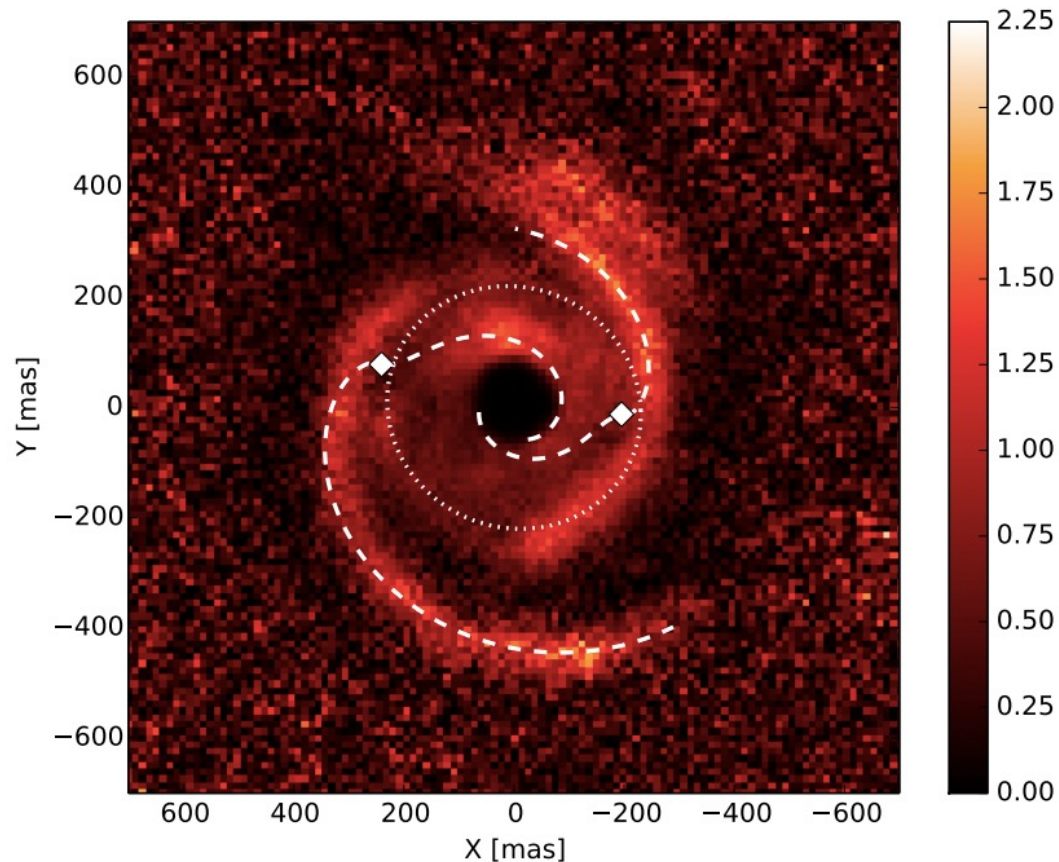


Instrumental Characterization of SCE_xAO VAMPIRES

Manxuan (Rebecca) Zhang, Maxwell Millar-Blanchaer, Boris Safonov,
Miles Lucas, Lucinda Lilley, Jaren Ashcraft, Barnaby Norris, Julien Lozi,
Olivier Guyon, Michael Bottom

Polarization of Circumstellar Disks

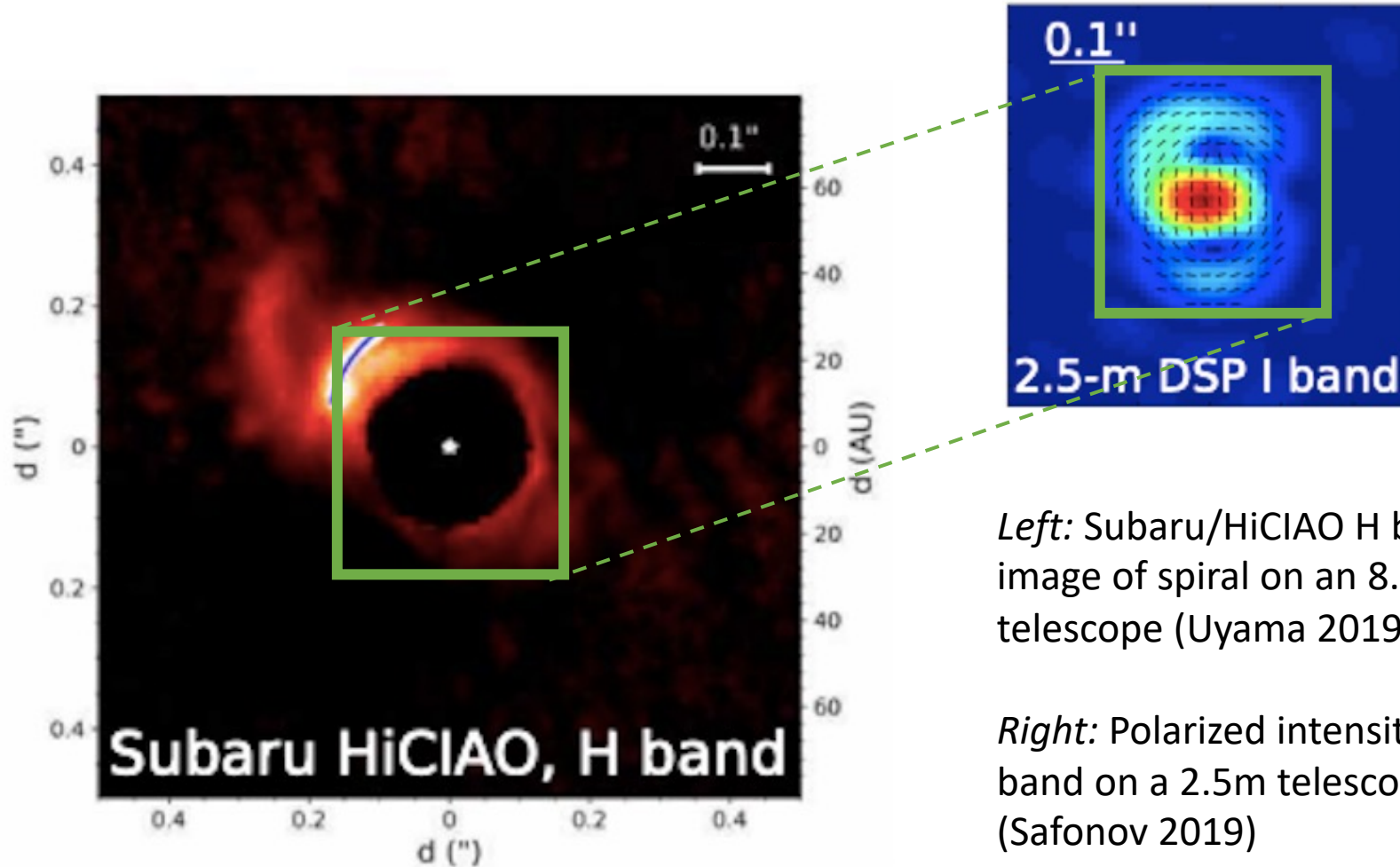


Advantages of Polarimetric Imaging

- Detecting fainter disks at smaller separations ($\sim 0.1''$)
- Well-suited to disks that appear face-on
- Characterization of scattering particles

Polarized intensity showing spiral arms of MWC 758 with SPHERE (Benisty 2014)

