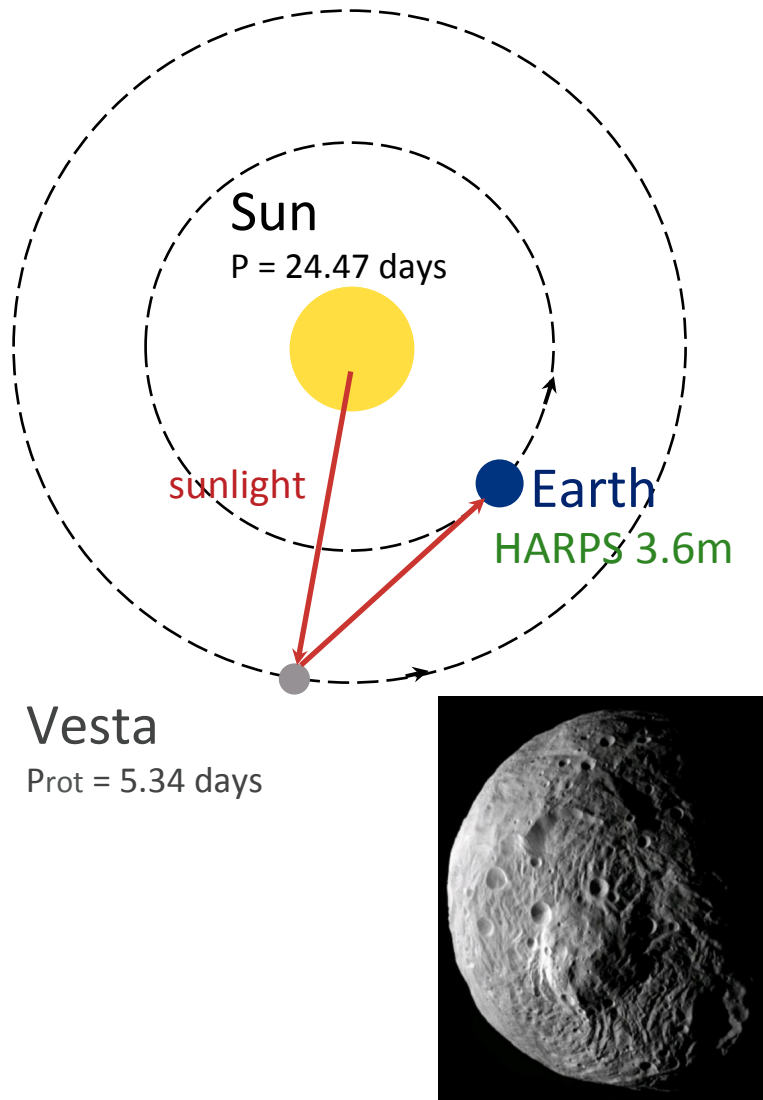
Using asteroid 4/Vesta to obtain the Sun's radial velocity variations



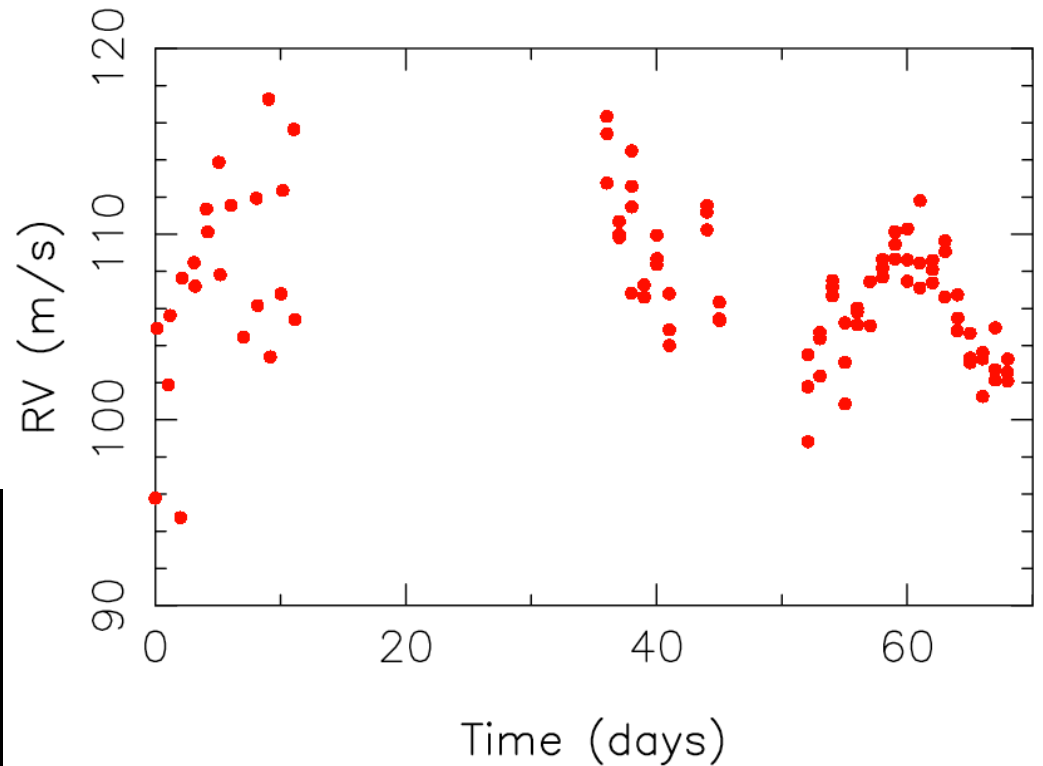
HARPS observations: 29 Sept. - 7 Dec. 2011