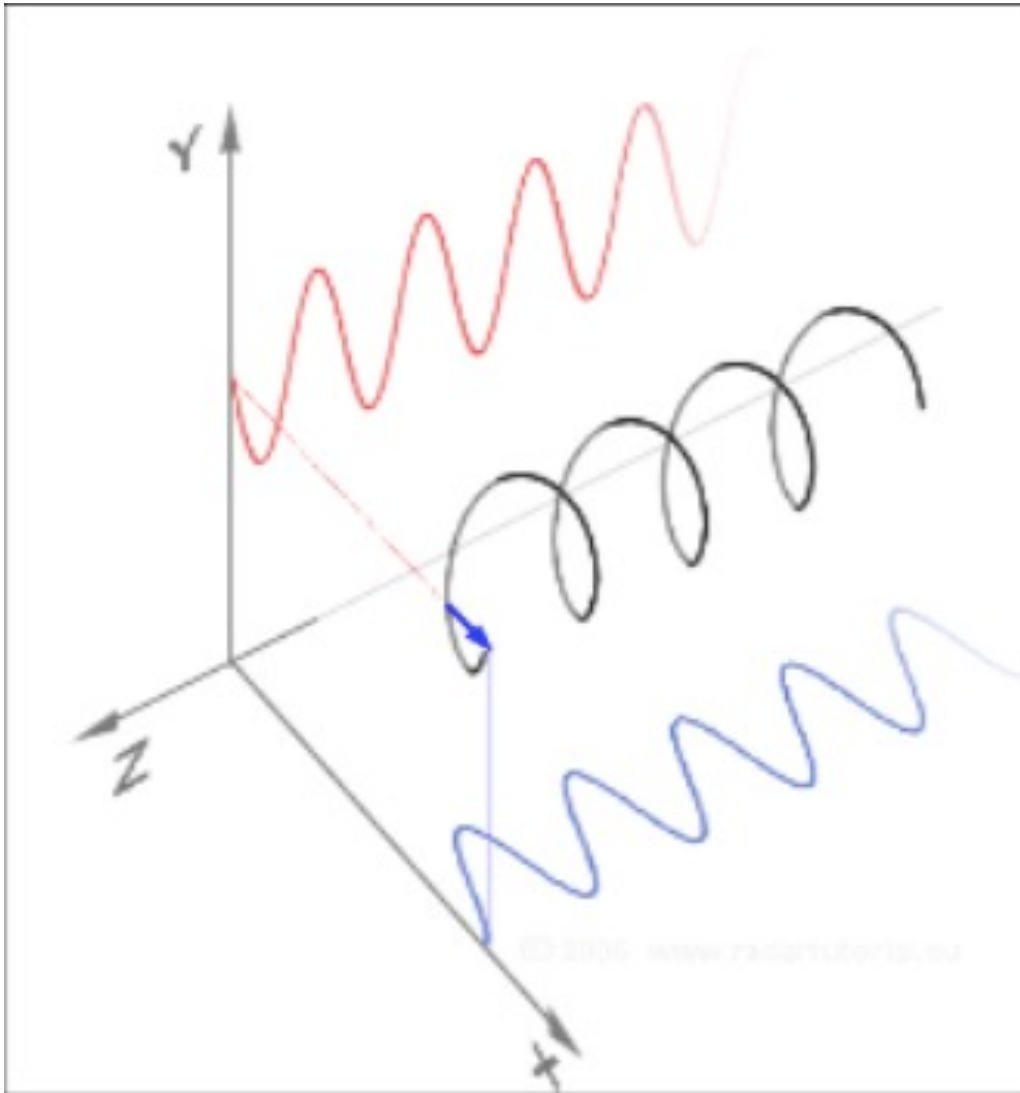
CQ Tau Disk



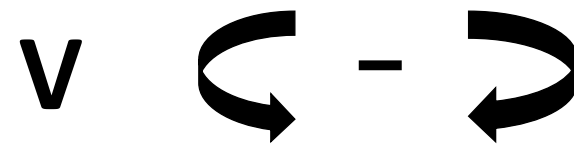
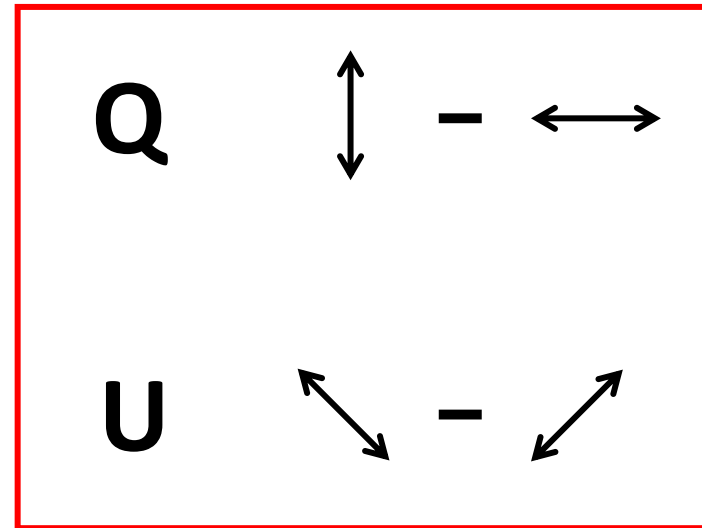
Left: Subaru/HiCIAO H band image of spiral on an 8.2m telescope (Uyama 2019)

Right: Polarized intensity in I band on a 2.5m telescope (Safonov 2019)

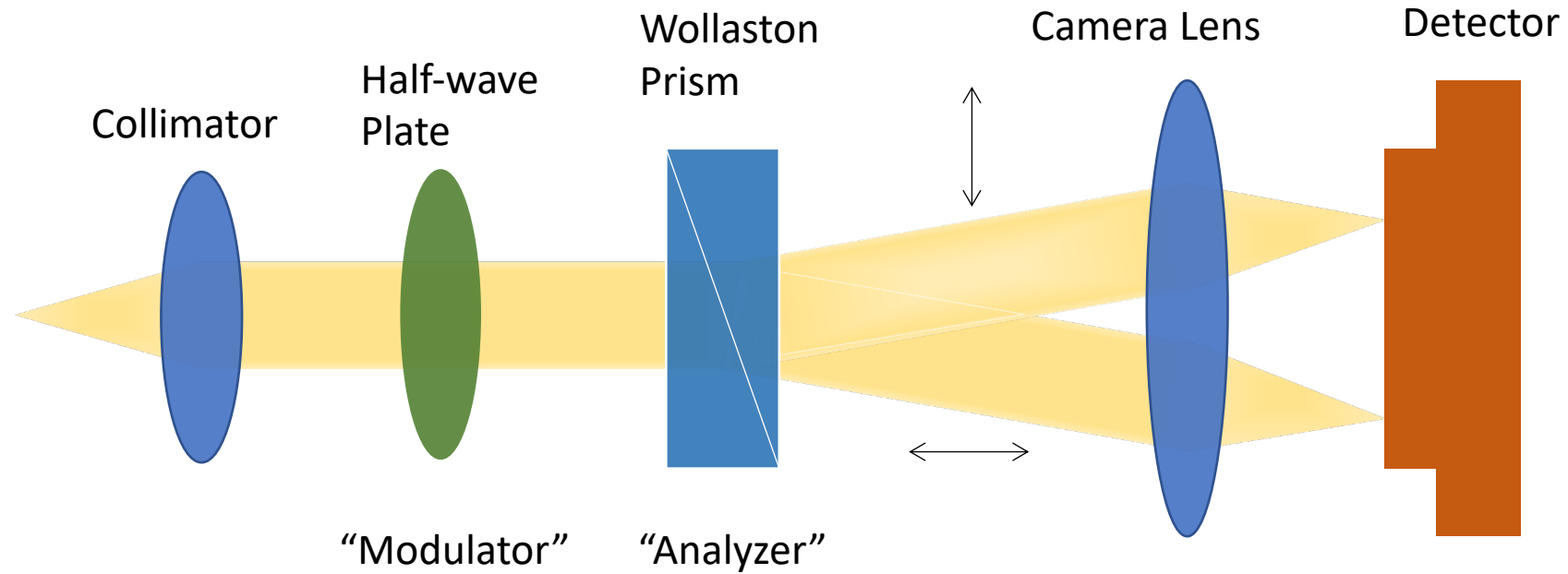
Polarimetry Basics



I Total Intensity

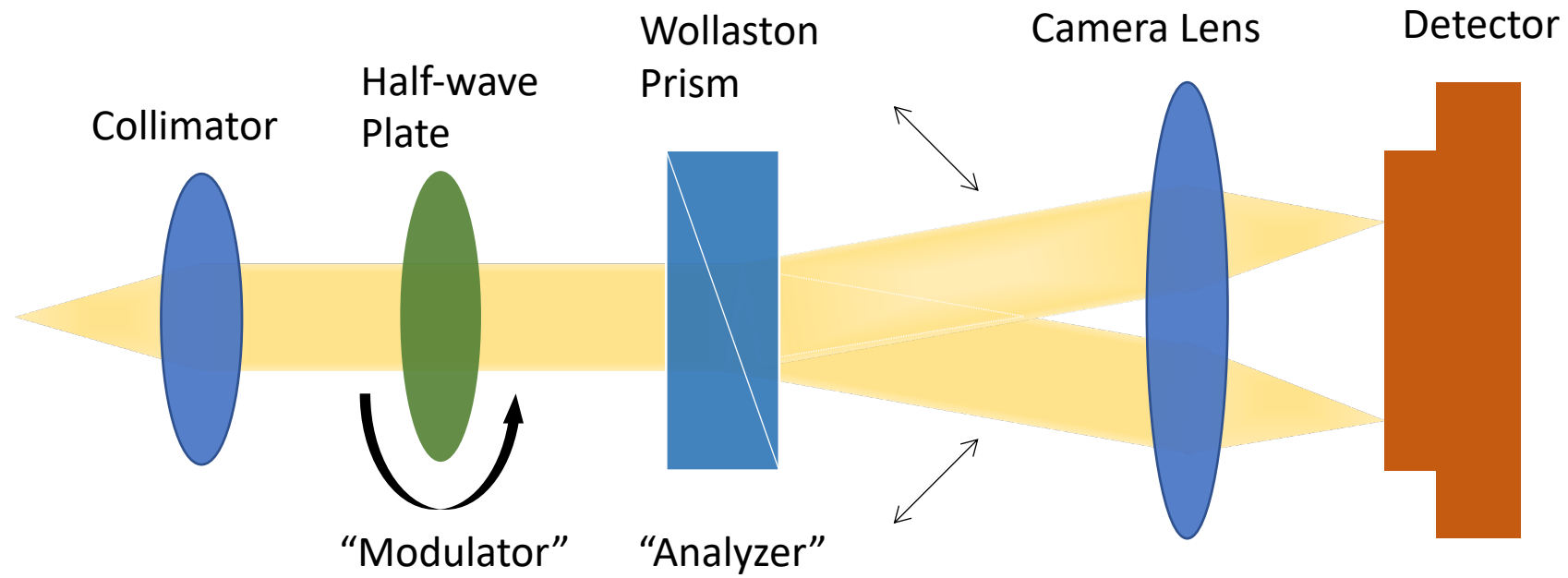


Measuring Polarization



$$\begin{aligned} I &= \begin{array}{c} \updownarrow \\ \star \\ \updownarrow \end{array} + \begin{array}{c} \leftarrow\rightarrow \\ \star \\ \leftarrow\rightarrow \end{array} \\ Q &= \begin{array}{c} \updownarrow \\ \star \\ \updownarrow \end{array} - \begin{array}{c} \leftarrow\rightarrow \\ \star \\ \leftarrow\rightarrow \end{array} \end{aligned}$$

Measuring Polarization



$$\mathbf{U} = \text{Star} - \text{Star}$$

The equation shows the Stokes parameter U as the difference between two stars. Each star has a double-headed arrow inside, representing the polarization state.

Mueller Matrix Representation

$$\begin{pmatrix} I_{\text{in}} \\ Q_{\text{in}} \\ U_{\text{in}} \\ V_{\text{in}} \end{pmatrix}$$

$$\mathbf{S}_{\text{in}}$$

Mueller Matrix Representation

$$\begin{pmatrix} I \rightarrow I & Q \rightarrow I & U \rightarrow I & V \rightarrow I \\ I \rightarrow Q & Q \rightarrow Q & U \rightarrow Q & V \rightarrow Q \\ I \rightarrow U & Q \rightarrow U & U \rightarrow U & V \rightarrow U \\ I \rightarrow V & Q \rightarrow V & U \rightarrow V & V \rightarrow V \end{pmatrix} \begin{pmatrix} I_{\text{in}} \\ Q_{\text{in}} \\ U_{\text{in}} \\ V_{\text{in}} \end{pmatrix}$$

\mathbf{M}_{comp}

\mathbf{S}_{in}

Mueller Matrix Representation

$$\begin{pmatrix} I \rightarrow I & Q \rightarrow I & U \rightarrow I & V \rightarrow I \\ I \rightarrow Q & Q \rightarrow Q & U \rightarrow Q & V \rightarrow Q \\ I \rightarrow U & Q \rightarrow U & U \rightarrow U & V \rightarrow U \\ I \rightarrow V & Q \rightarrow V & U \rightarrow V & V \rightarrow V \end{pmatrix} \begin{pmatrix} I_{\text{in}} \\ Q_{\text{in}} \\ U_{\text{in}} \\ V_{\text{in}} \end{pmatrix}$$