Using asteroid 4/Vesta to obtain the Sun's radial velocity variations



HARPS observations: 29 Sept. - 7 Dec. 2011
(Vesta rotation signal removed)

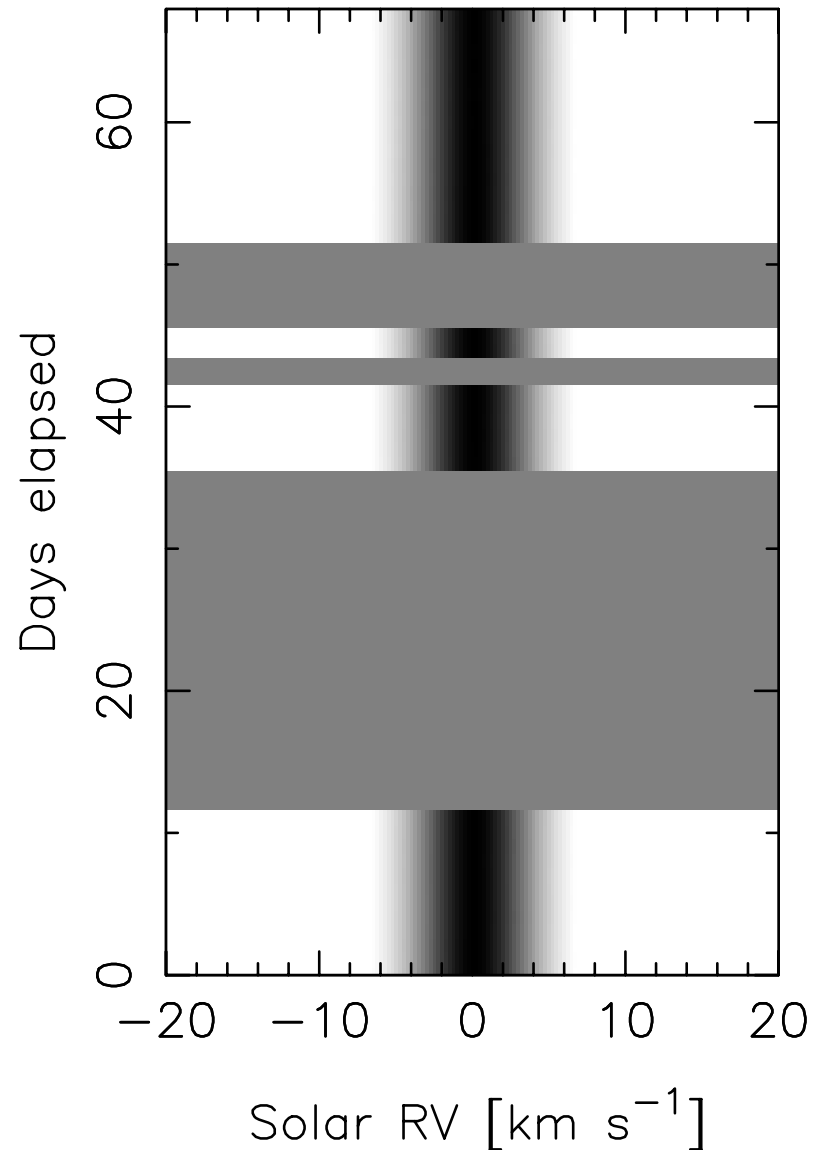


HARPS detects ... spots on the Sun!

HARPS CCF of asteroid 4 Vesta

2011 September 29 – December 7

(R Haywood et al, in prep.)

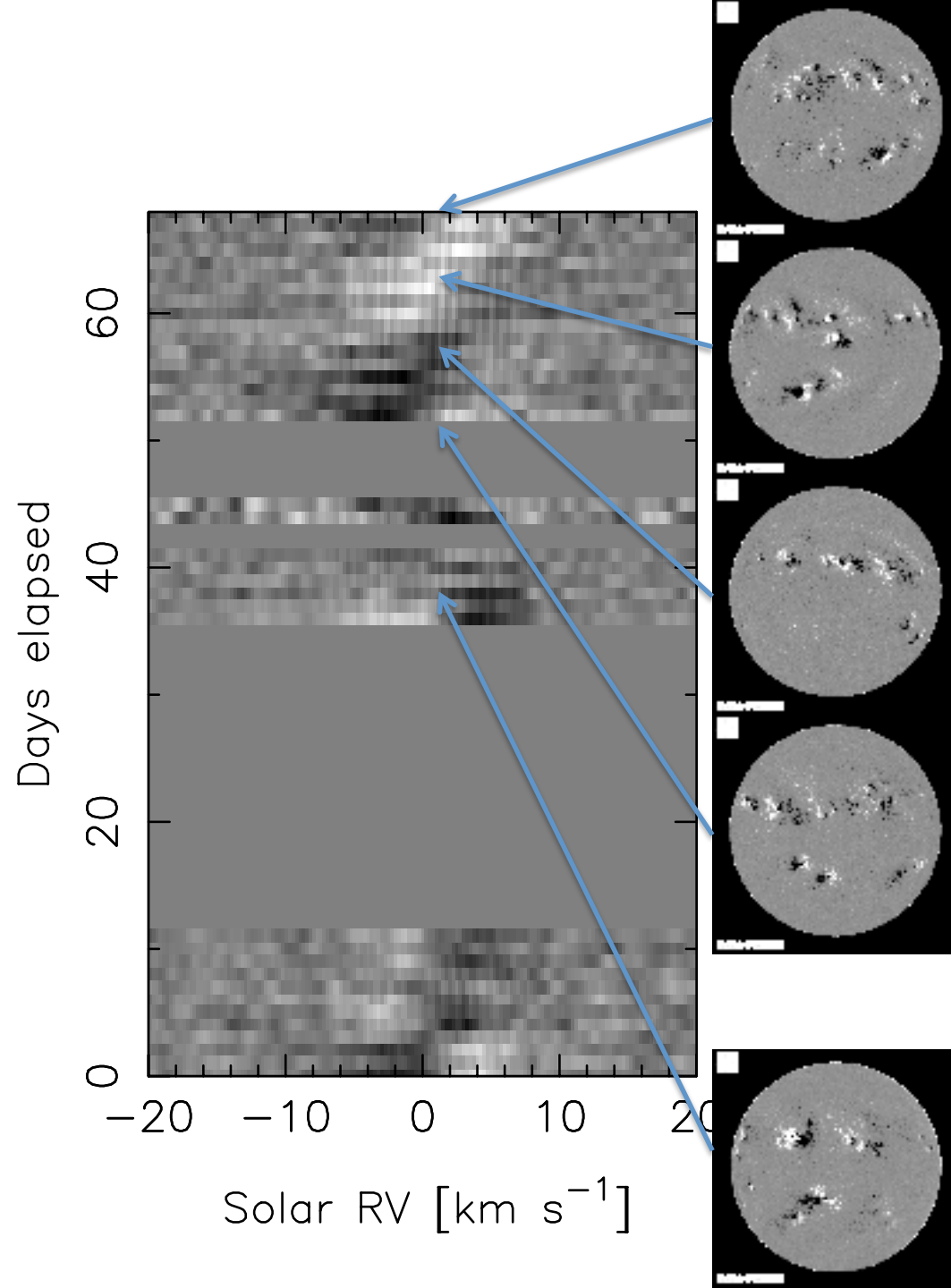


HARPS detects ... spots on the Sun!