Instrumental
Polarization

\mathbf{M}_{comp}

\mathbf{S}_{in}

Mueller Matrix Representation

$$\begin{pmatrix} I \rightarrow I & Q \rightarrow I & U \rightarrow I & V \rightarrow I \\ I \rightarrow Q & Q \rightarrow Q & U \rightarrow Q & V \rightarrow Q \\ I \rightarrow U & Q \rightarrow U & U \rightarrow U & V \rightarrow U \\ I \rightarrow V & Q \rightarrow V & U \rightarrow V & V \rightarrow V \end{pmatrix} \begin{pmatrix} I_{\text{in}} \\ Q_{\text{in}} \\ U_{\text{in}} \\ V_{\text{in}} \end{pmatrix}$$

Instrumental
Polarization

Crosstalk

\mathbf{M}_{comp}

\mathbf{S}_{in}

Mueller Matrix Representation

$$\begin{pmatrix} I_{\text{out}} \\ Q_{\text{out}} \\ U_{\text{out}} \\ V_{\text{out}} \end{pmatrix} = \begin{pmatrix} I \rightarrow I & Q \rightarrow I & U \rightarrow I & V \rightarrow I \\ I \rightarrow Q & Q \rightarrow Q & U \rightarrow Q & V \rightarrow Q \\ I \rightarrow U & Q \rightarrow U & U \rightarrow U & V \rightarrow U \\ I \rightarrow V & Q \rightarrow V & U \rightarrow V & V \rightarrow V \end{pmatrix} \begin{pmatrix} I_{\text{in}} \\ Q_{\text{in}} \\ U_{\text{in}} \\ V_{\text{in}} \end{pmatrix}$$

$\mathbf{S}_{\text{out}} \qquad \qquad \qquad \mathbf{M}_{\text{comp}} \qquad \qquad \qquad \mathbf{S}_{\text{in}}$

Instrumental Polarization Crosstalk

Mueller Matrix Representation

$$M_{retarder} = \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & \cos \phi & \sin \phi \\ 0 & 0 & -\sin \phi & \cos \phi \end{pmatrix}$$

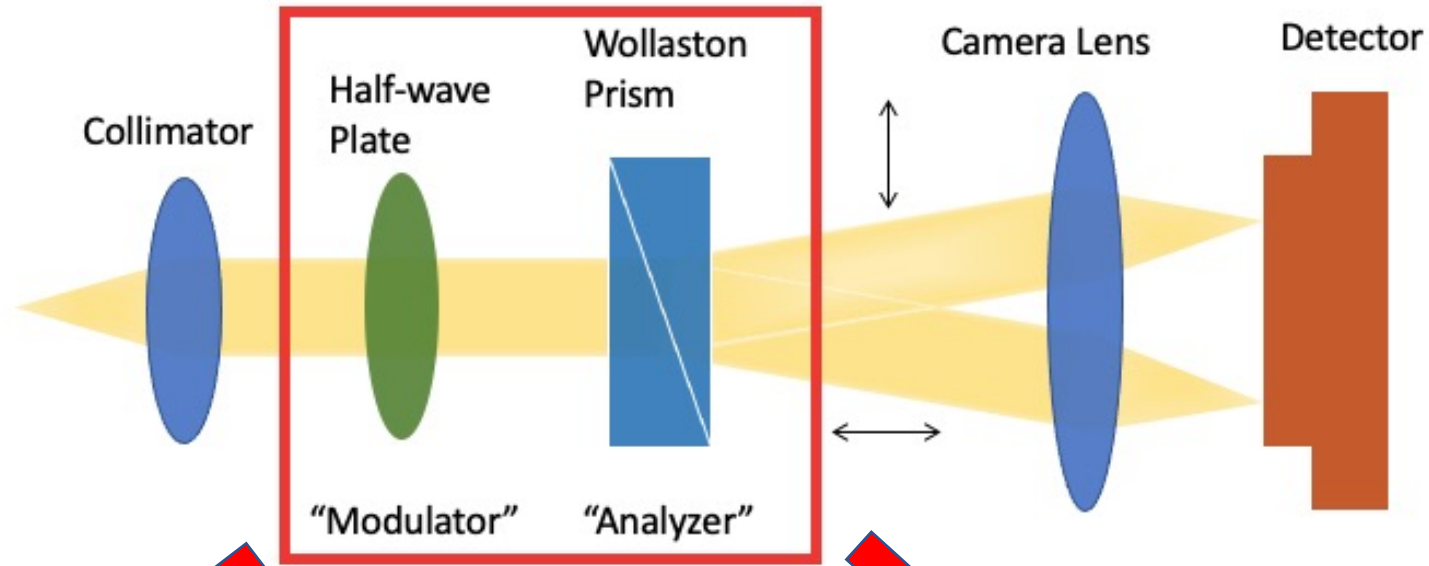
Mueller Matrix Representation

$$M_{retarder} = \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & \cos \phi & \sin \phi \\ 0 & 0 & -\sin \phi & \cos \phi \end{pmatrix}$$

$$M_{diattenuator} = \begin{pmatrix} 1 & \varepsilon & 0 & 0 \\ \varepsilon & 1 & 0 & 0 \\ 0 & 0 & \sqrt{1 - \varepsilon^2} & \sqrt{1 - \varepsilon^2} \\ 0 & 0 & -\sqrt{1 - \varepsilon^2} & \sqrt{1 - \varepsilon^2} \end{pmatrix}$$

Mueller Matrix Representation

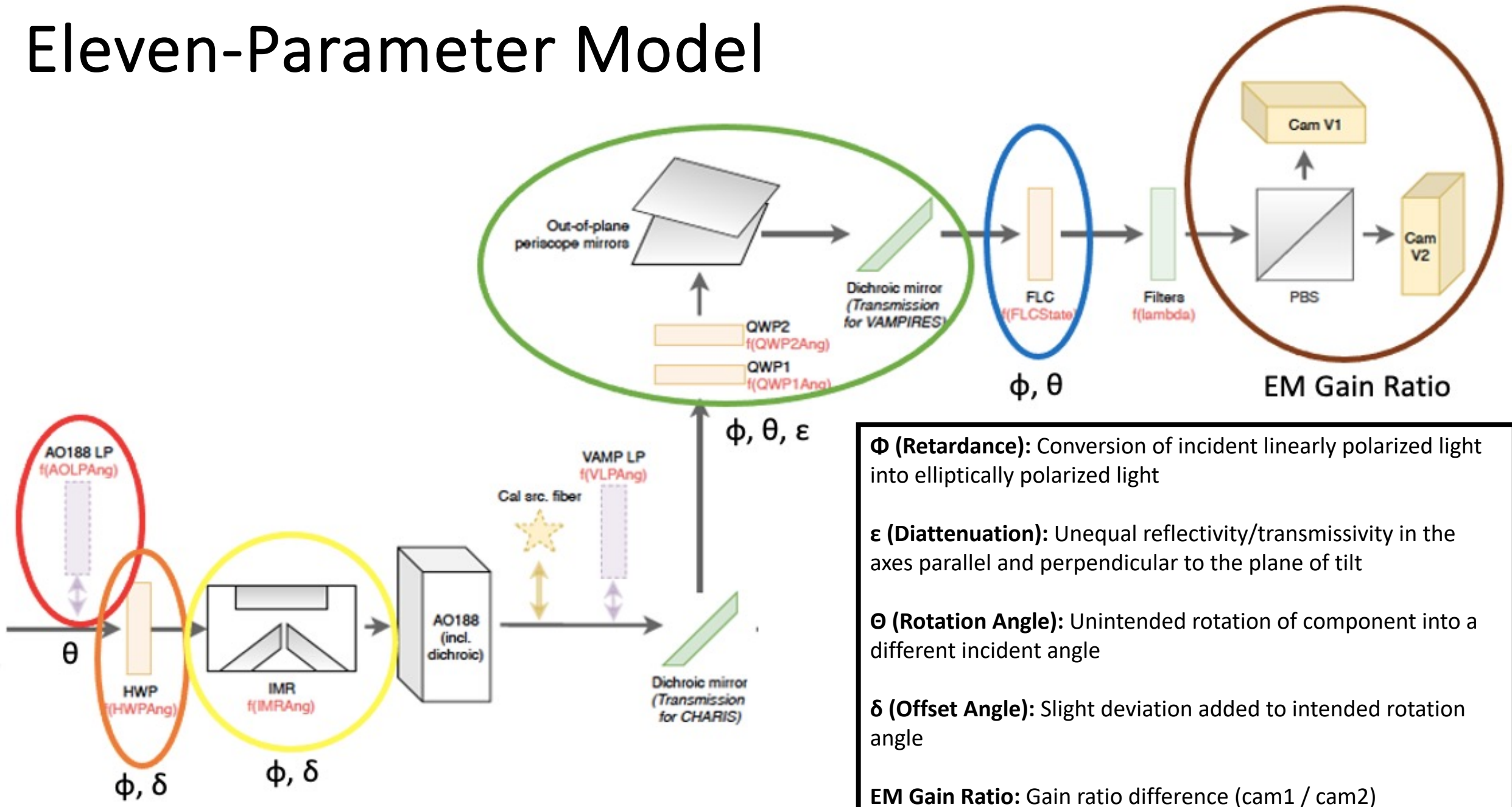
$$\mathbf{S}_{out} = \mathbf{M}_{Wollaston} \cdot \mathbf{M}_{HWP} \cdot \mathbf{S}_{in}$$



$$\mathbf{M}_{HWP} = \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & -1 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix}$$

$$\mathbf{M}_{Wollaston} = \frac{1}{2} \begin{pmatrix} 1 & \pm 1 & 0 & 0 \\ \pm 1 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{pmatrix}$$

Eleven-Parameter Model



Φ (Retardance): Conversion of incident linearly polarized light into elliptically polarized light

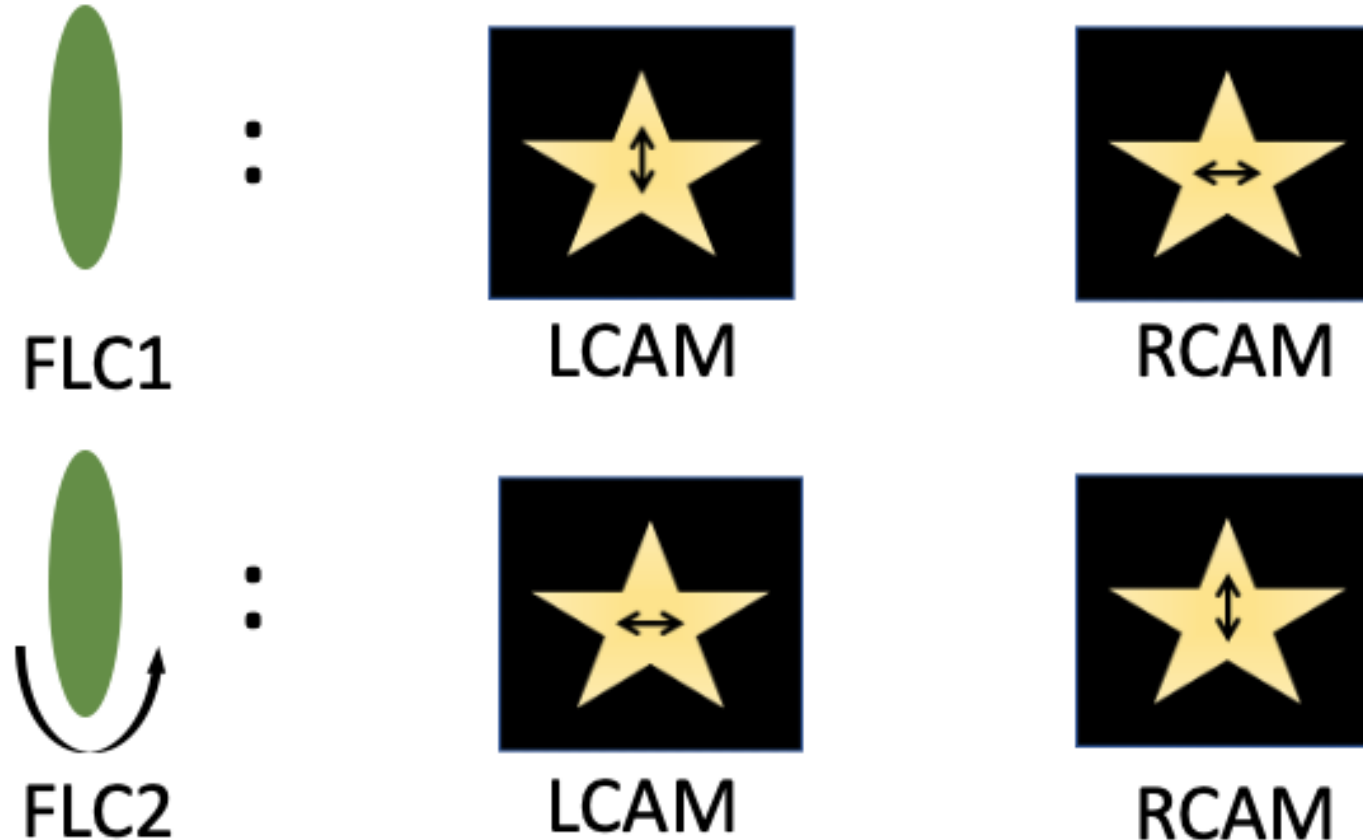
ϵ (Diattenuation): Unequal reflectivity/transmissivity in the axes parallel and perpendicular to the plane of tilt

Θ (Rotation Angle): Unintended rotation of component into a different incident angle

δ (Offset Angle): Slight deviation added to intended rotation angle

EM Gain Ratio: Gain ratio difference (cam1 / cam2)