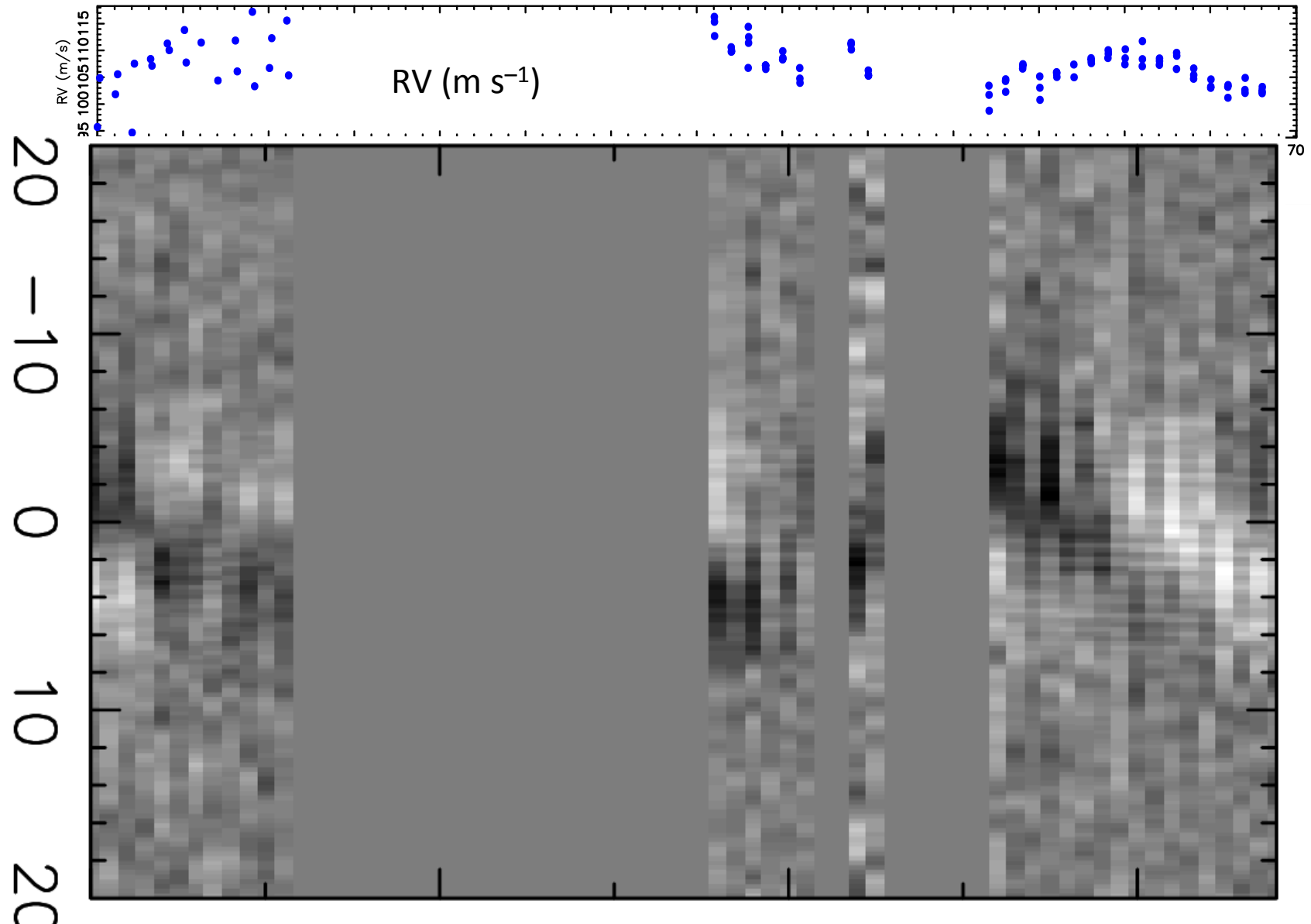
HARPS CCF of asteroid 4 Vesta

2011 September 29 – December 7

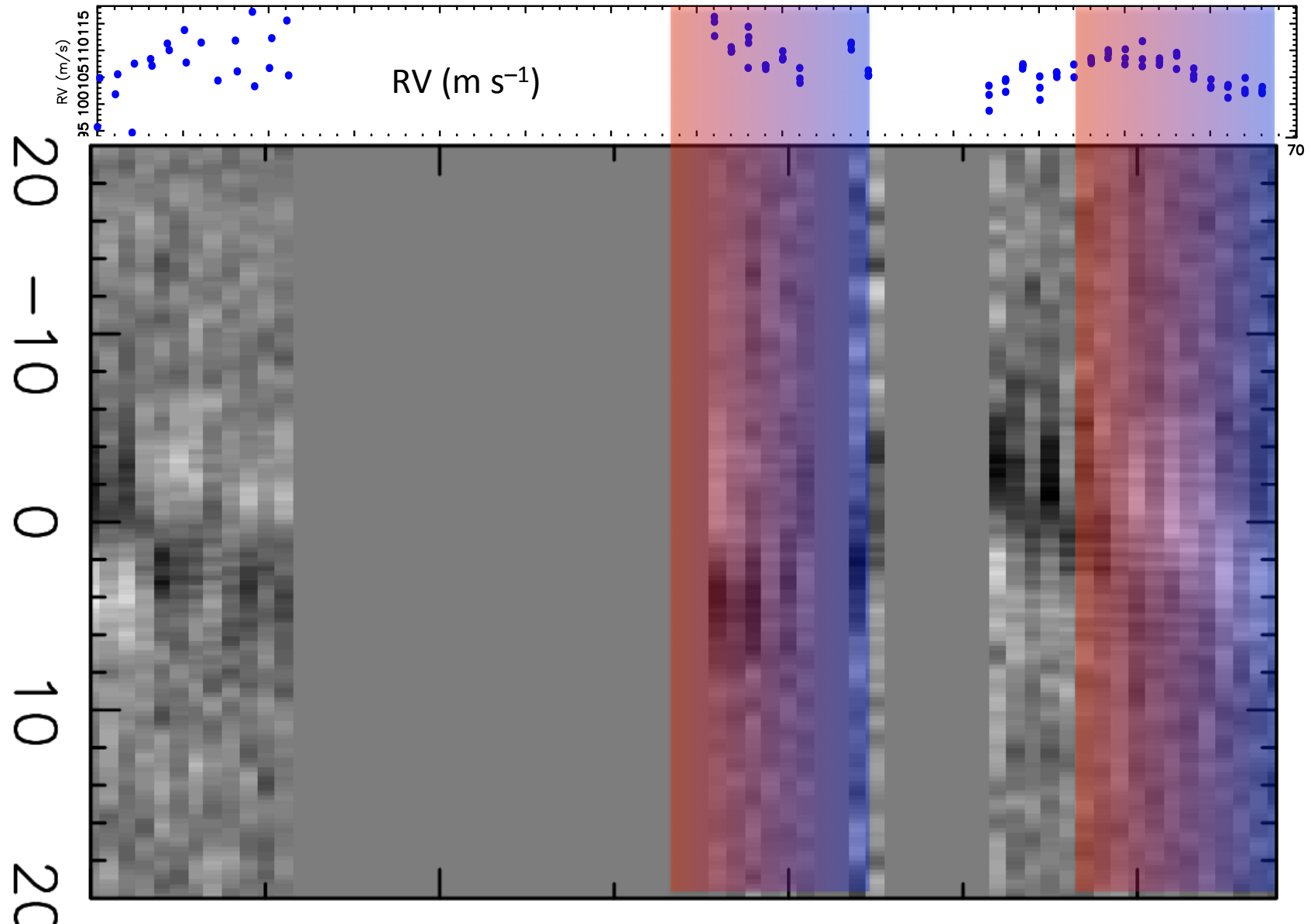
(R Haywood et al, in prep.)