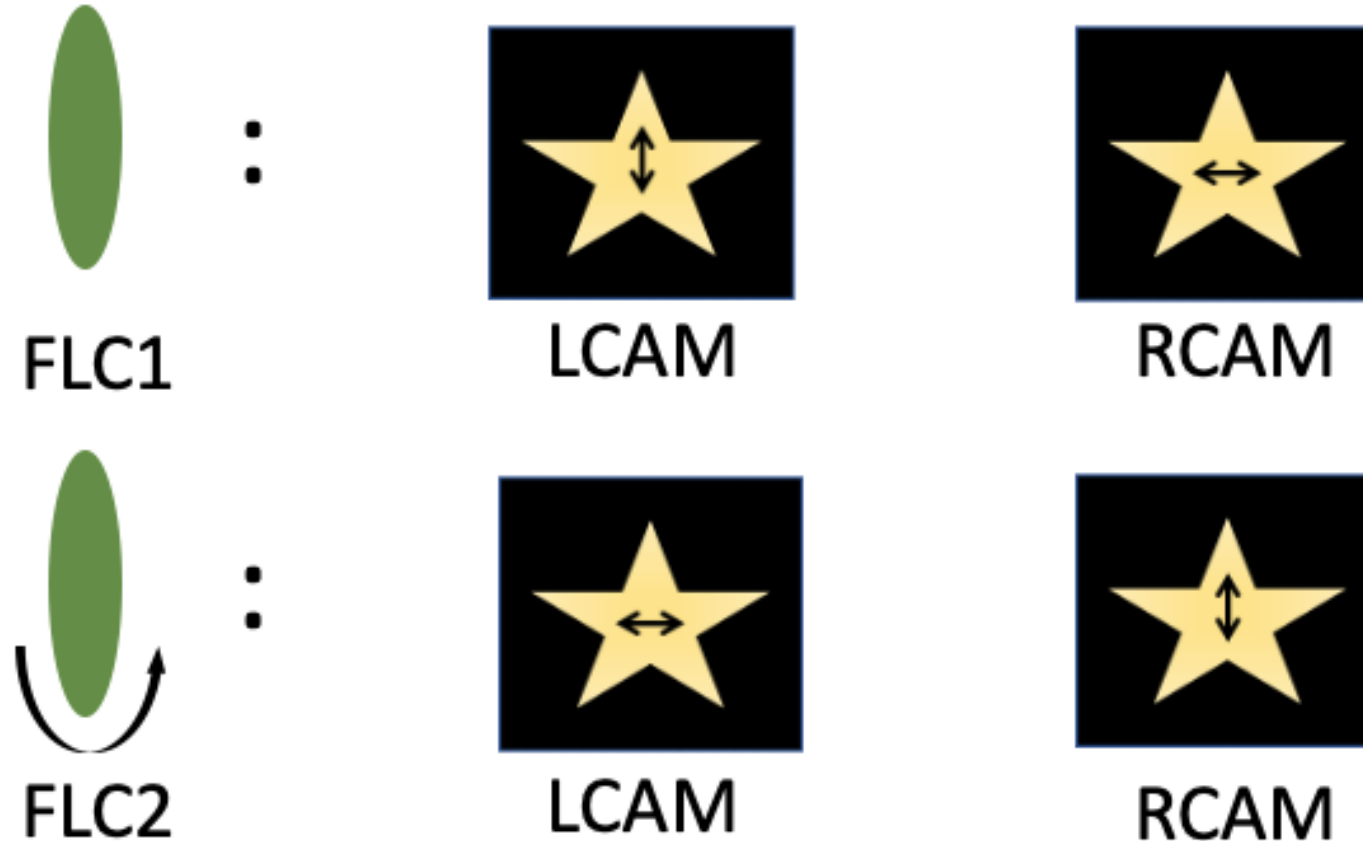
Internal Lab Calibrations: Expressions



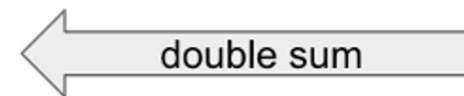
$$D = (L1 - R1) - (L2 - R2)$$

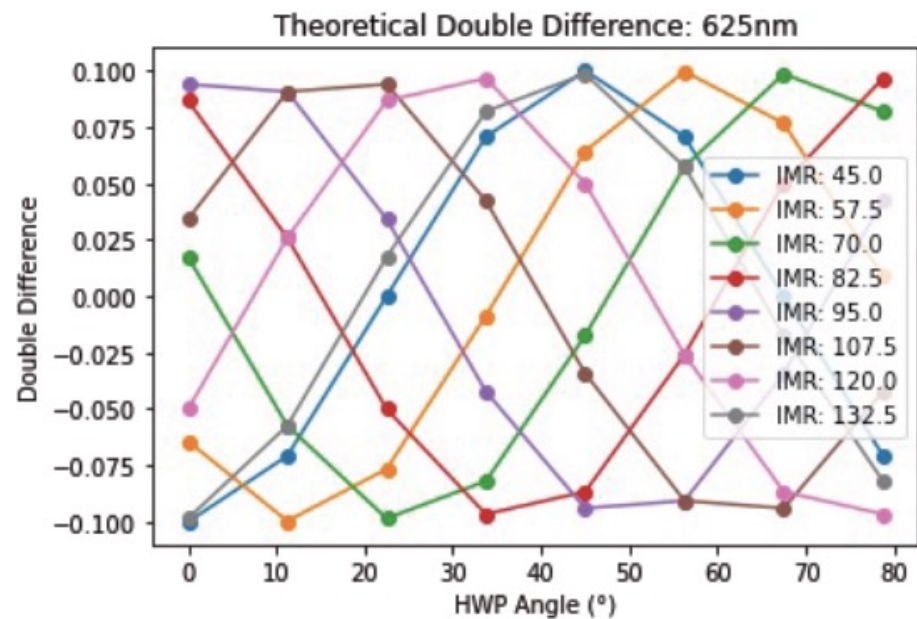
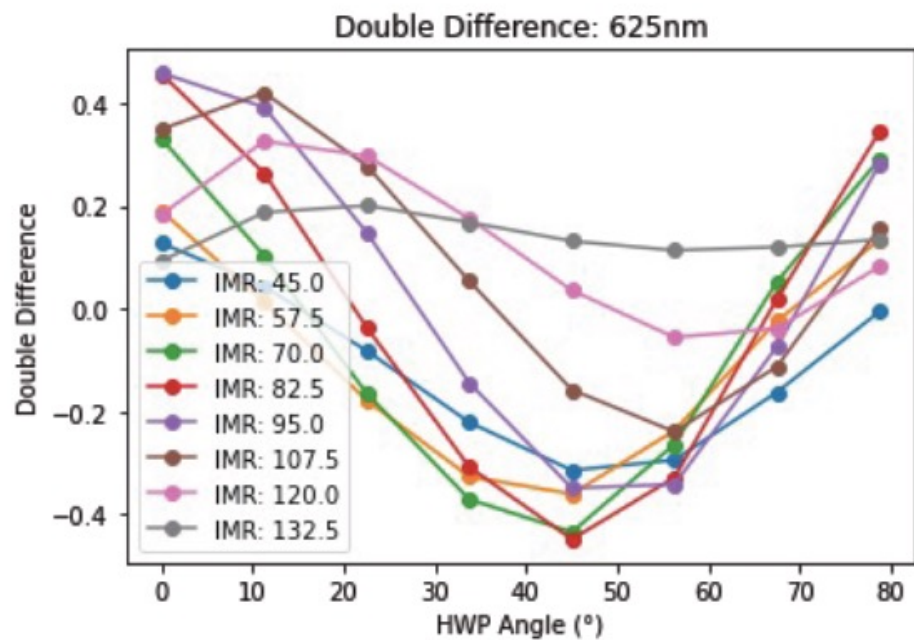
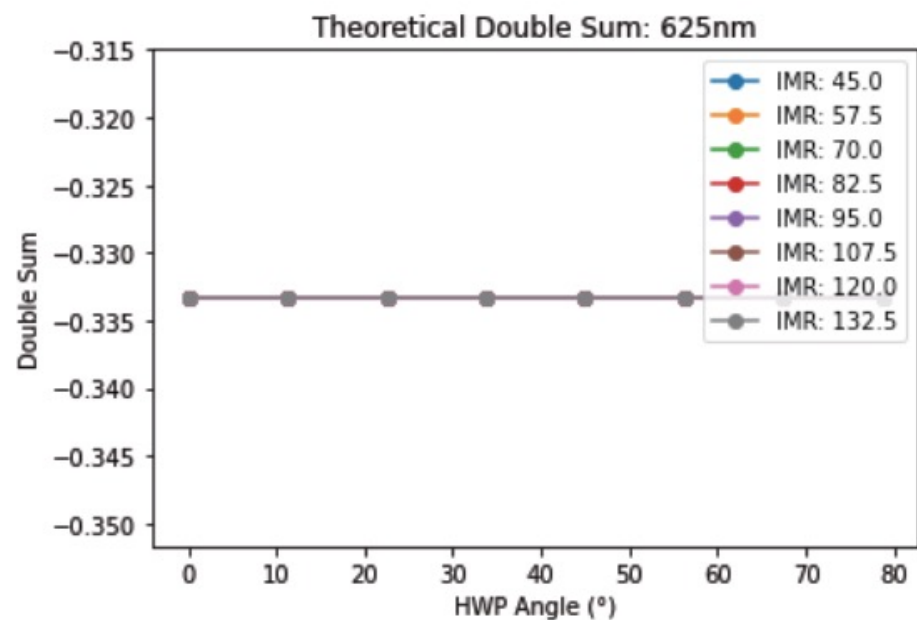
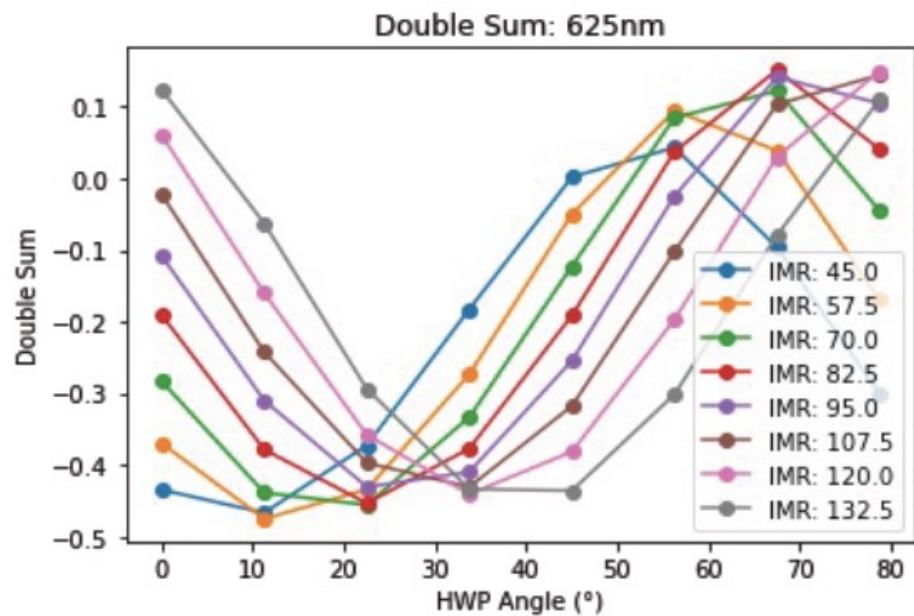
← double difference

Internal Lab Calibrations: Expressions

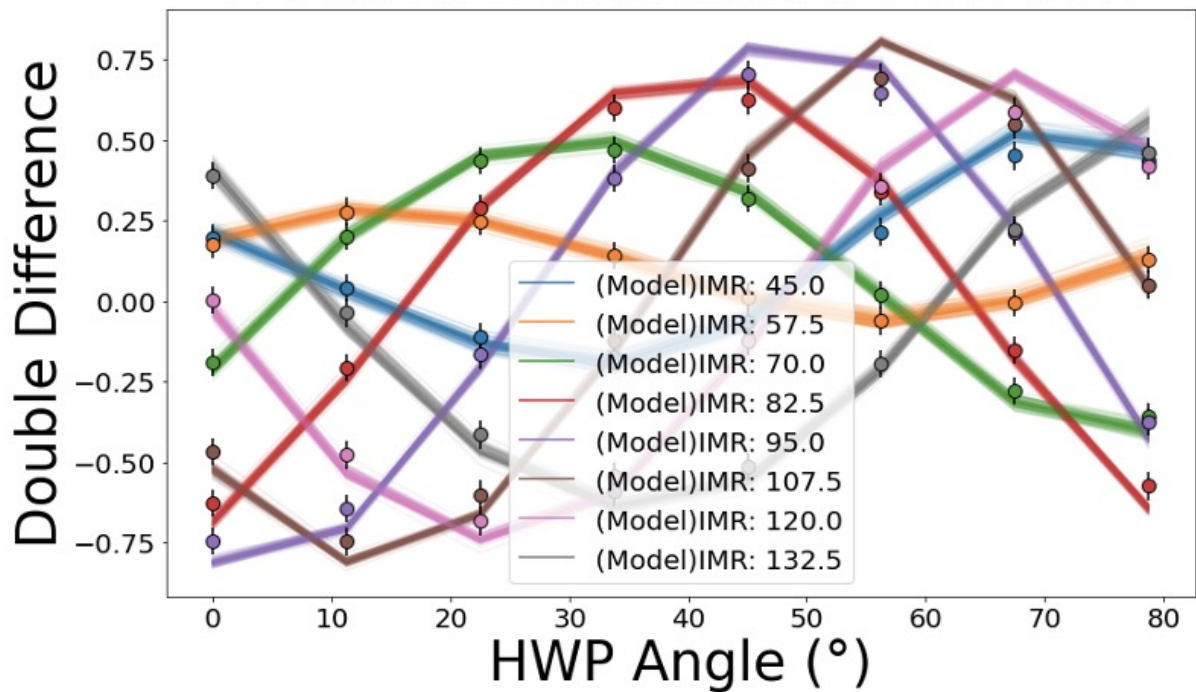


$$S = (L1 - R1) + (L2 - R2)$$

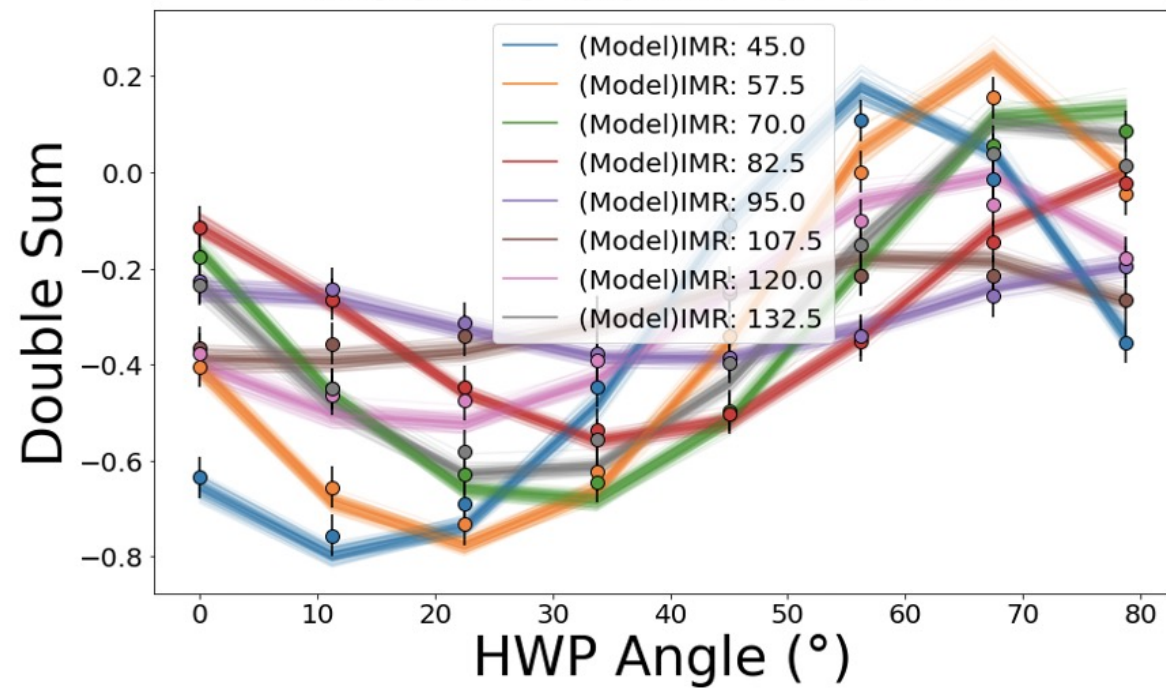


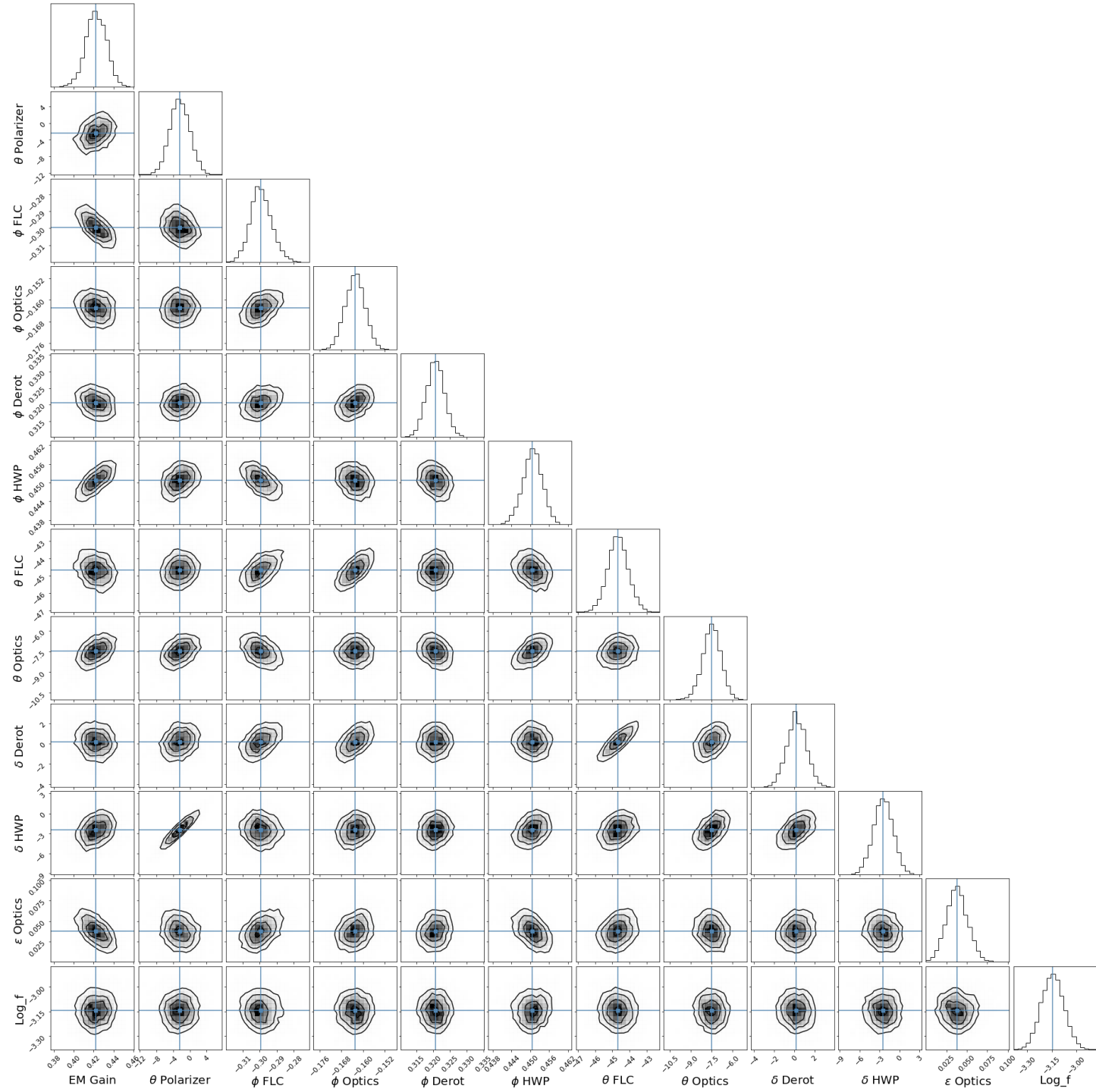


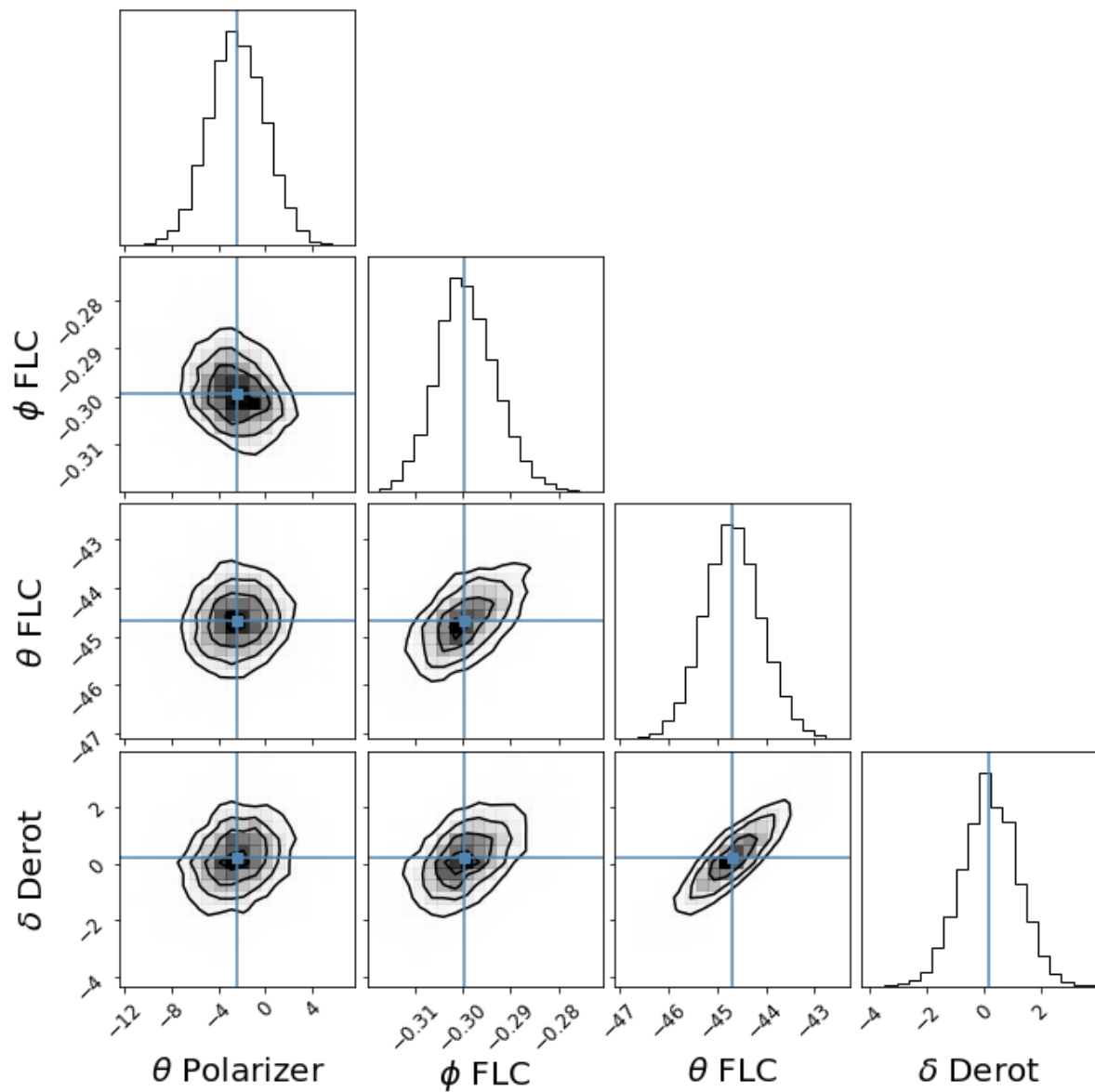
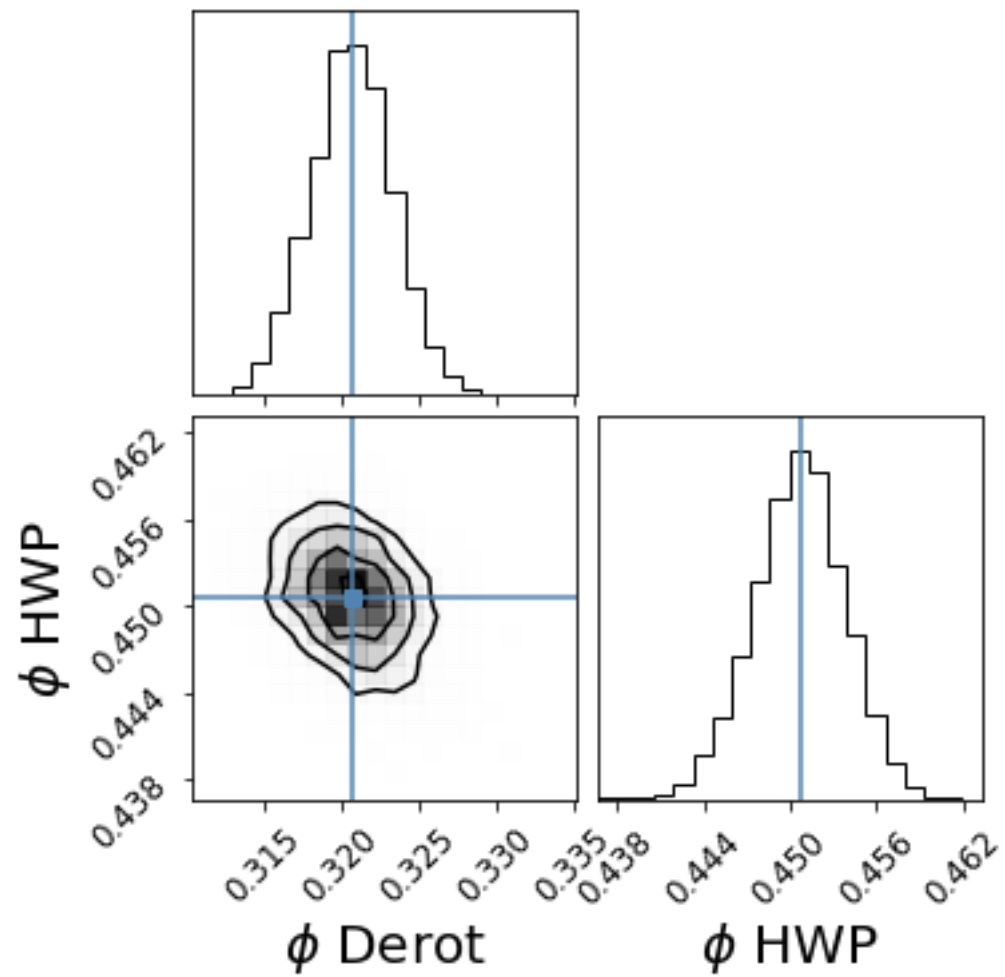
Double Difference: 675 nm