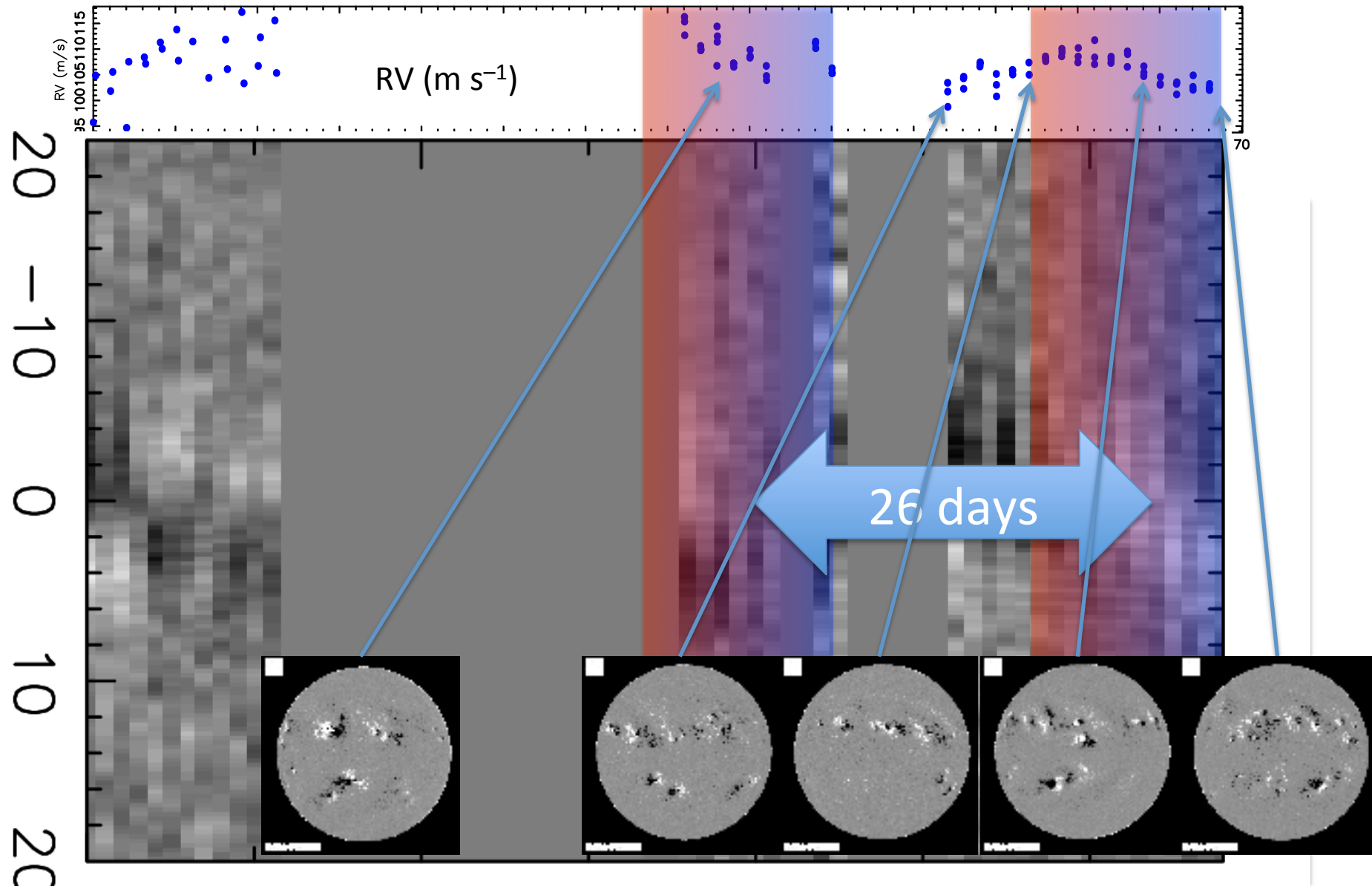
The Sun's radial-velocity jitter



The Sun's radial-velocity jitter

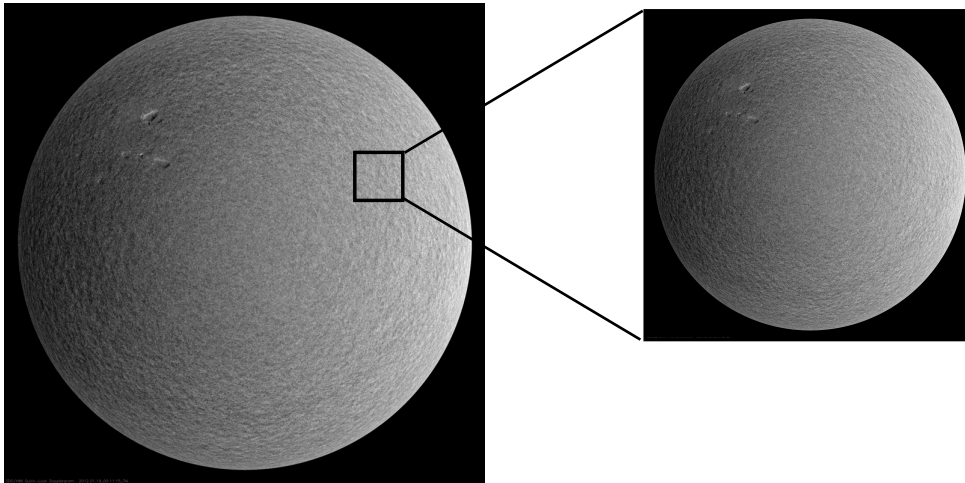
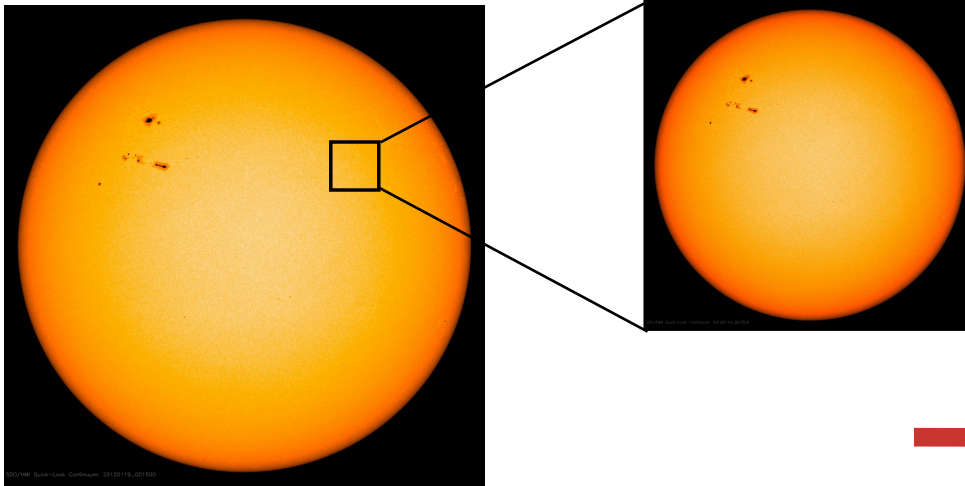


The Sun's radial-velocity jitter

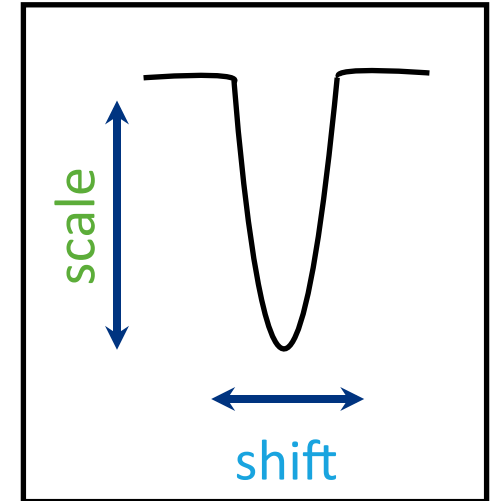


Next step: model line-profile distortions caused by sunspots, granulation, faculae,...

Continuum image
(scale)

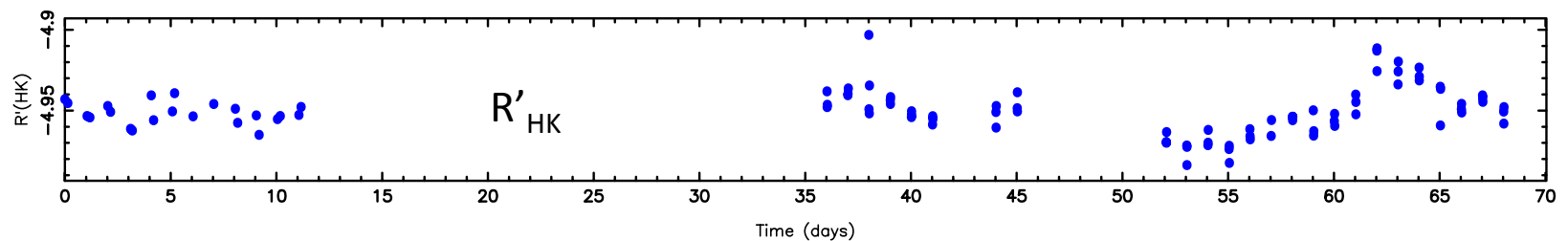
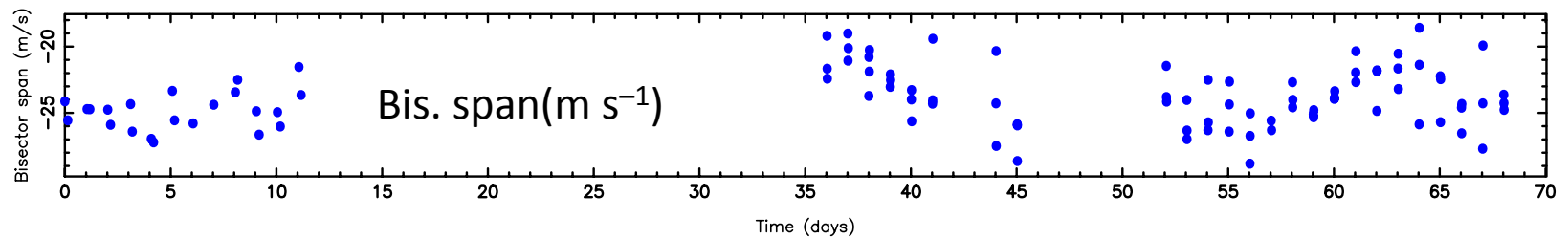
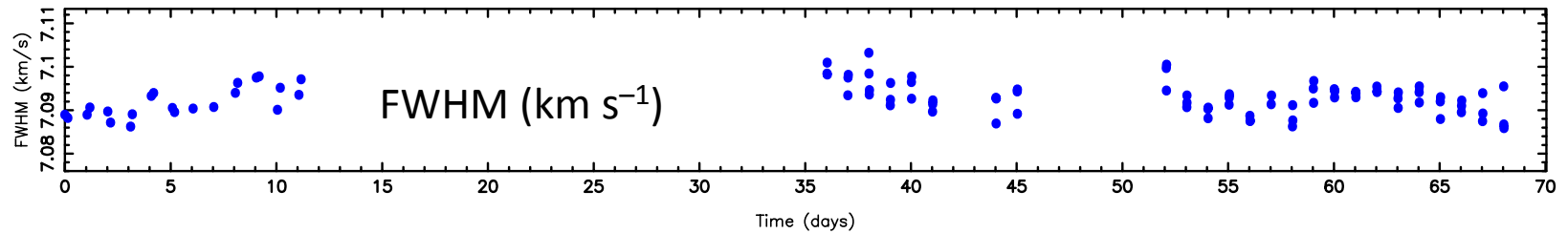
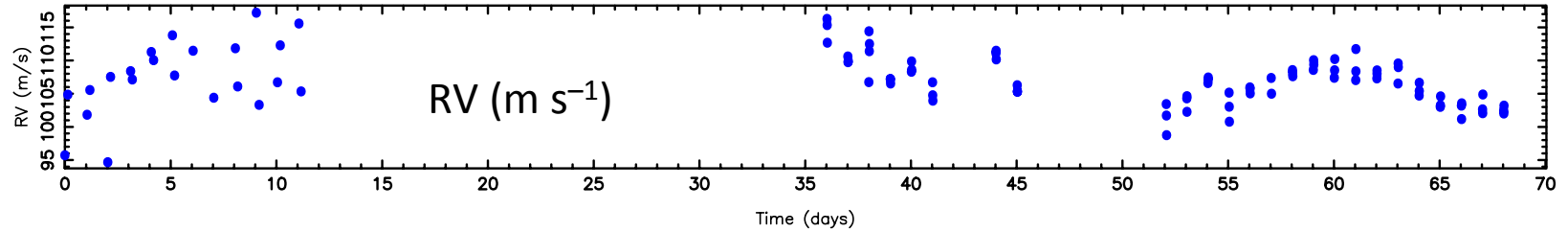