Double Sum: 675 nm

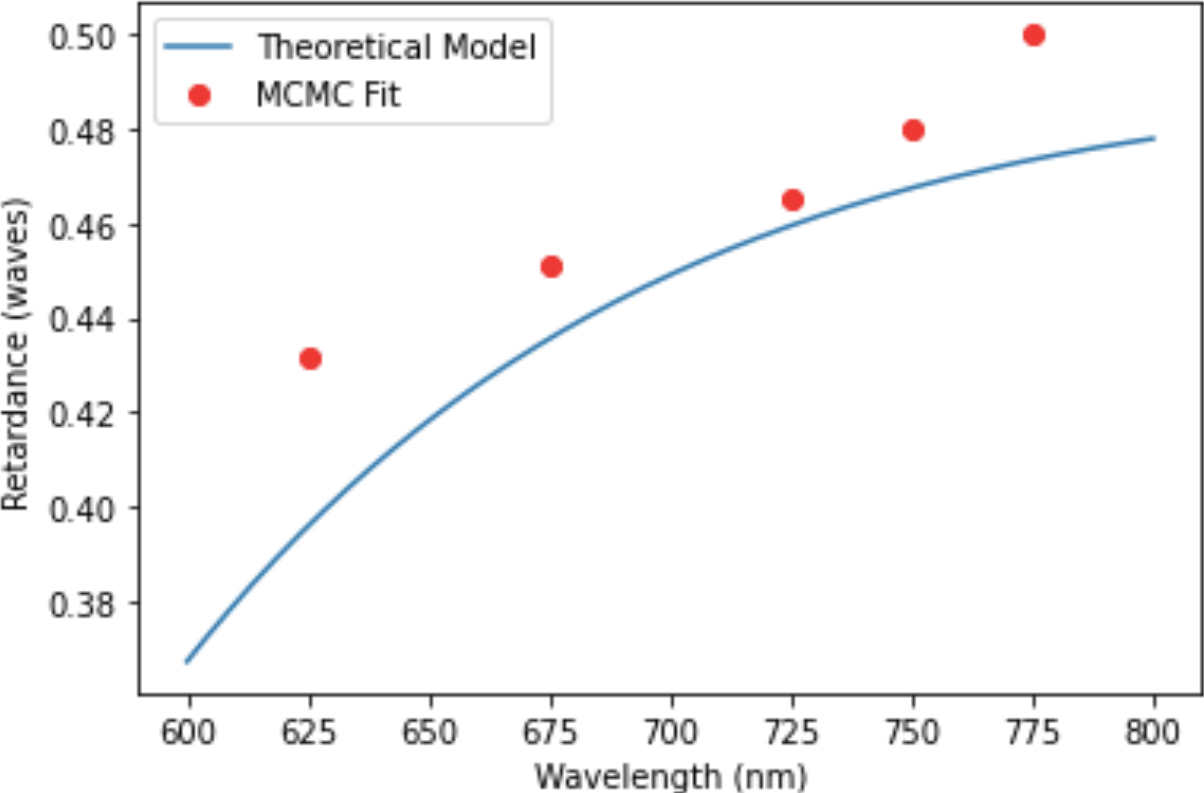




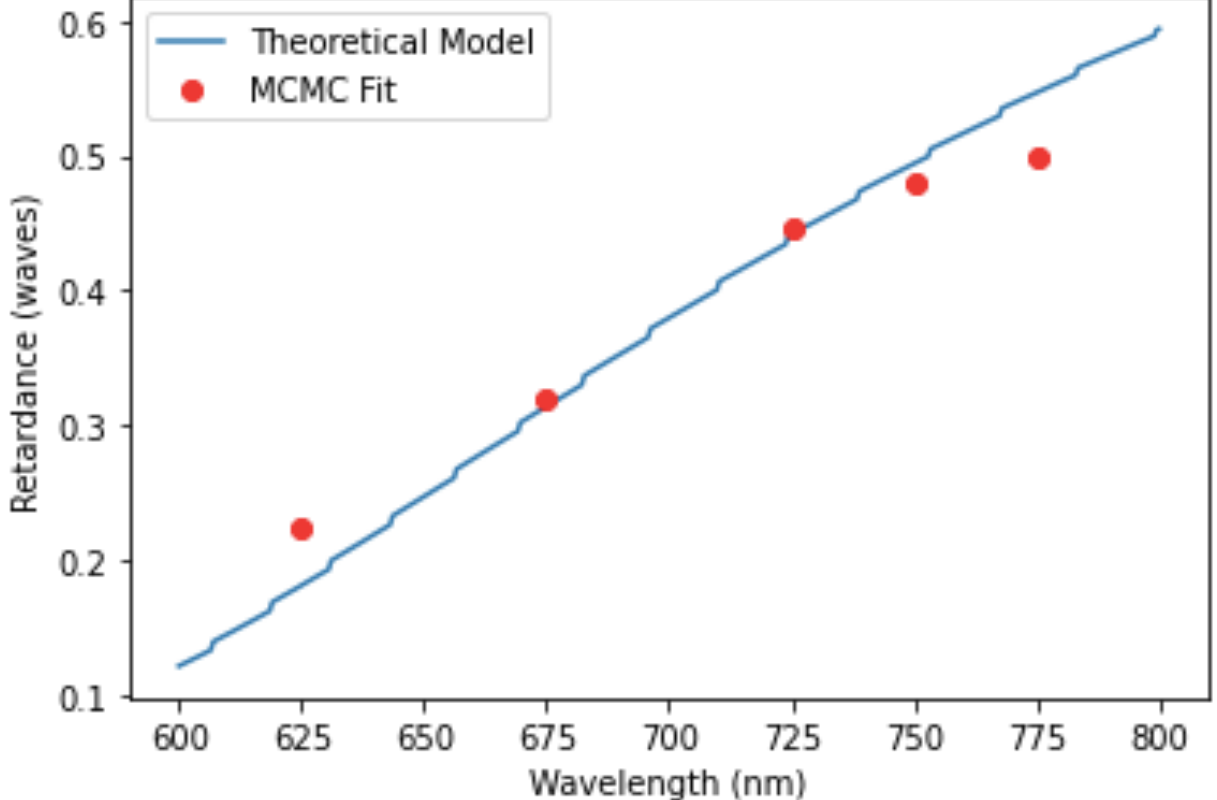


HWP and IMR Performance

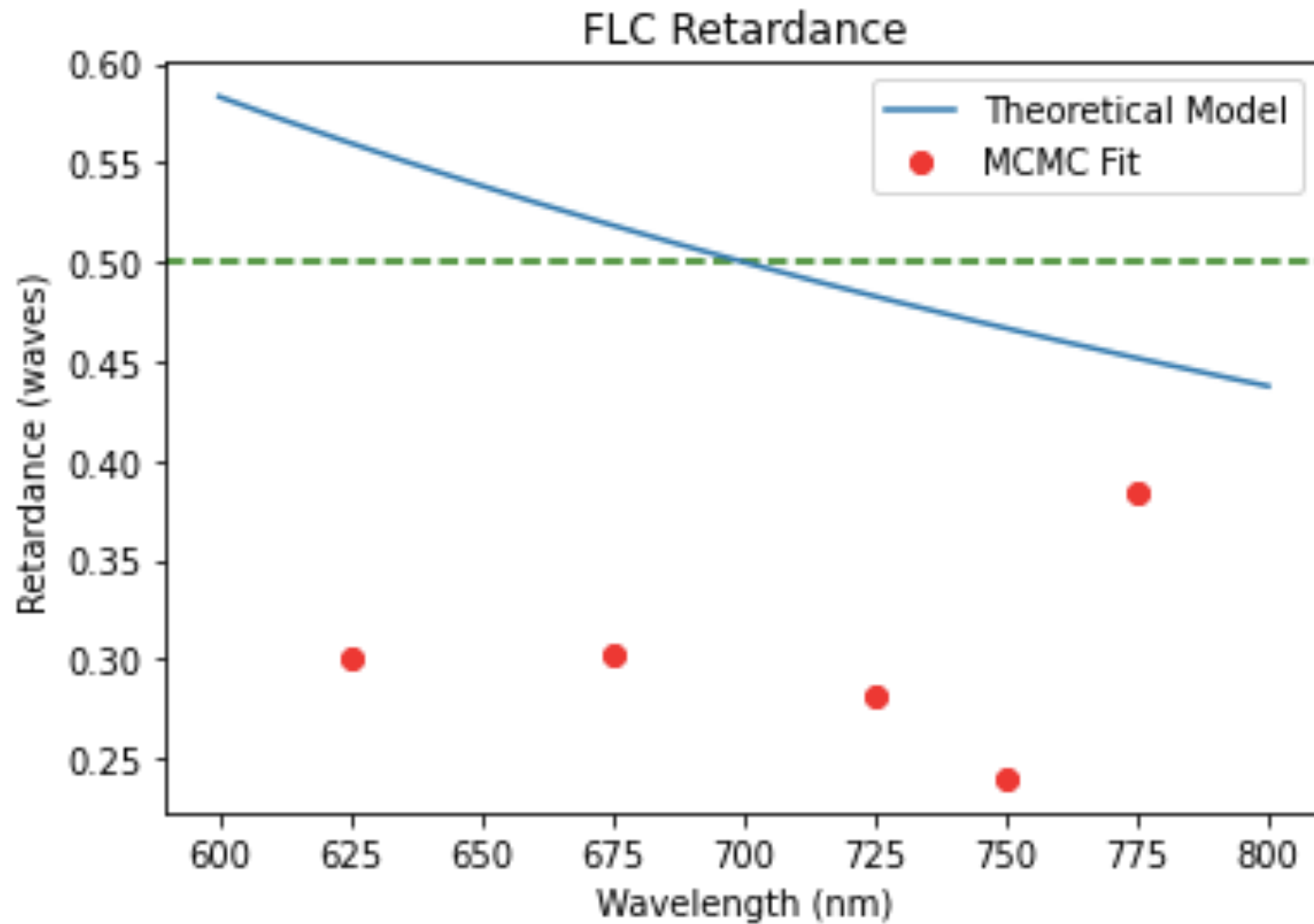
HWP Retardance



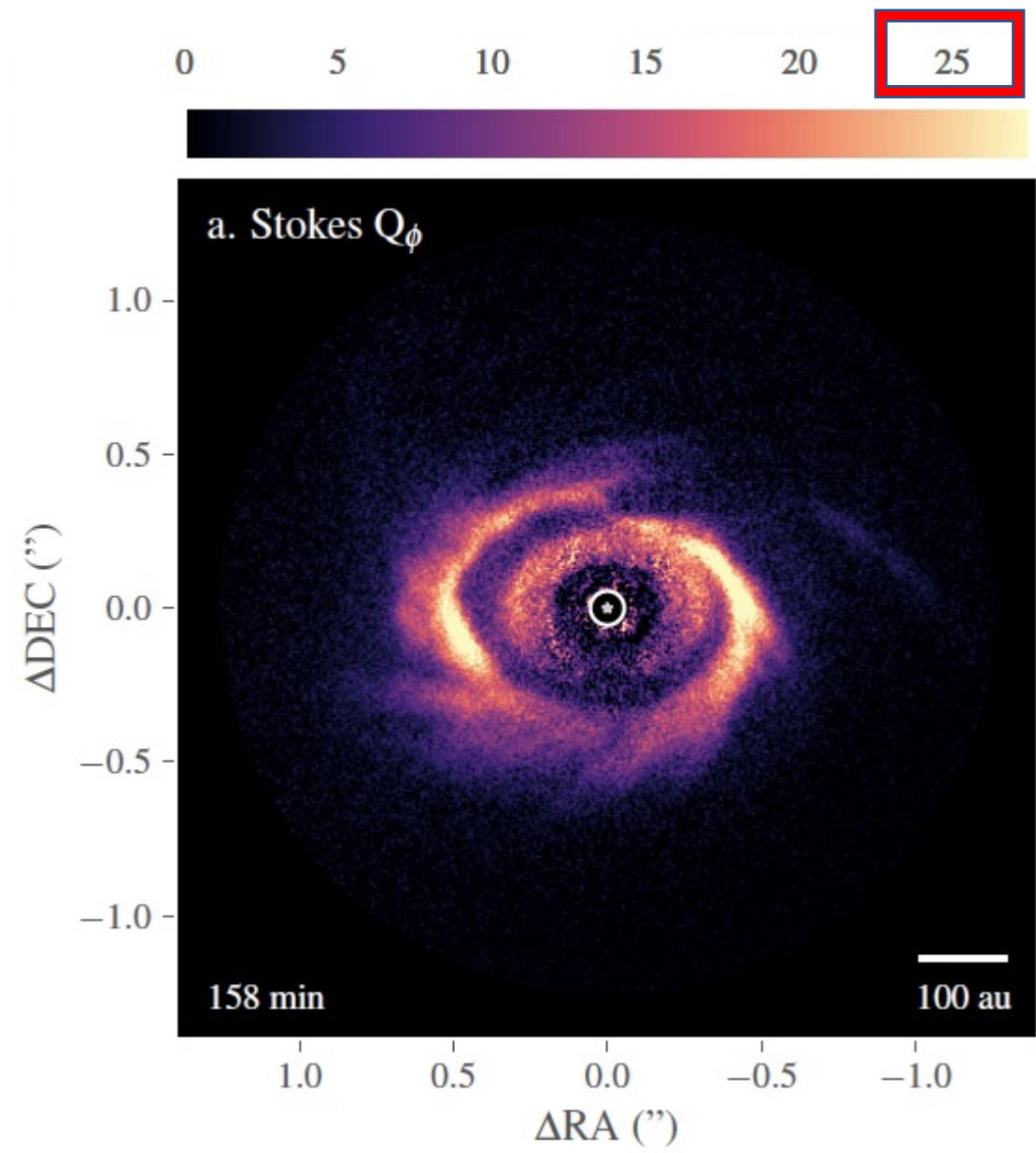
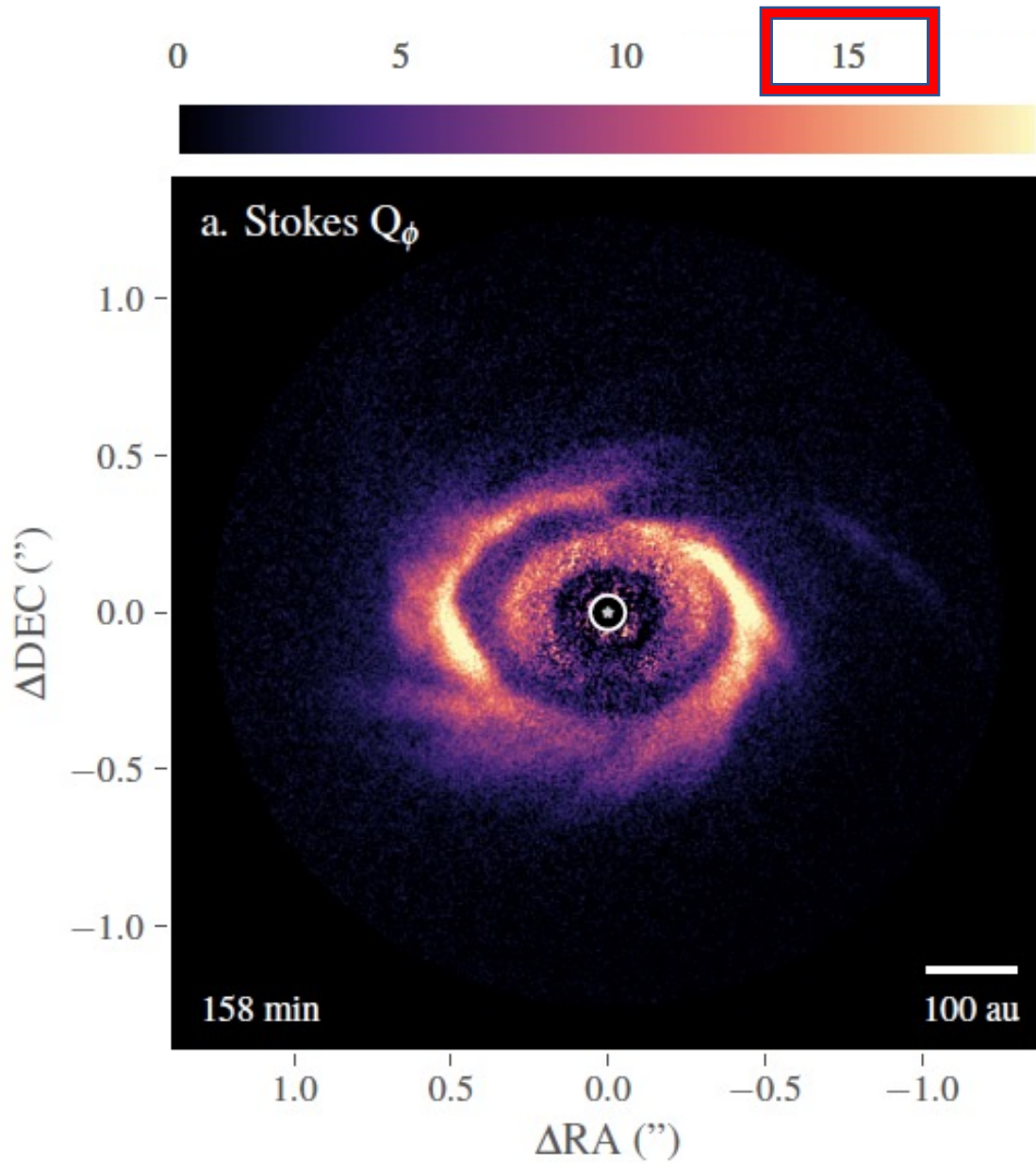
IMR Retardance



FLC Performance



HD34700



Internal Lab Calibrations: Takeaways

- Highly non-ideal and wavelength-dependent behaviour
- Confirmation of HWP and IMR retardance physical models
- Confirmation of anomalous behaviour at 625 and 775 nm
- Many sources of degeneracy
- FLC retardance deviates significantly from $1/2$ wave