Doppler image
(shift)



Identify proxies to remove stellar jitter from exoplanet RV curves

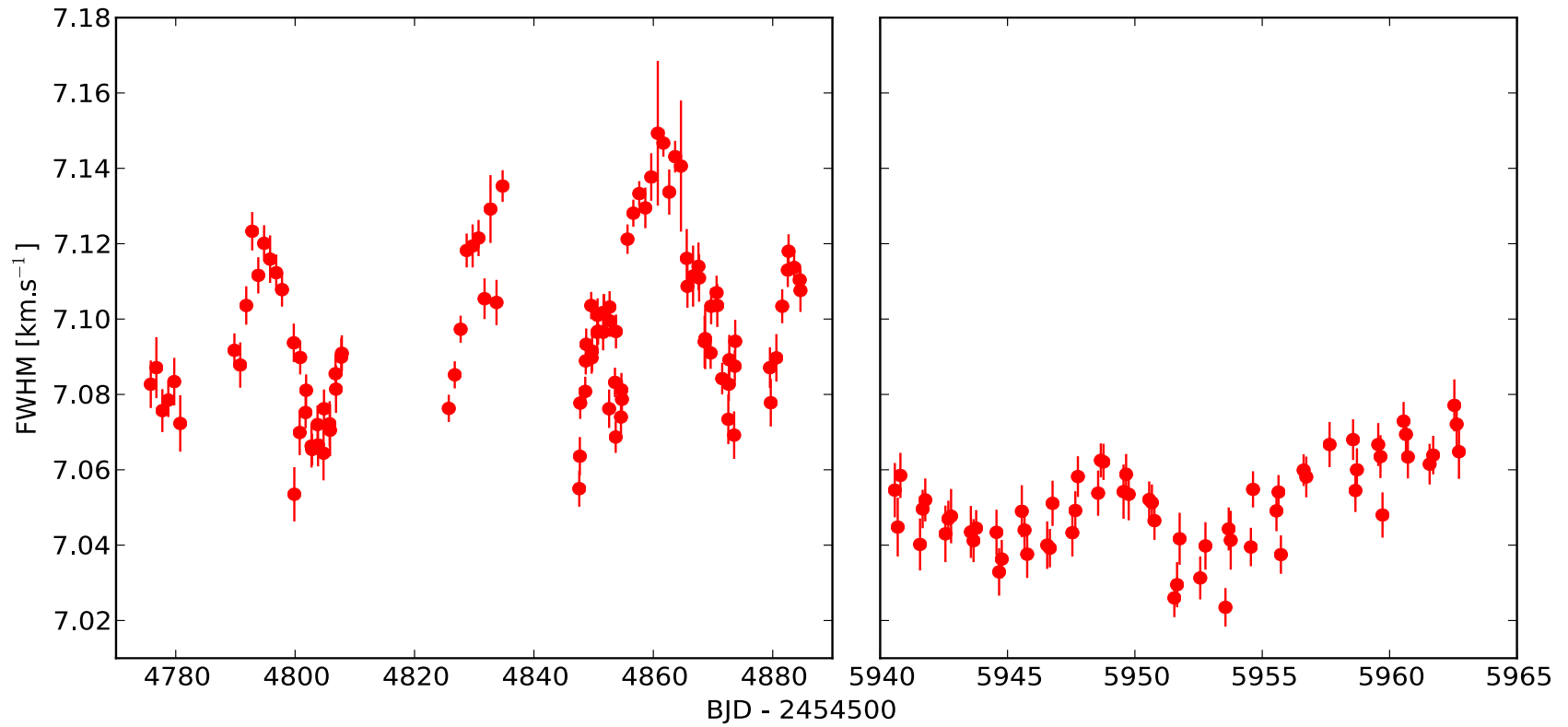
The Sun's radial-velocity jitter



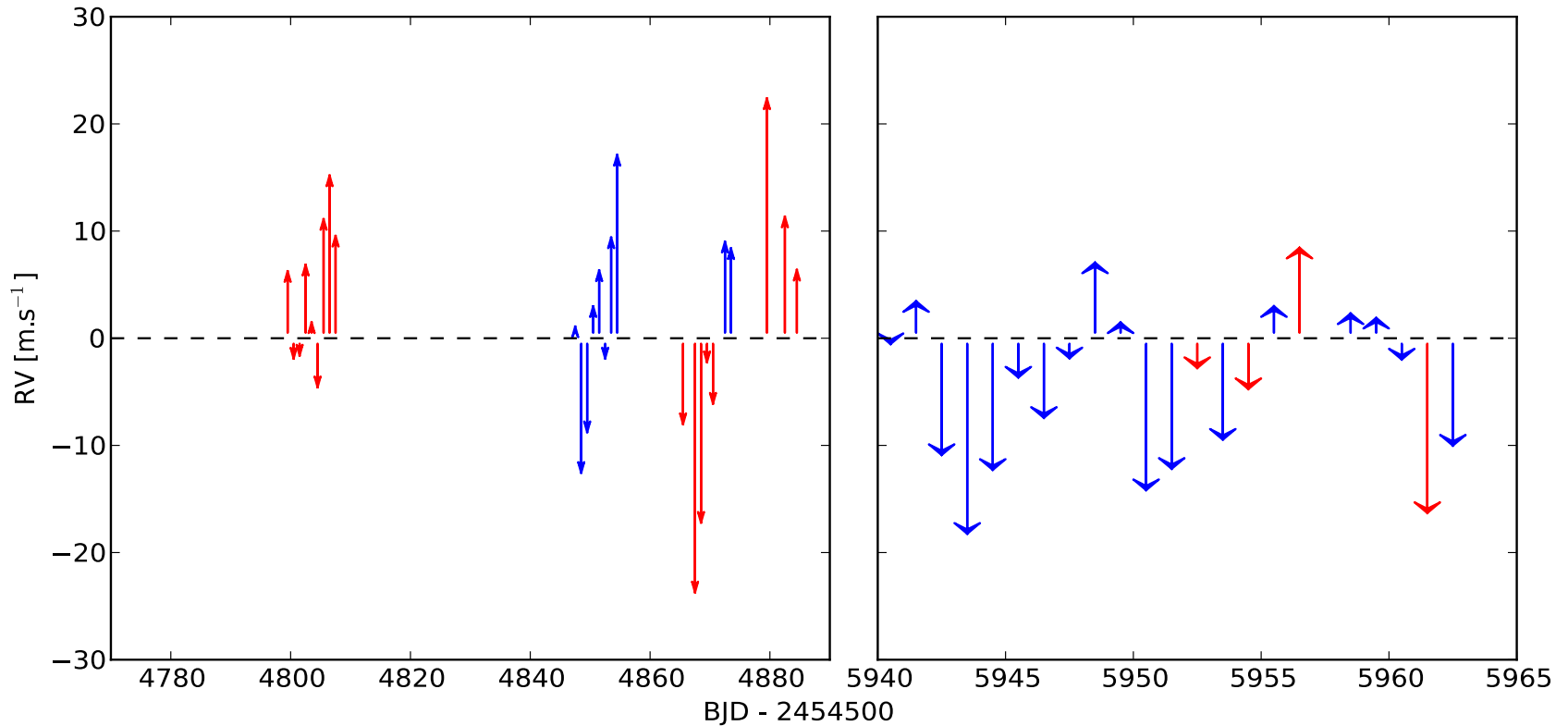
The Last Word (courtesy Stephen Kane)



CoRoT-7: FWHM of CCF dip

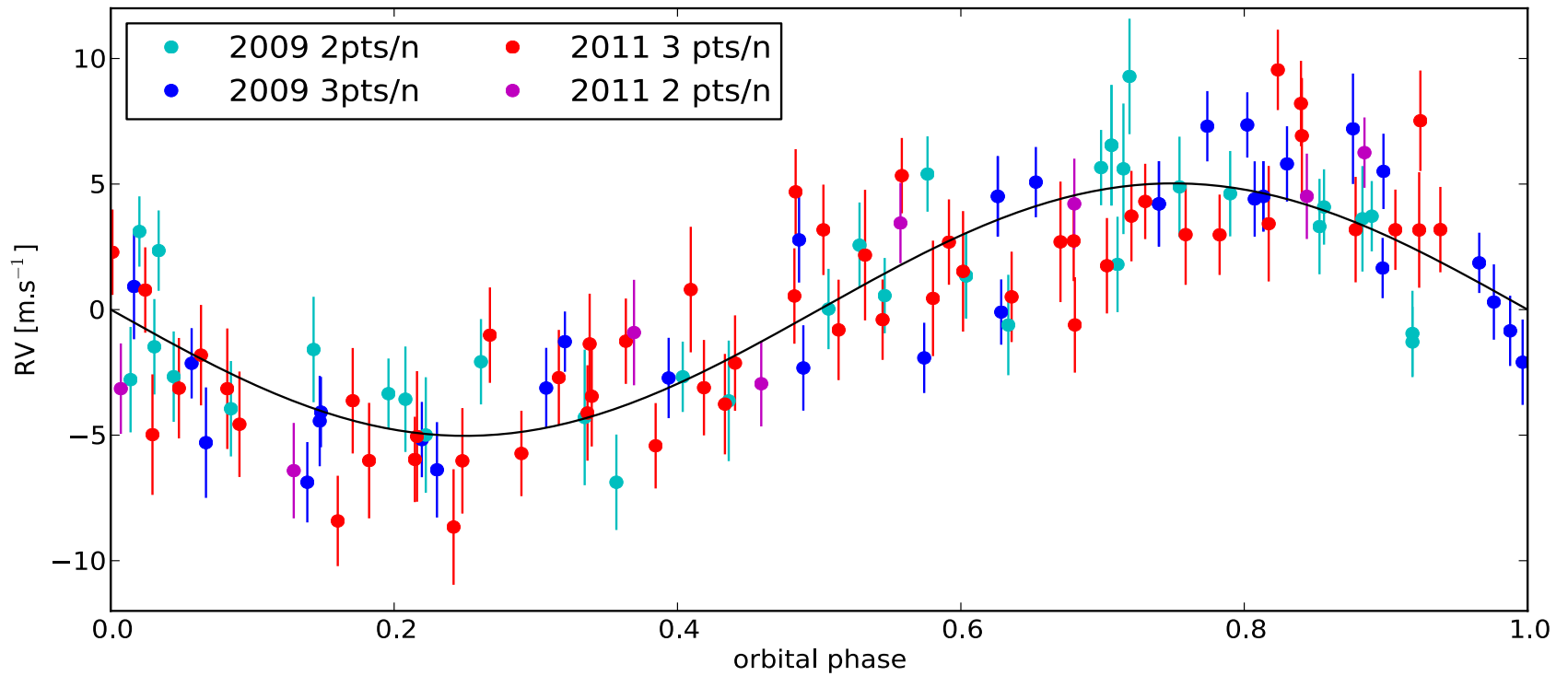


CoRoT-7: Nightly RV zero-point



Using technique of Hatzes et al (2010)
Red: 2 points/night; Blue = 3 points/night

Phased RV curve of CoRoT-7b



Gyrochronology

Asteroseismology

- See Bill Chaplin's talk on Friday!