- Camera EM gain drift

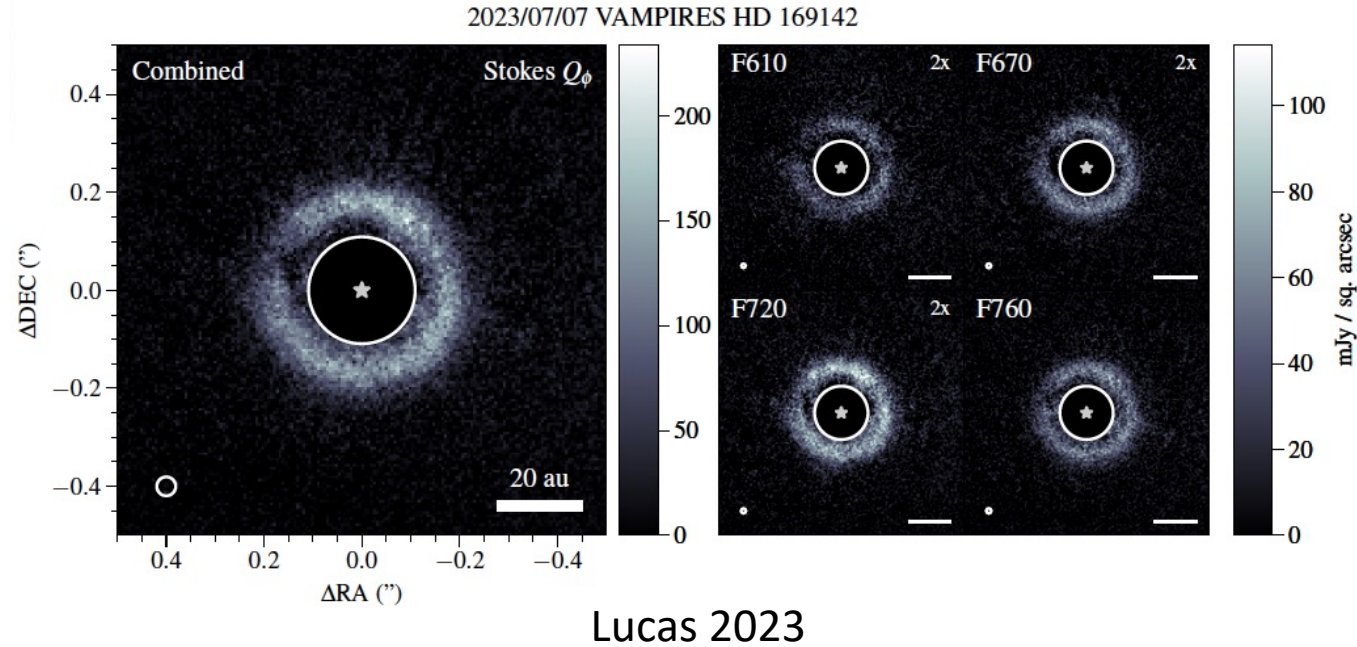
Conclusions

- Retroactive parameter extraction is time-consuming
 - Isolated calibrations for each component is invaluable
- Regular lab and on-sky calibrations are needed to track IP changes

Next Steps

- Determination of diattenuation and retardance of M3
- Verification of polarized standards
- Developing a calibration routine
- Apply on more science data!

VAMPIRES 2023 Upgrade



- New multiband imaging mode
- New achromatic FLC
- Some of the highest dynamic range of any SCExAO instruments